

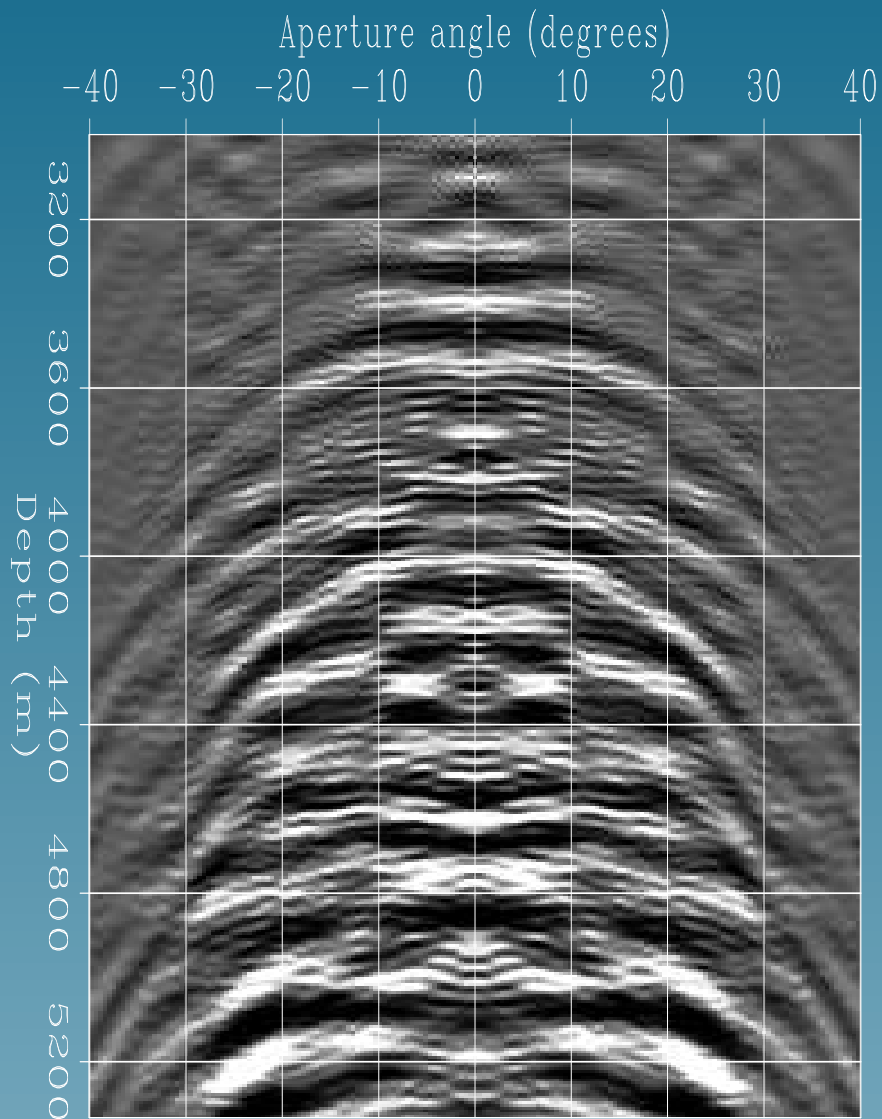
Multiples in Image Space

Gabriel Alvarez

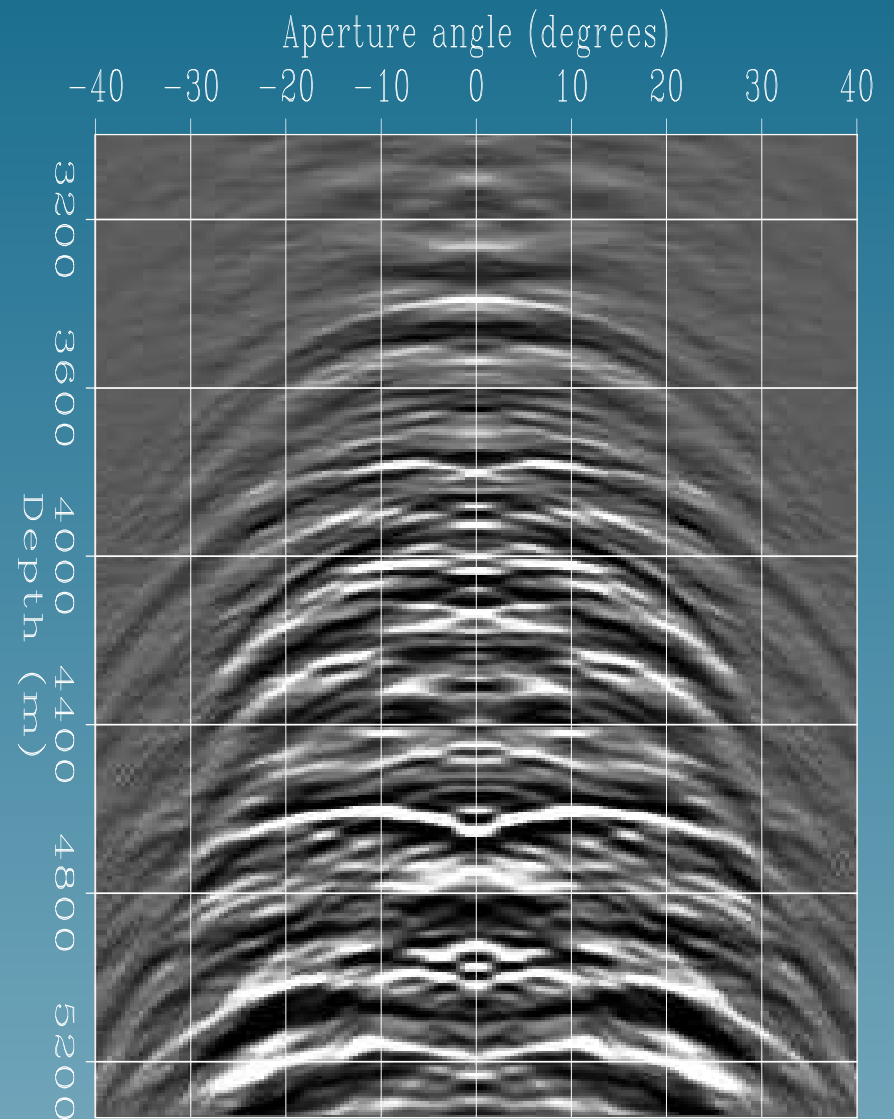
SEP120 pages: 365-376

Email: gabriel@sep.stanford.edu

From Last Year



(a) ADCIG 6744 m



(b) ADCIG 6744 m. Multiples 3D transform

Residual Moveout (RMO) Equation

Biondi and Symes (2004) residual moveout equation:

$$\Delta \mathbf{n}_{RMO} = (\rho - 1) \tan^2 \gamma z_0 \mathbf{n}$$

where:

\mathbf{n} : unit normal to the reflector.

ρ : true slowness/migration slowness.

γ : true half-aperture angle.

Aproximations of RMO Equation

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- Flat reflectors

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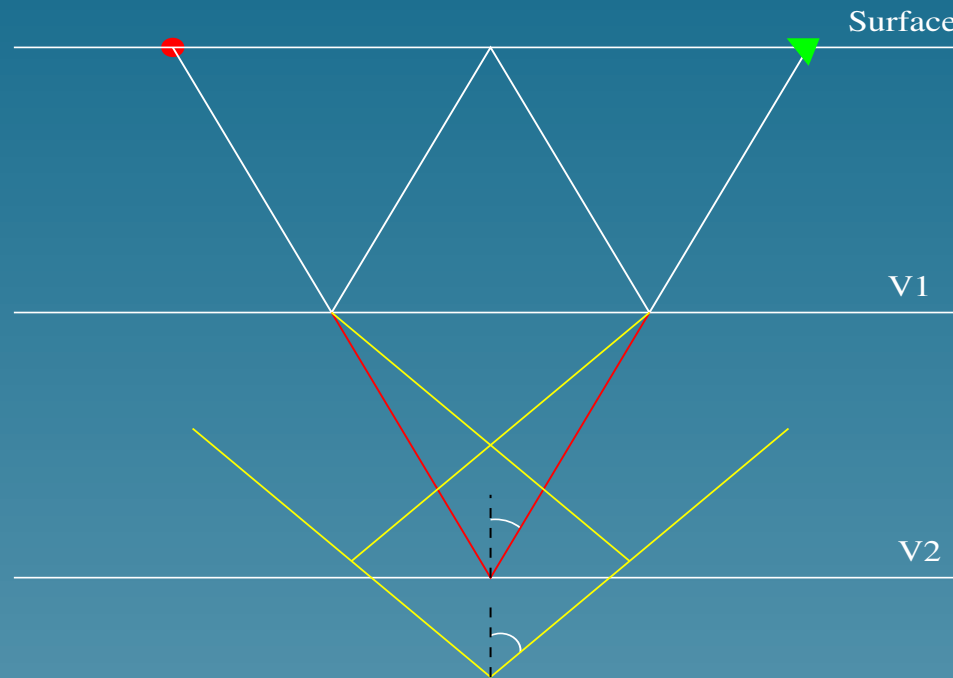
- Flat reflectors
- Rays are stationary: apparent angles taken as equal to true angles.

Aproximations of RMO Equation

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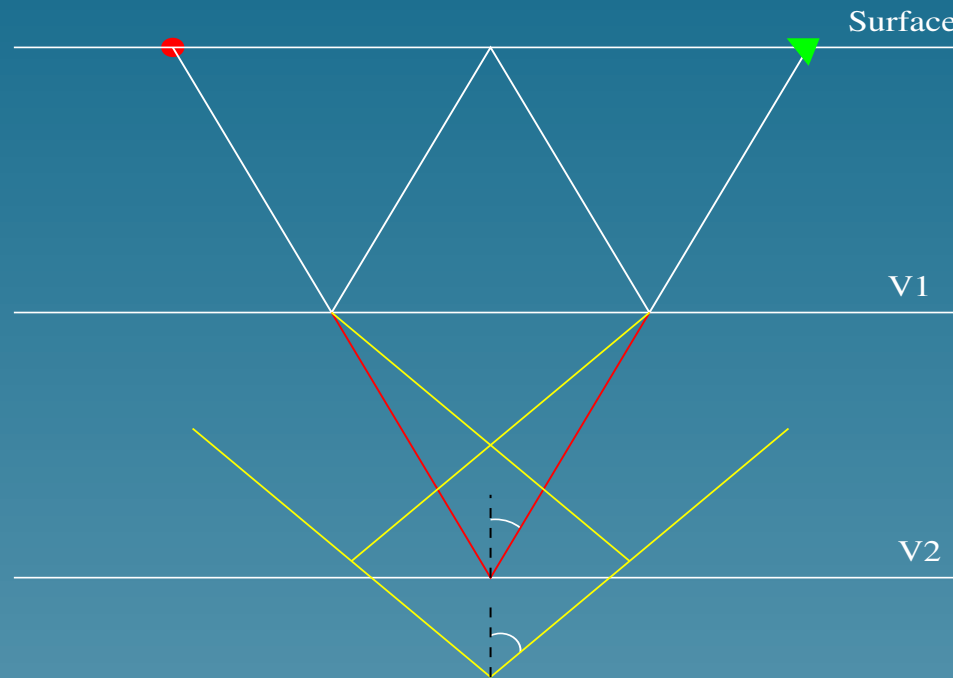
- Flat reflectors
- Rays are stationary: apparent angles taken as equal to true angles.
- ρ is small.

RMO approximation for Multiples



For water-bottom multiples $V_2 \gg V_1$ so apparent aperture angle may be significantly different than true aperture angle and ρ is not close to one.

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What about diffracted multiples?

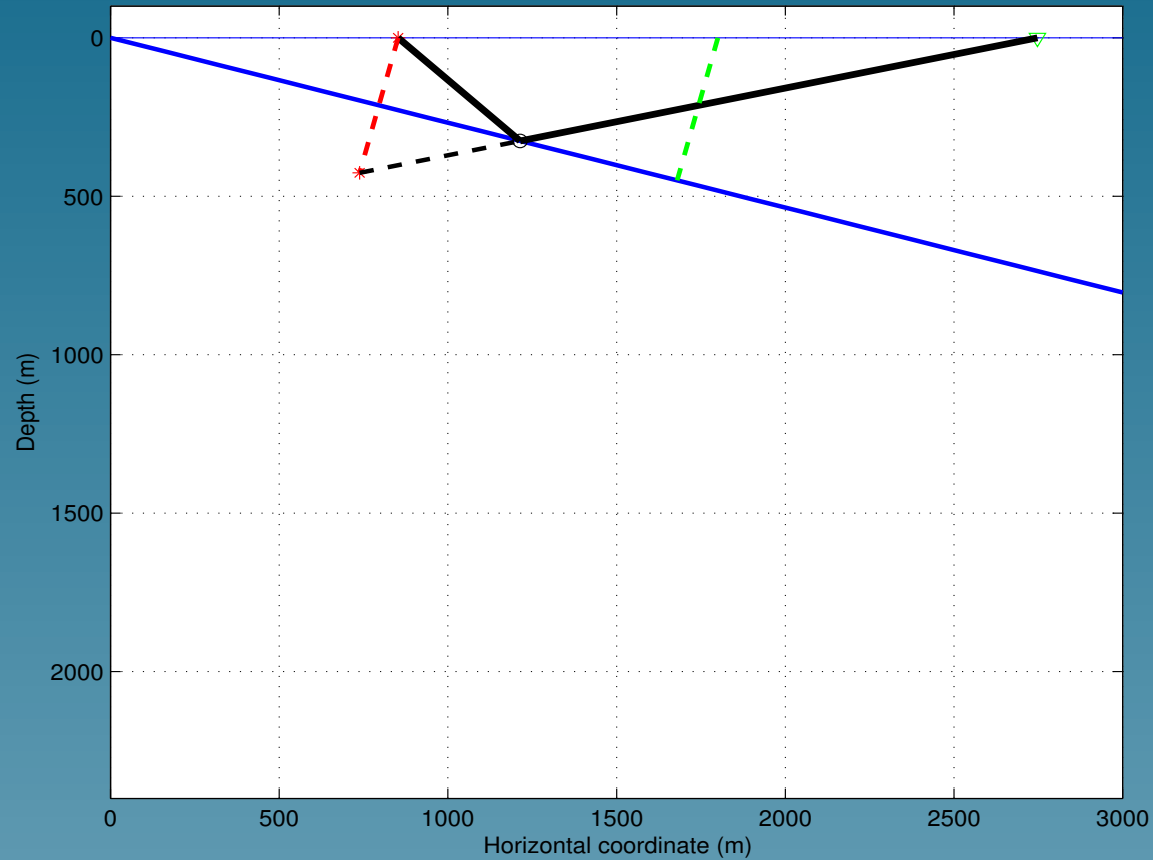
Motivation

- Understand the residual moveout of multiples in image space when migrated with the velocity of the primaries.

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- Understand the residual moveout of multiples in image space when migrated with the velocity of the primaries.
- Use the residual moveout to design the appropriate Radon transform to attenuate the multiples in the image space.

Raypath of Primary



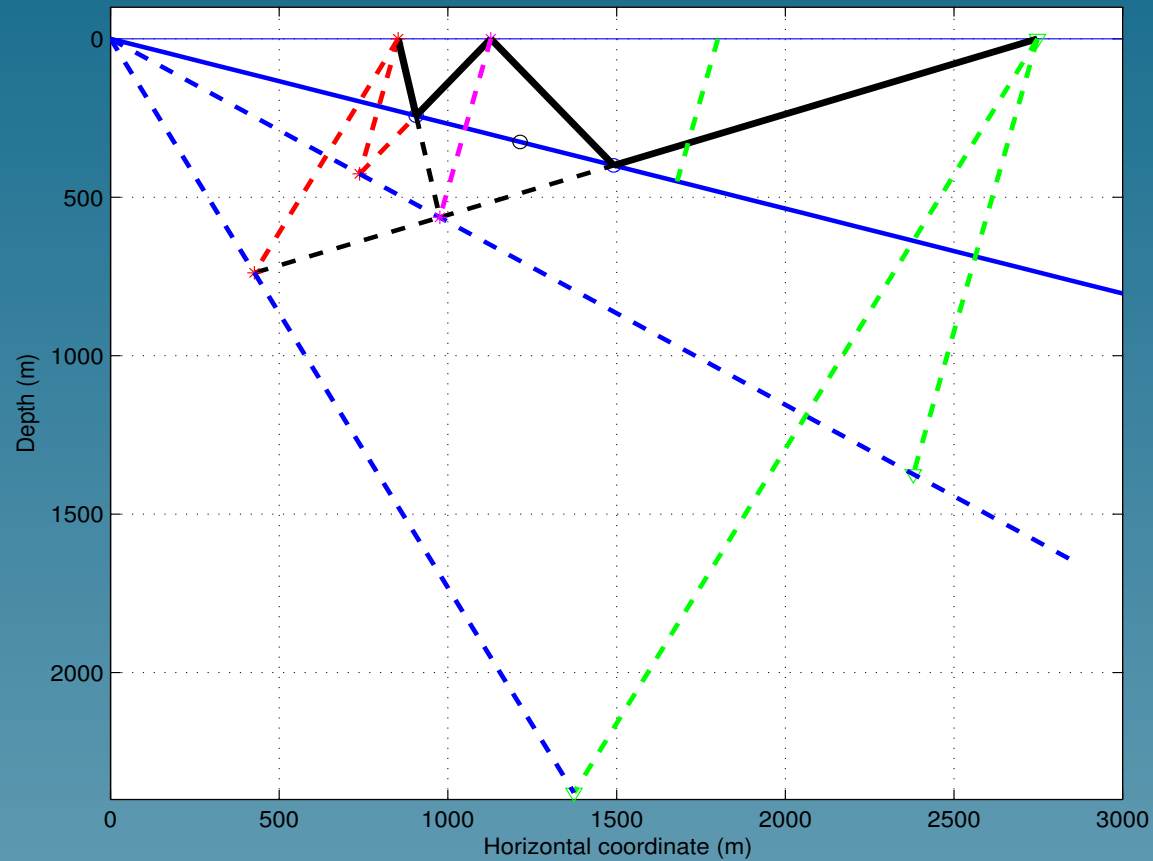
$$t_p(h_D) = \sqrt{t_p^2(0) + \left(\frac{2h_D}{V_{NMO}}\right)^2}$$

$$V_{NMO} = \frac{V}{\cos \varphi}$$

h_D : half-offset

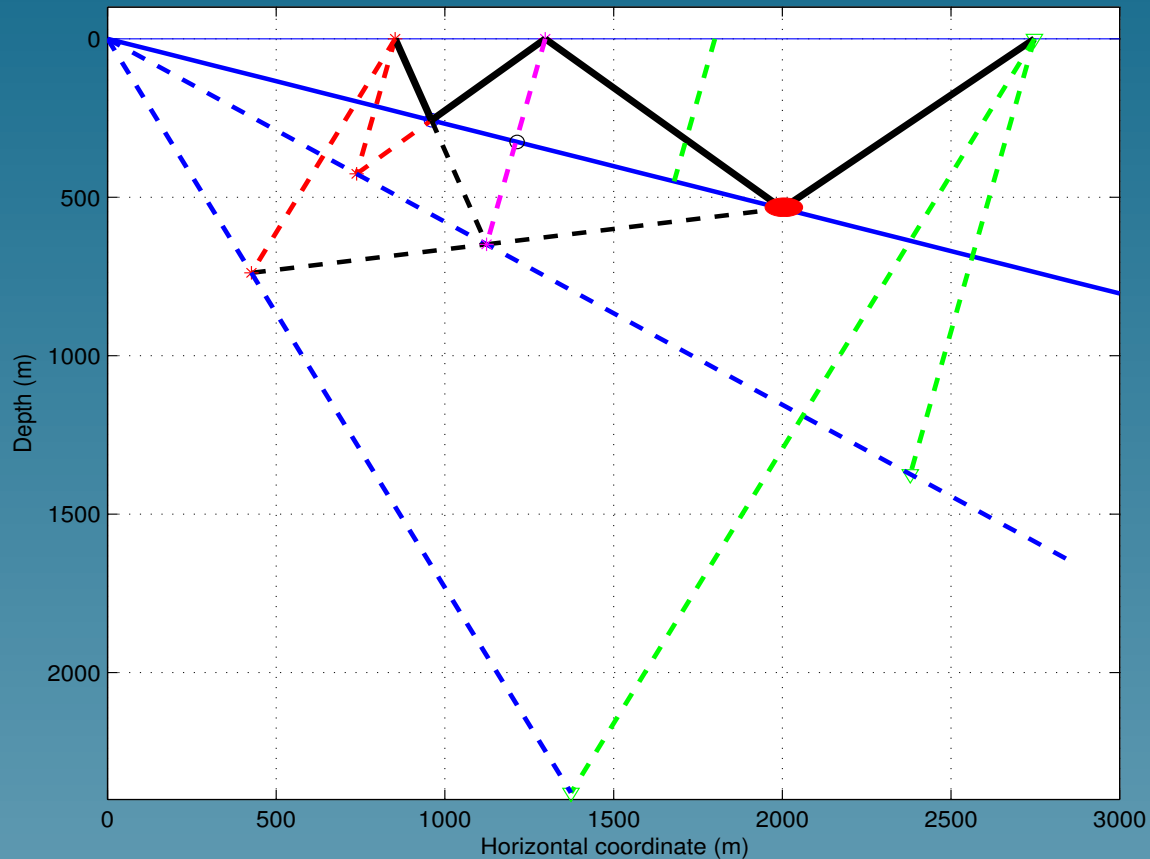
φ : reflector dip

Raypath of Water-bottom Multiple



$$t_m(h_D) = \sqrt{t_m^2(0) + \left(\frac{2h_D}{\hat{V}_{NMO}}\right)^2} \quad \hat{V}_{NMO} = \frac{V}{\cos(2\varphi)}$$

Raypath of Diffracted Multiple

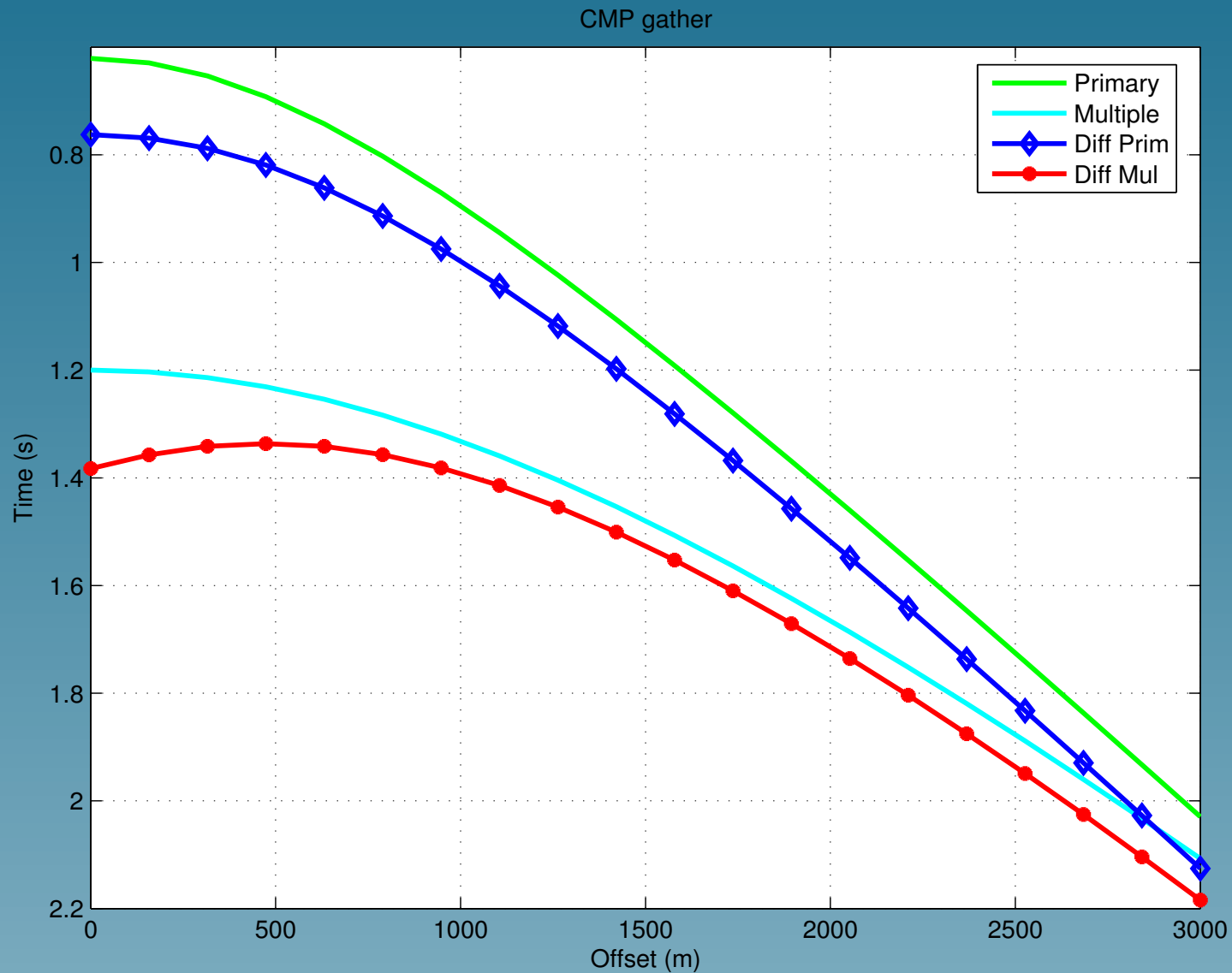


$$t_m(h_D) = \frac{2(Z_D - h_D \sin \varphi) \cos \varphi}{\cos(\beta_s + 3\varphi)} + \frac{z_d}{V \cos \beta_r}$$

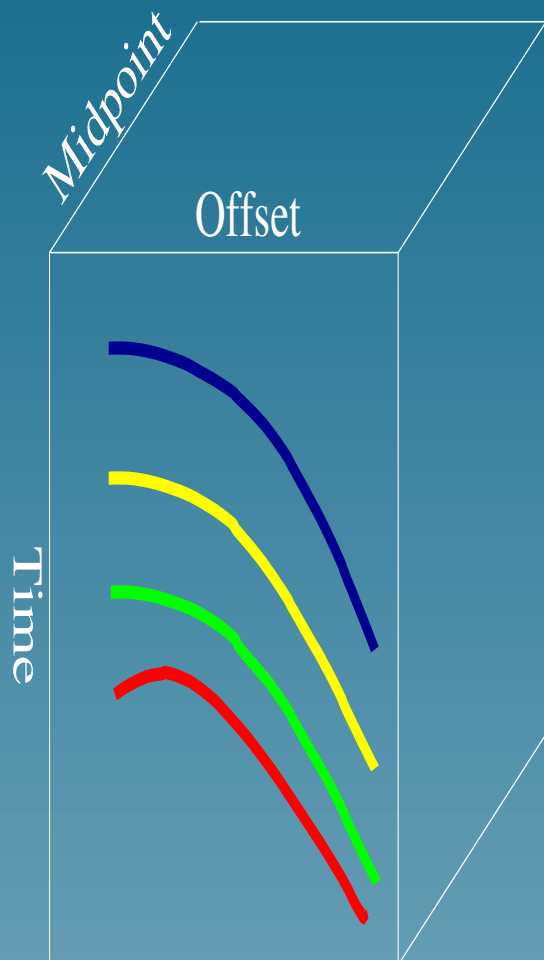
β_s, β_r : take-off angles

z_d : diffractor position

Moveouts on a CMP Gather



Schematic of Moveout of Multiples



Data space

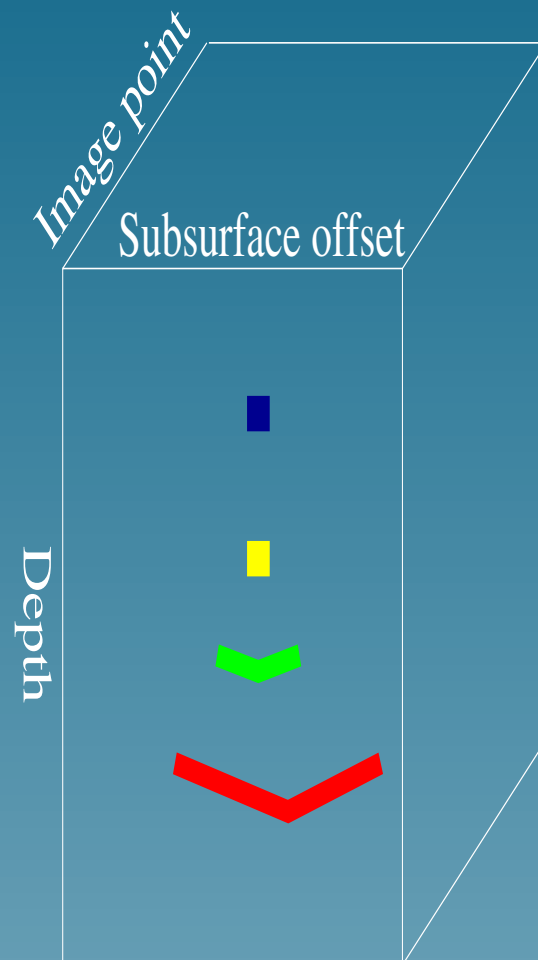


Image space

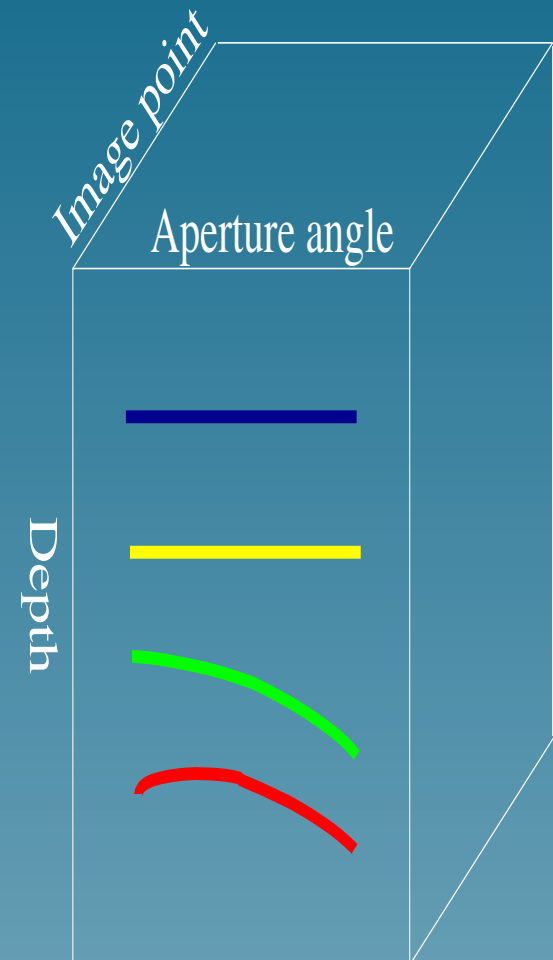


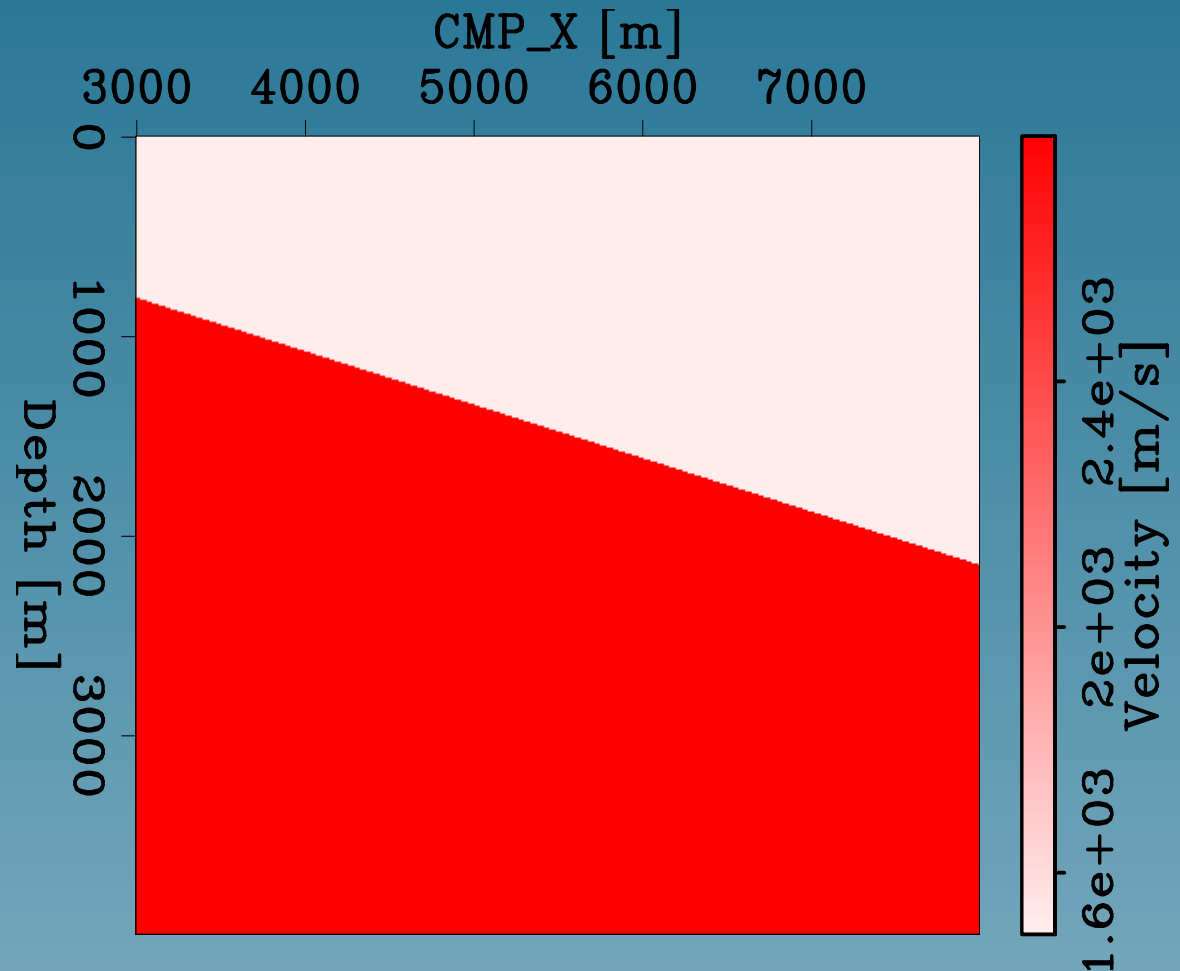
Image space

Example with 2-D Synthetic Dataset

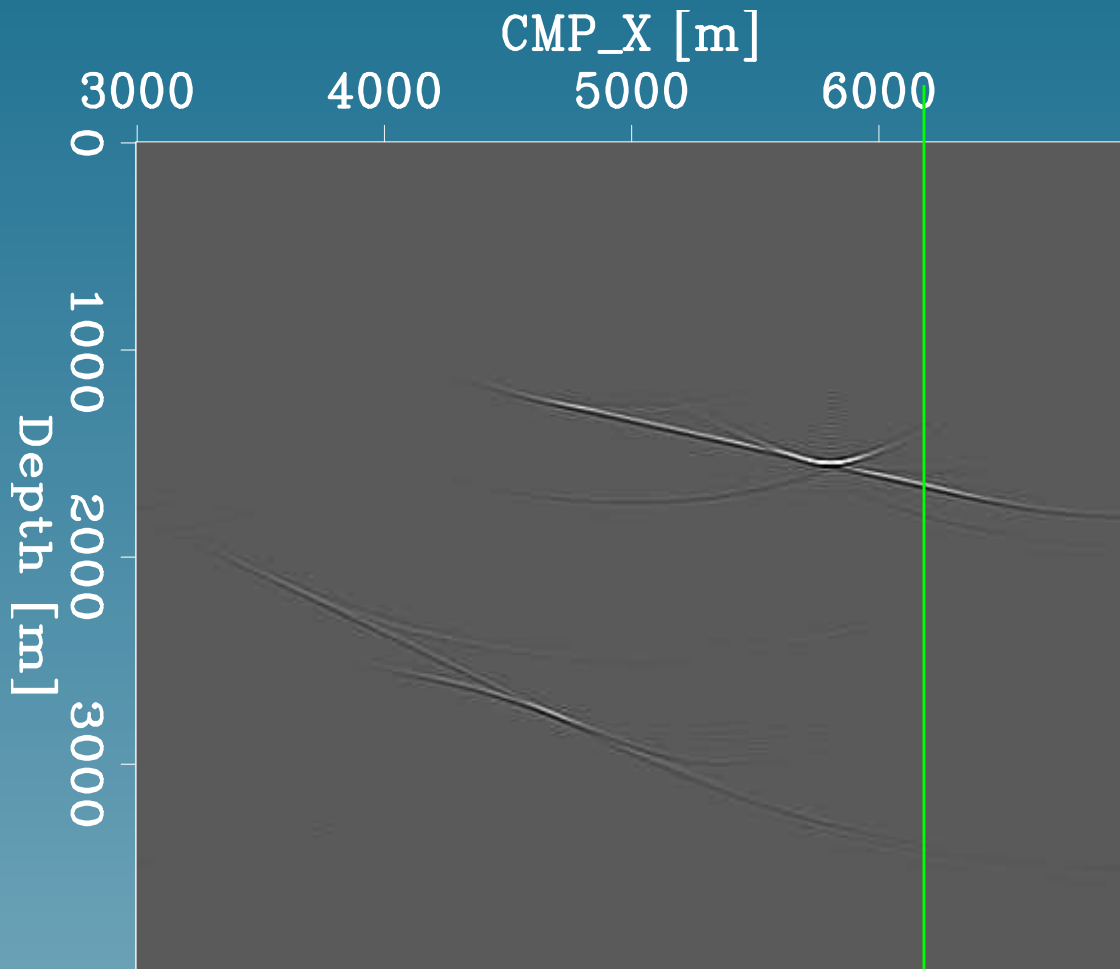
200 cmps
100 traces/cmp
0-2970 m offsets
20 m cmp interval

4 events:

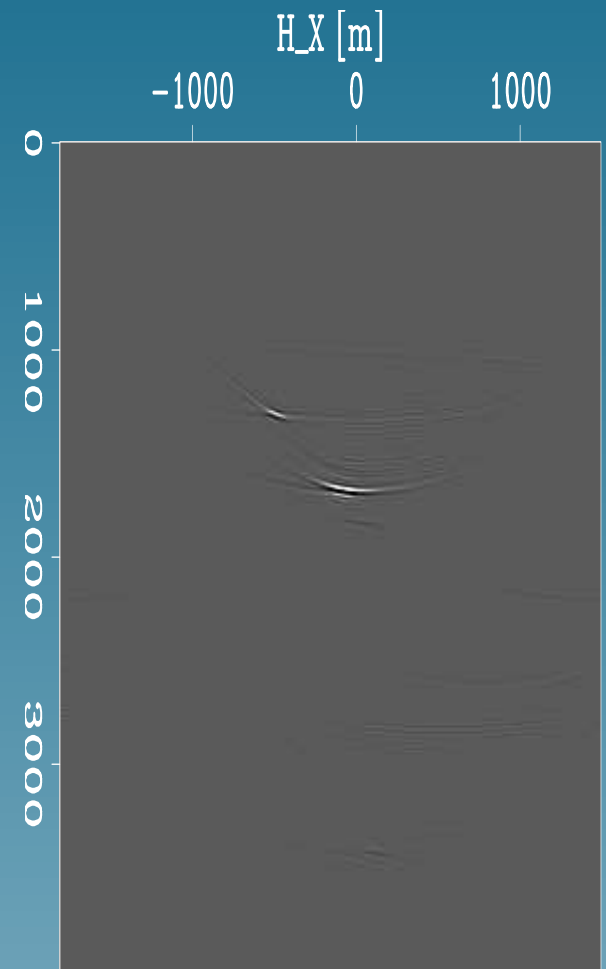
- ★ primary
- ★ wb multiple
- ★ primary diffraction
- ★ diffracted multiple



Primary. Two Velocities

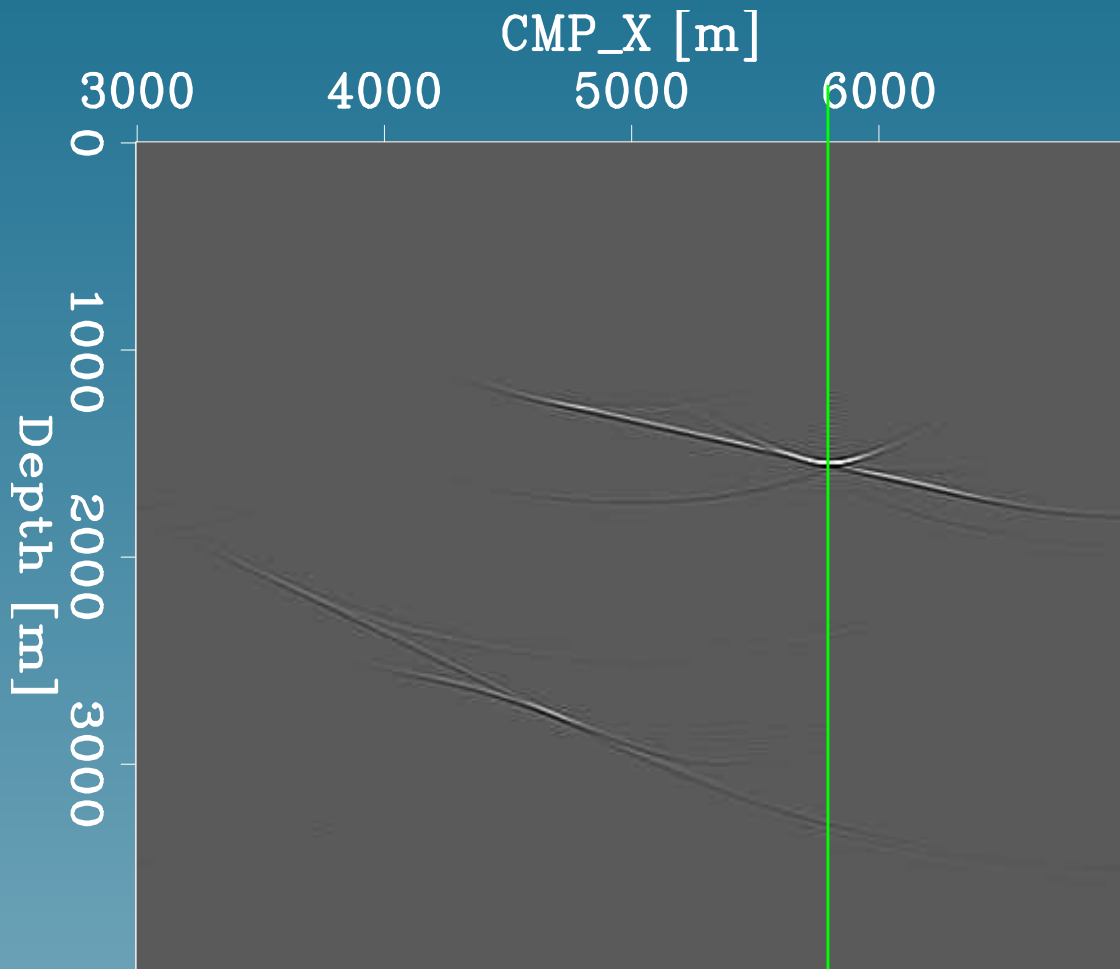


Zero subsurface-offset section



SOCIG ($x=6280$)

Diffraction. Two Velocities

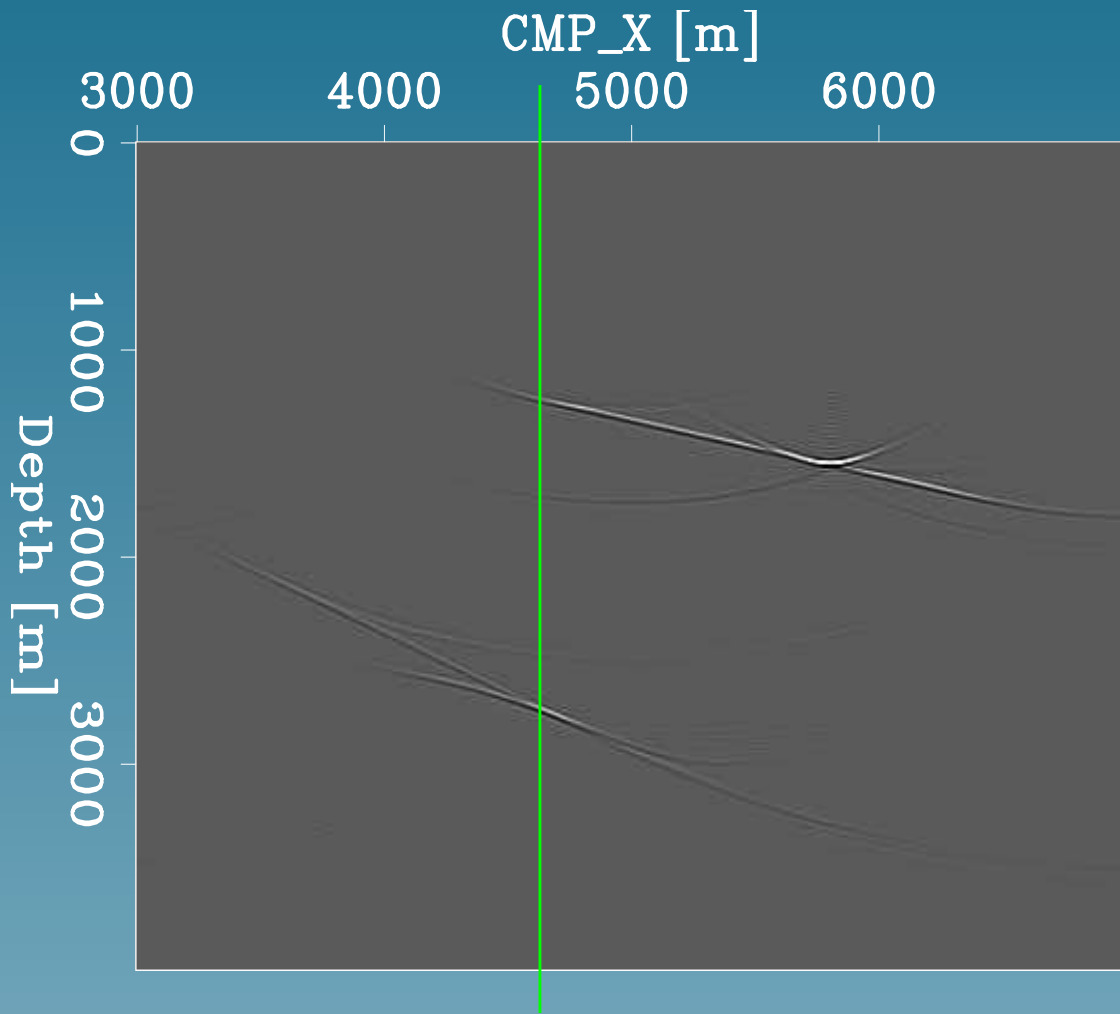


Zero subsurface-offset section

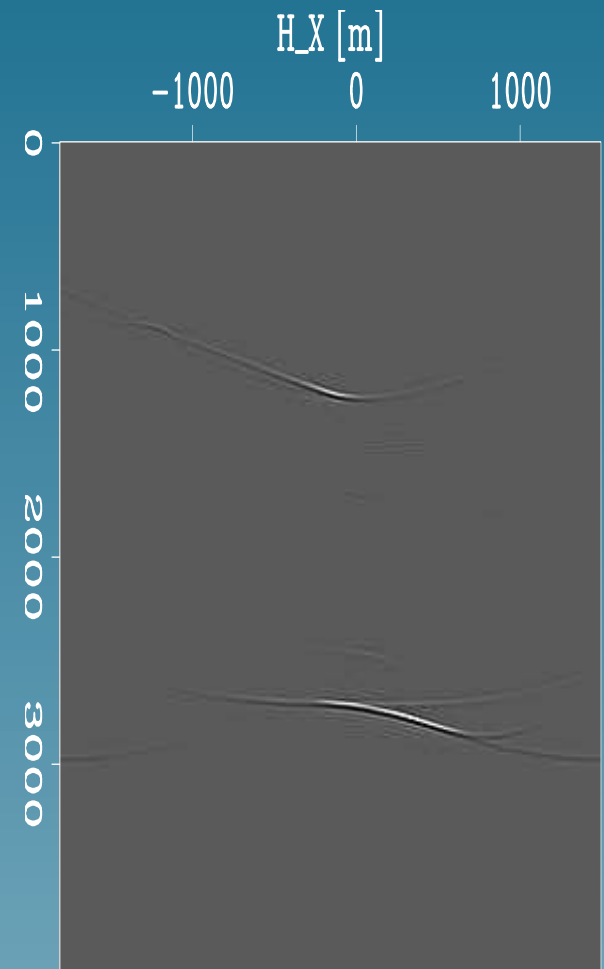


SOCIG ($x=5800$)

Diffracted Multiple. Two Velocities

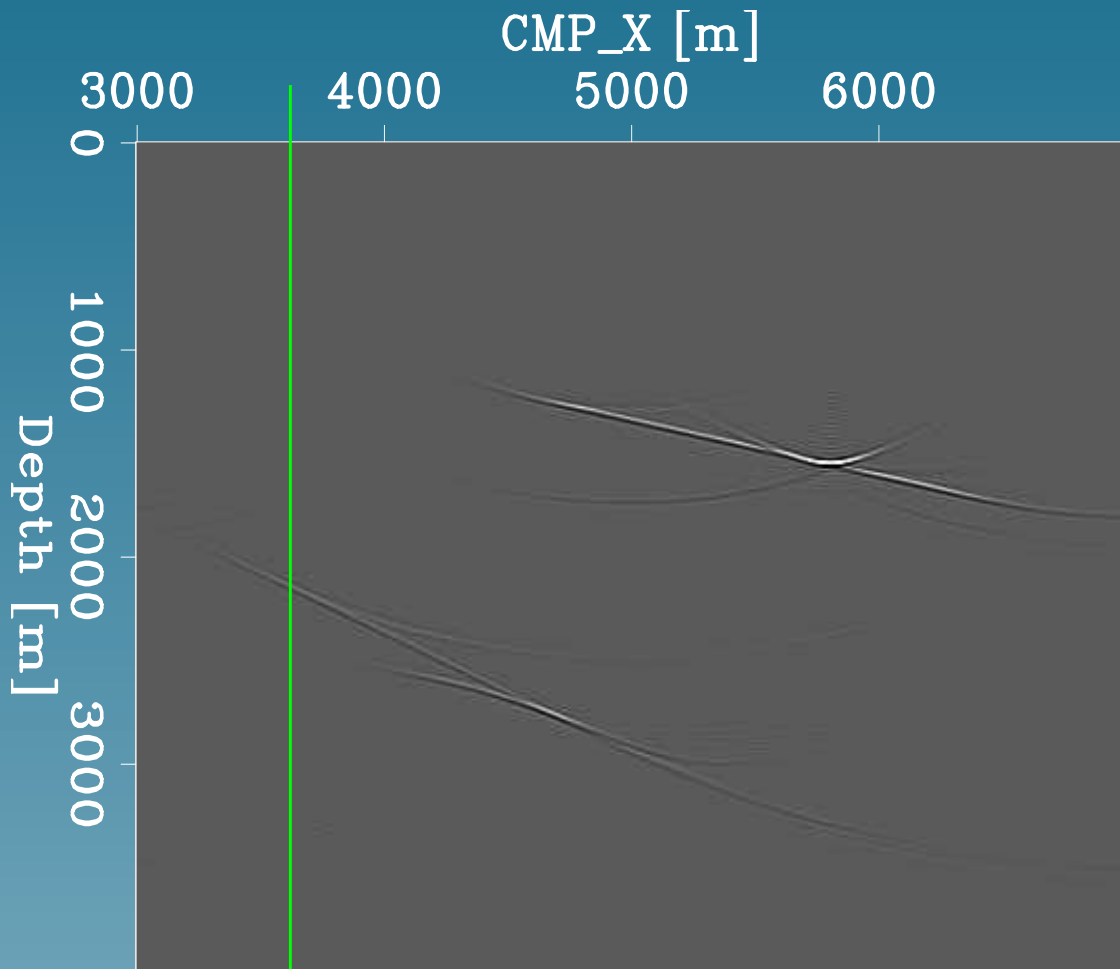


Zero subsurface-offset section

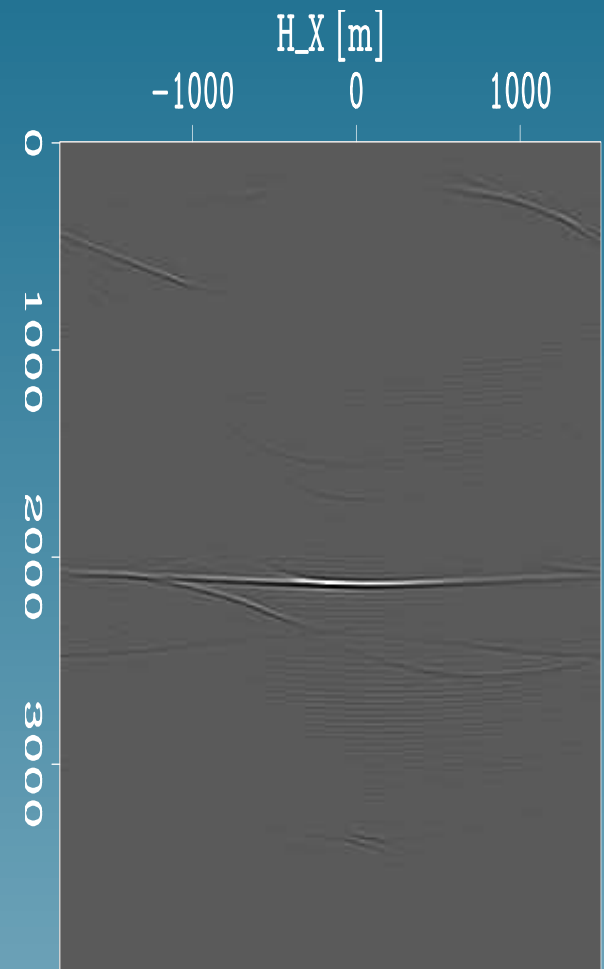


SOCIG ($x=4600$)

WB Multiple. Two Velocities

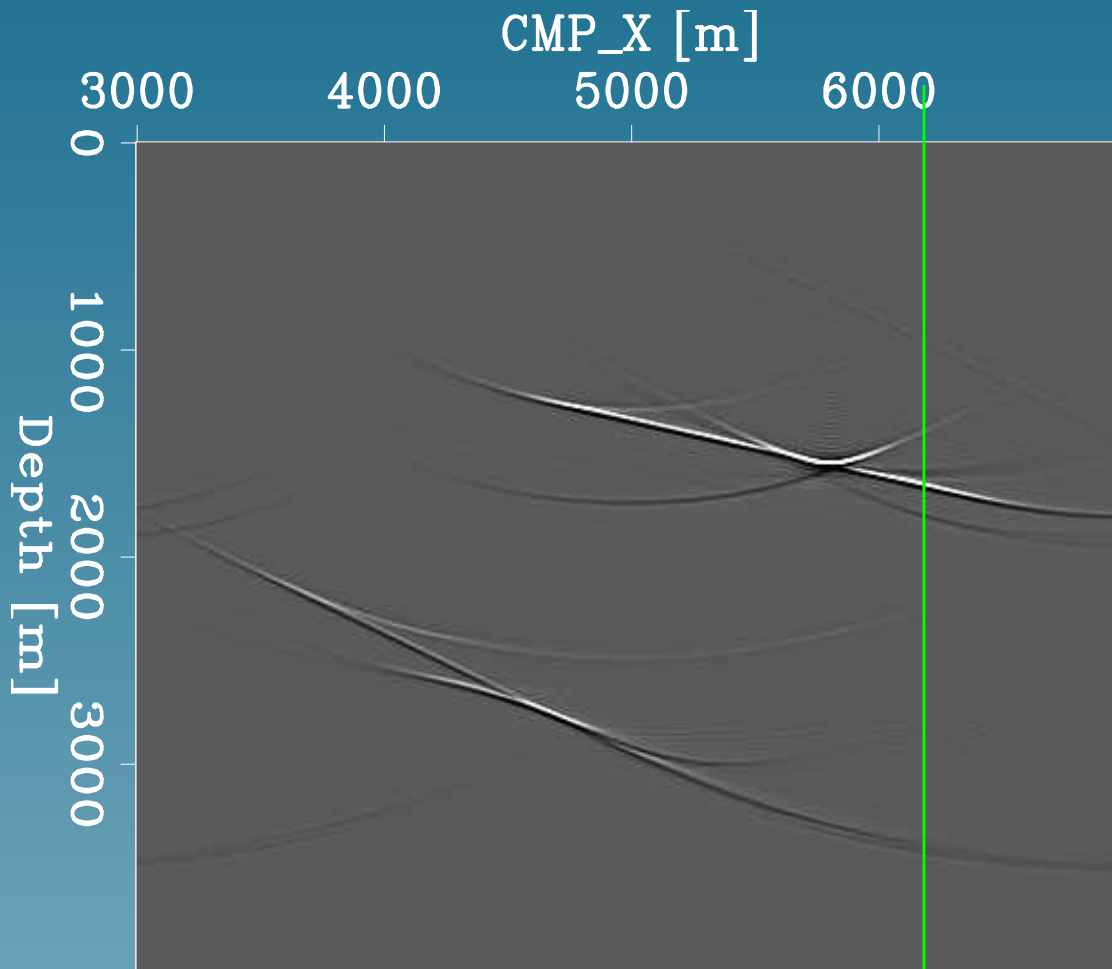


Zero subsurface-offset section

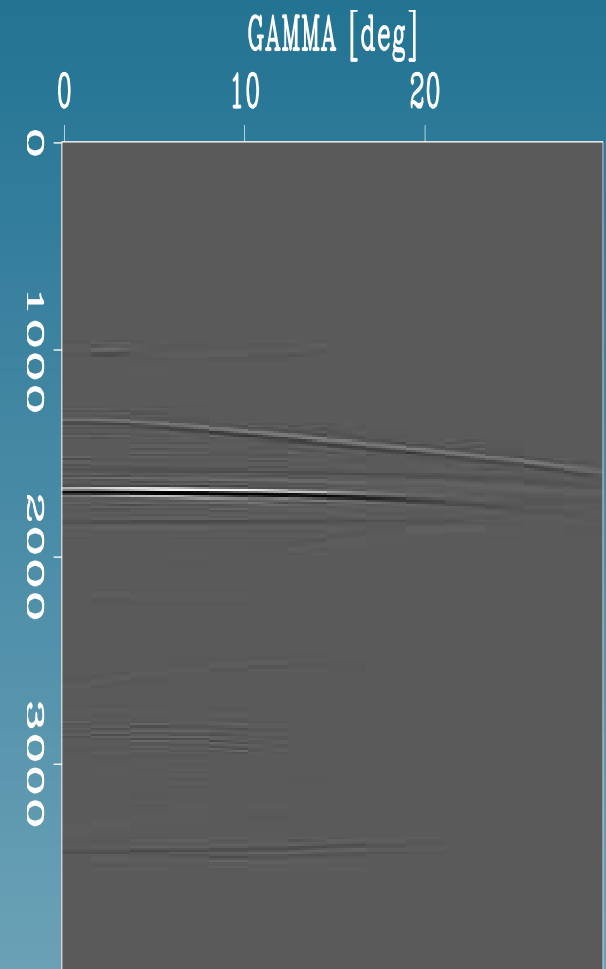


SOCIG ($x=3600$)

Primary. Two Velocities

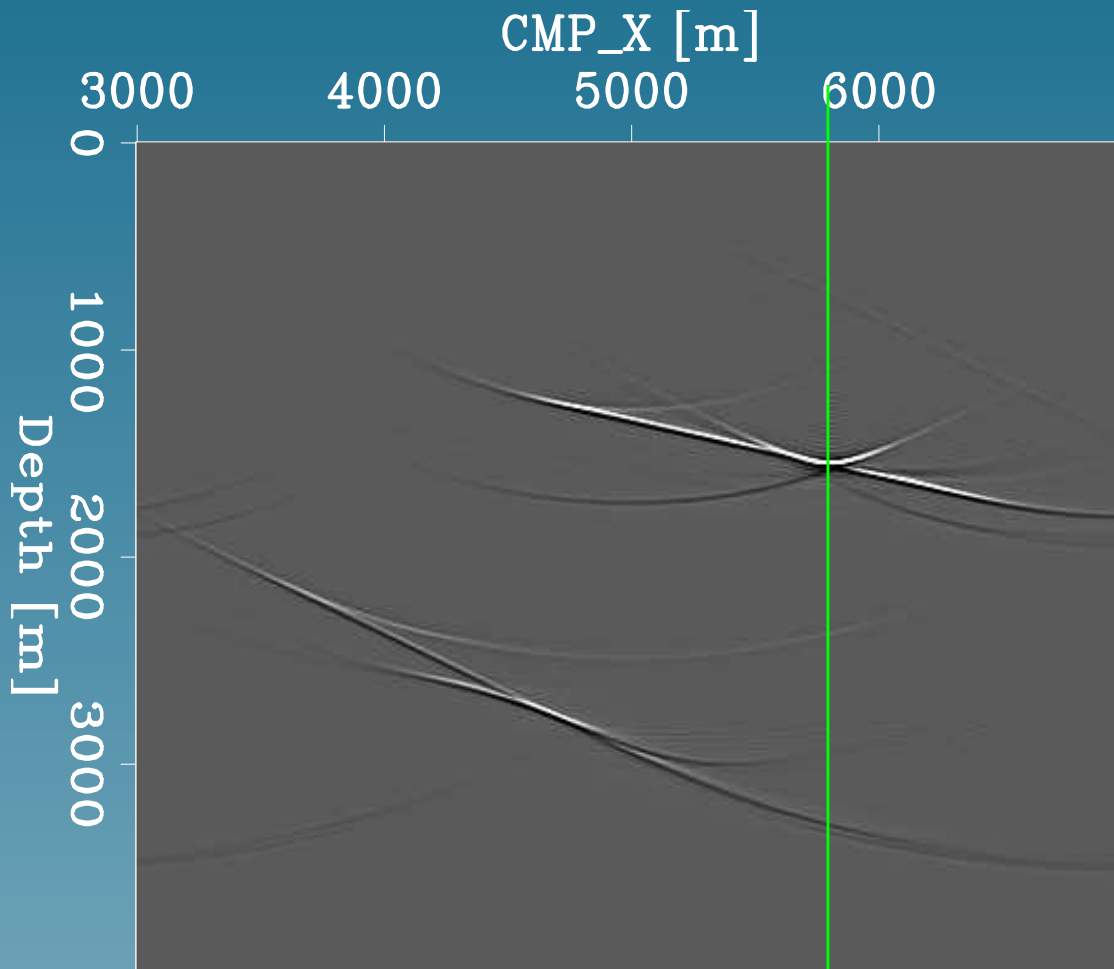


Angle stack

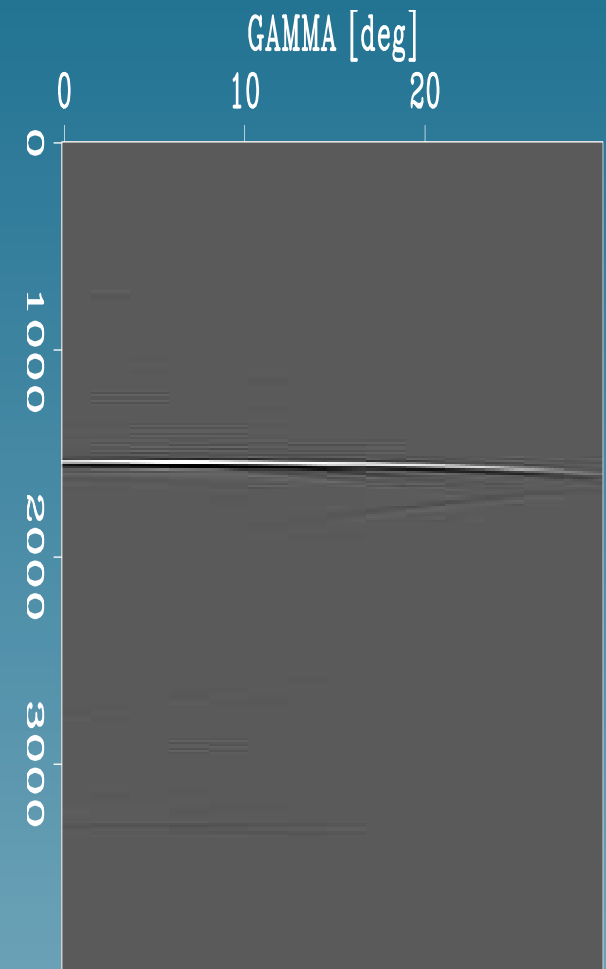


ADCIG (x=6280)

Diffraction. Two Velocities

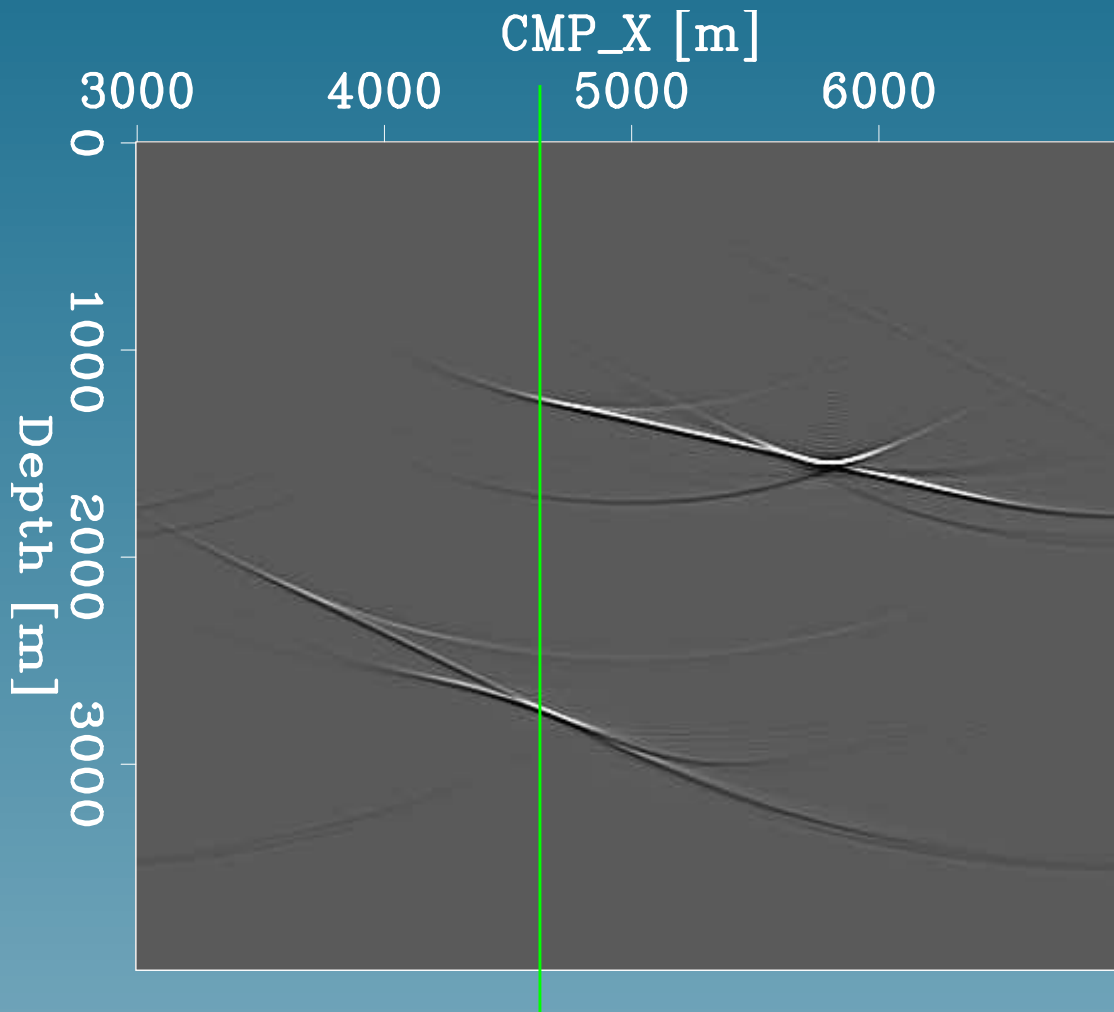


Angle stack

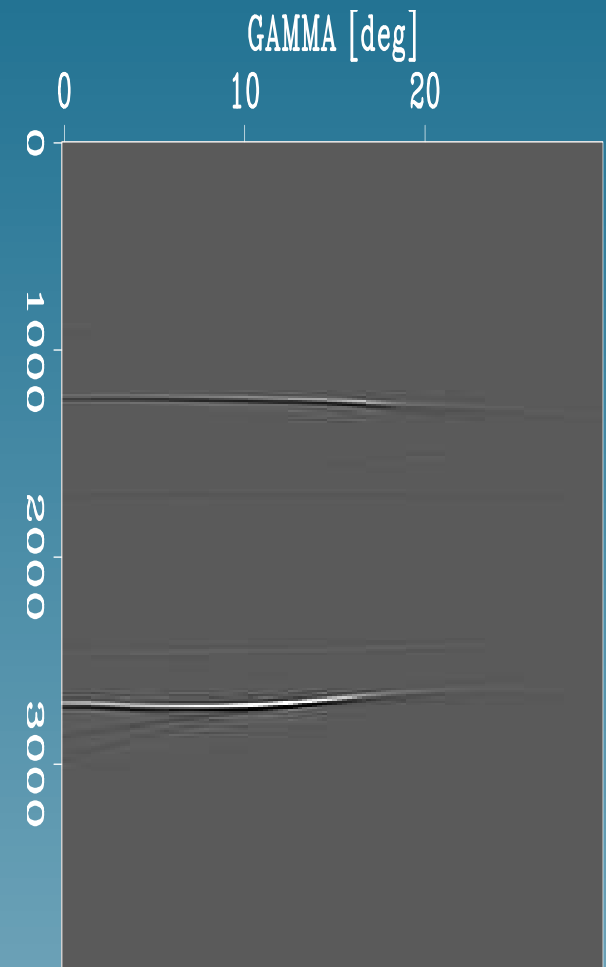


ADCIG ($x=5800$)

WB Multiple. Two Velocities

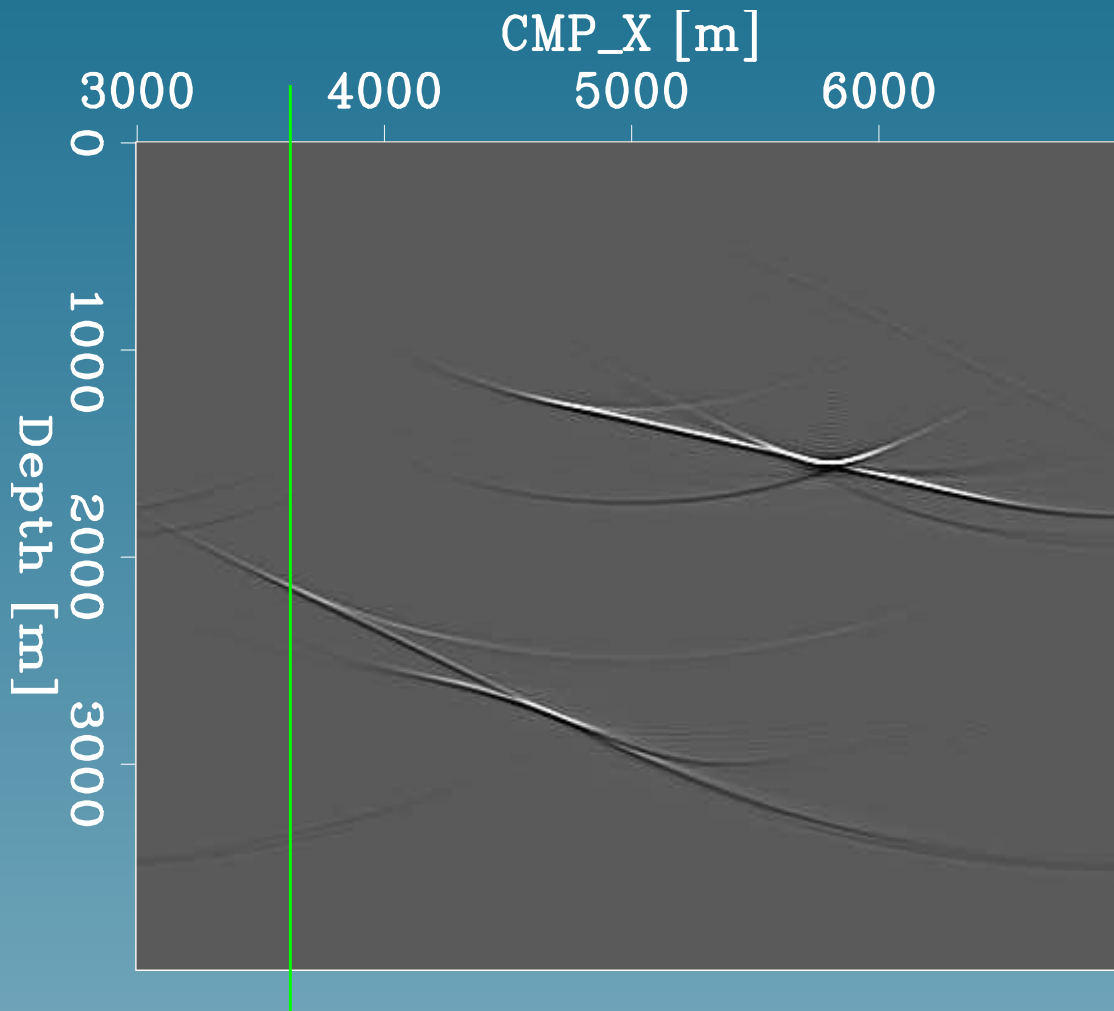


Angle stack

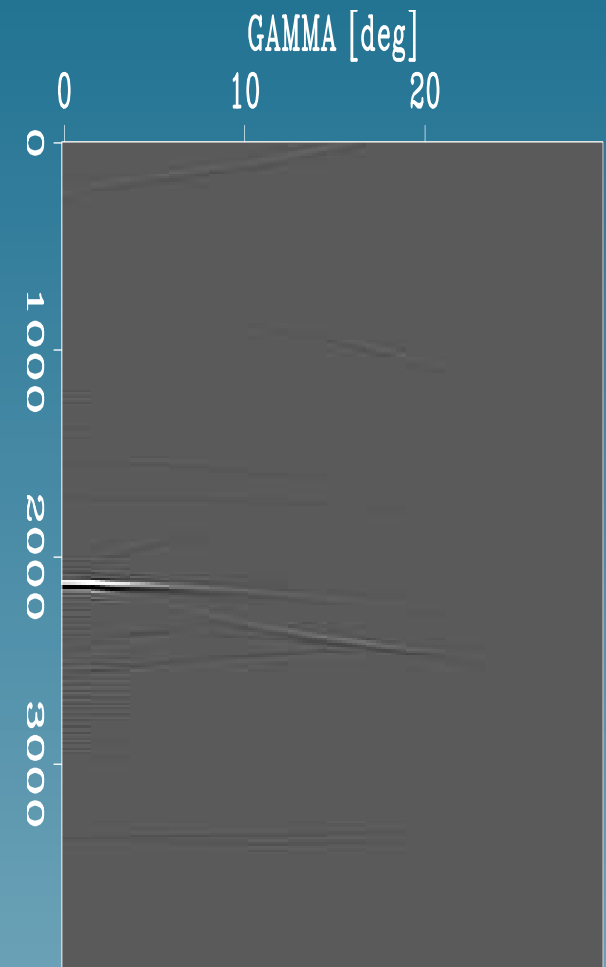


ADCIG (x=4600)

WB Multiple. Two Velocities

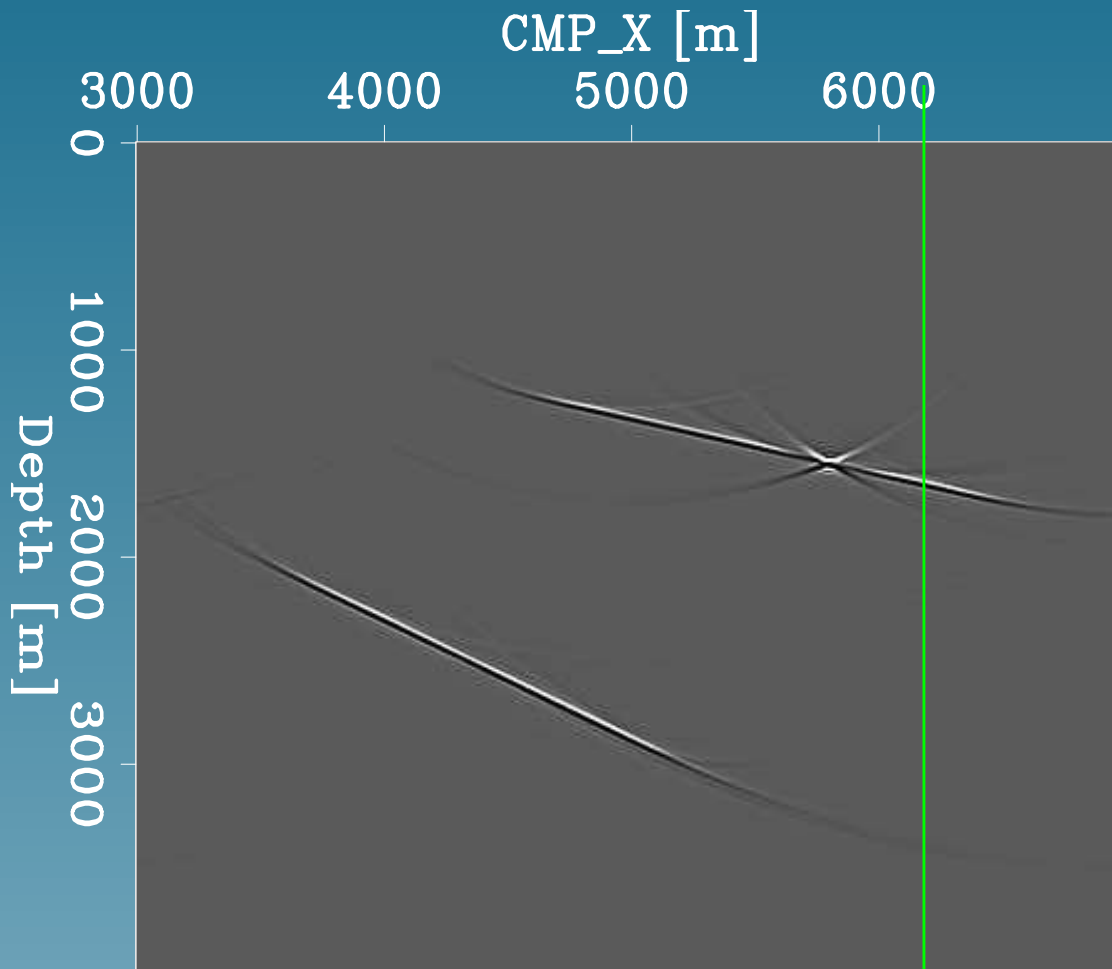


Angle stack

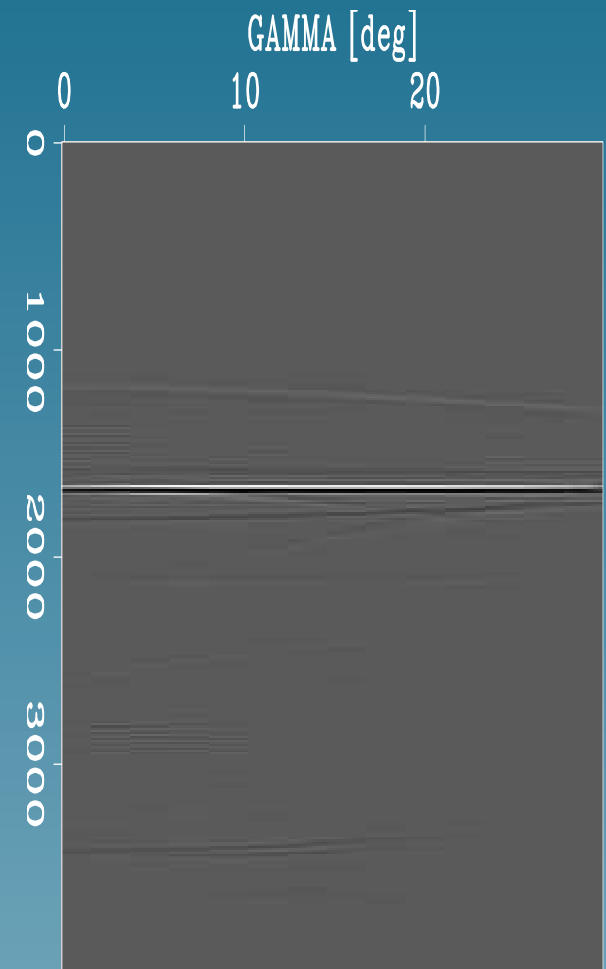


ADCIG ($x=3600$)

Primary. One Velocity

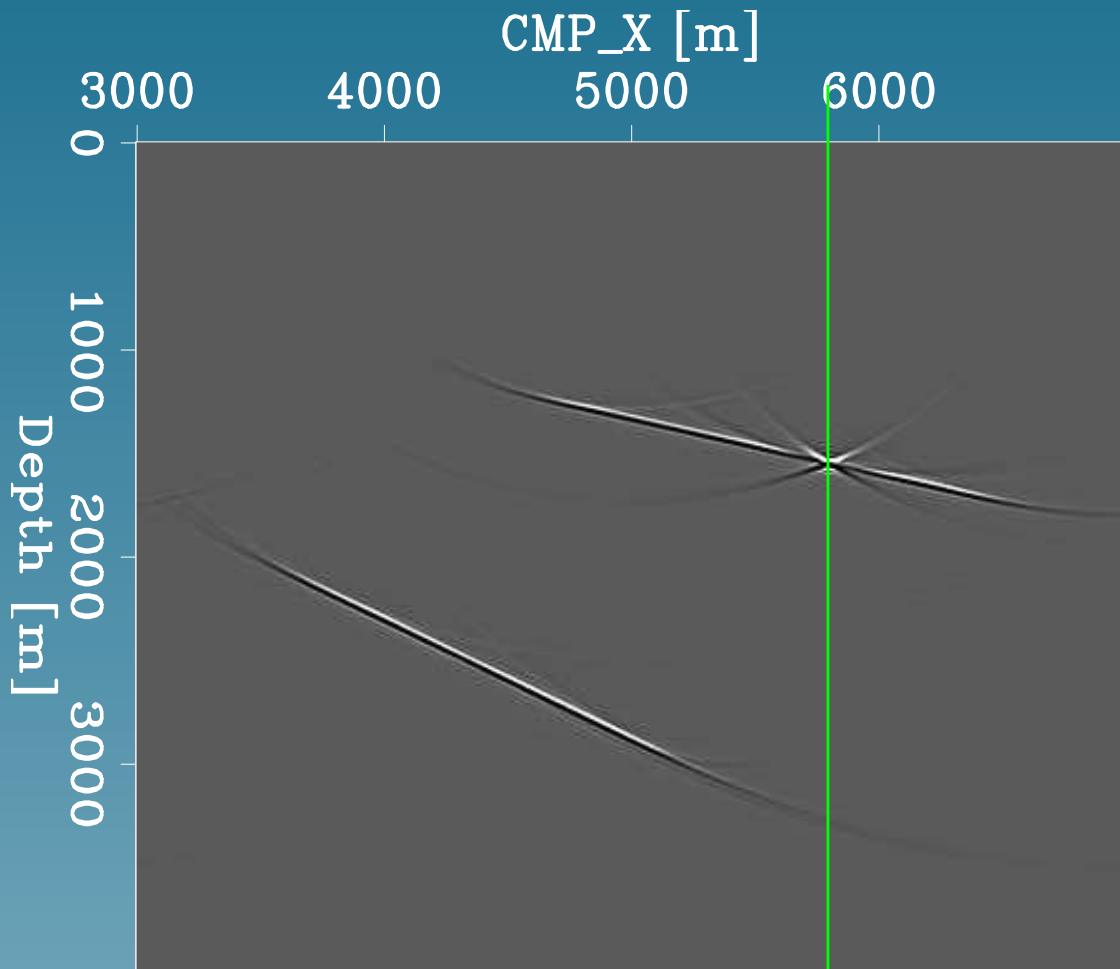


Angle stack

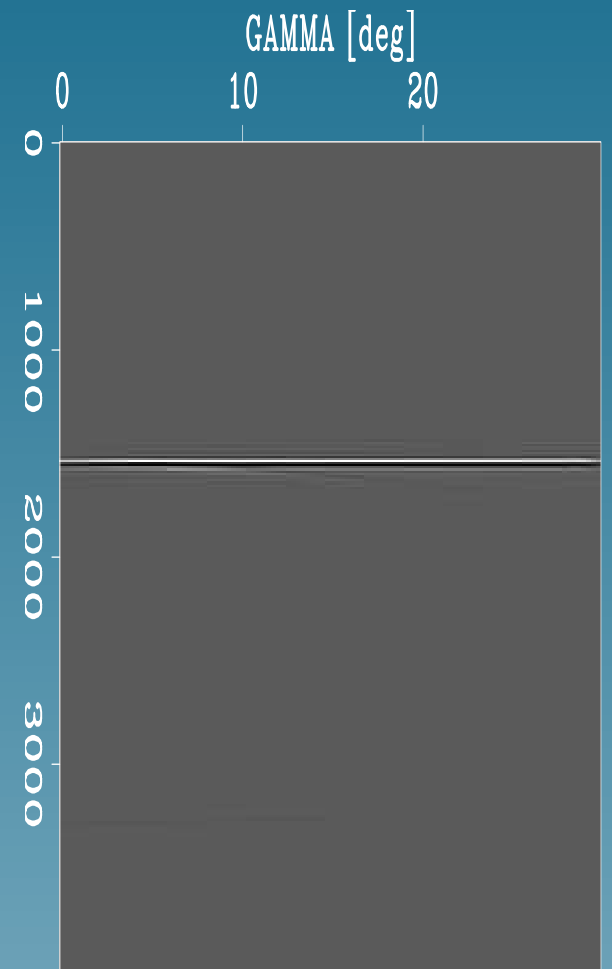


ADCIG ($x=6280$)

Diffraction. One Velocity

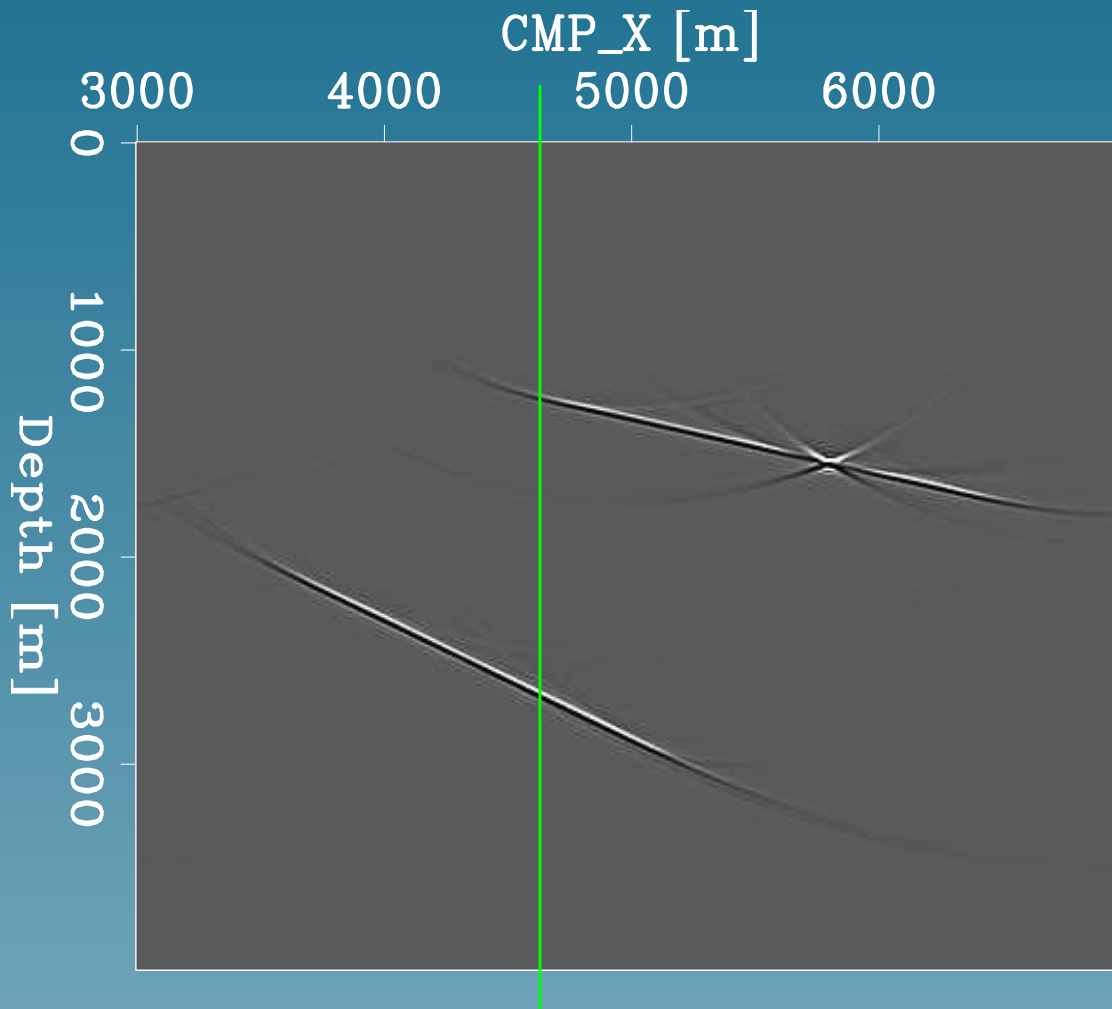


Angle stack

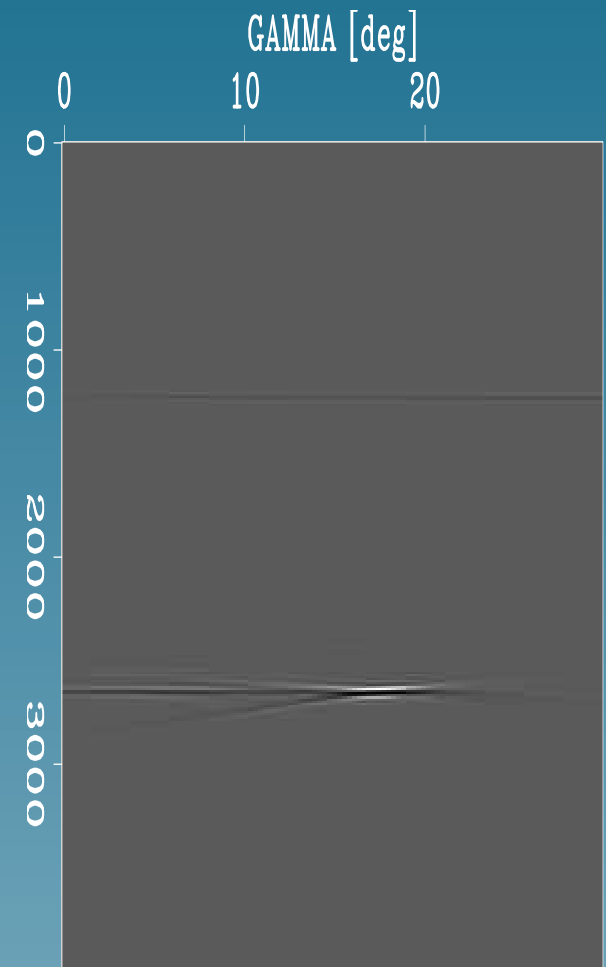


ADCIG (x=5800)

Diffracted Multiple. One Velocity

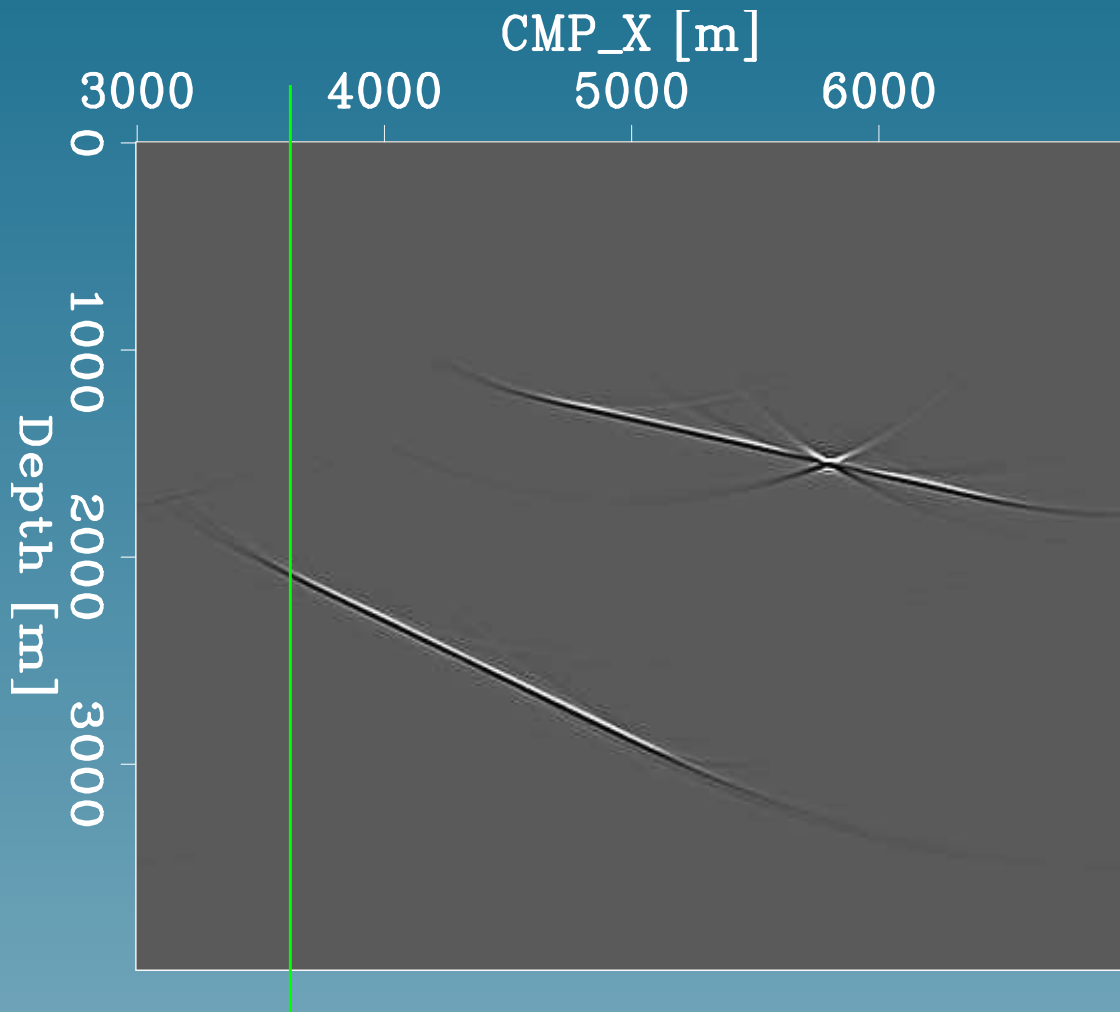


Angle stack

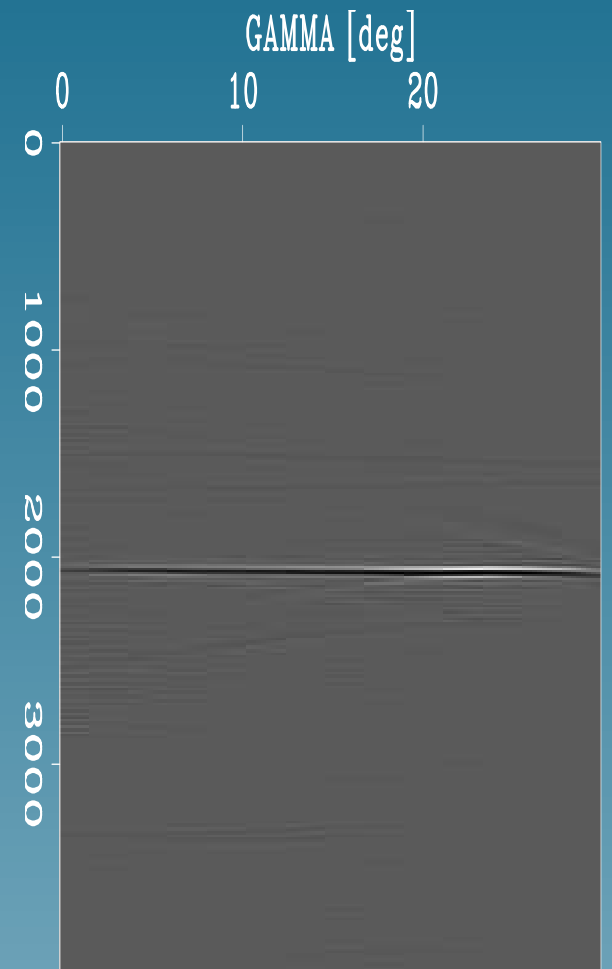


ADCIG ($x=4600$)

WB Multiple. One Velocity

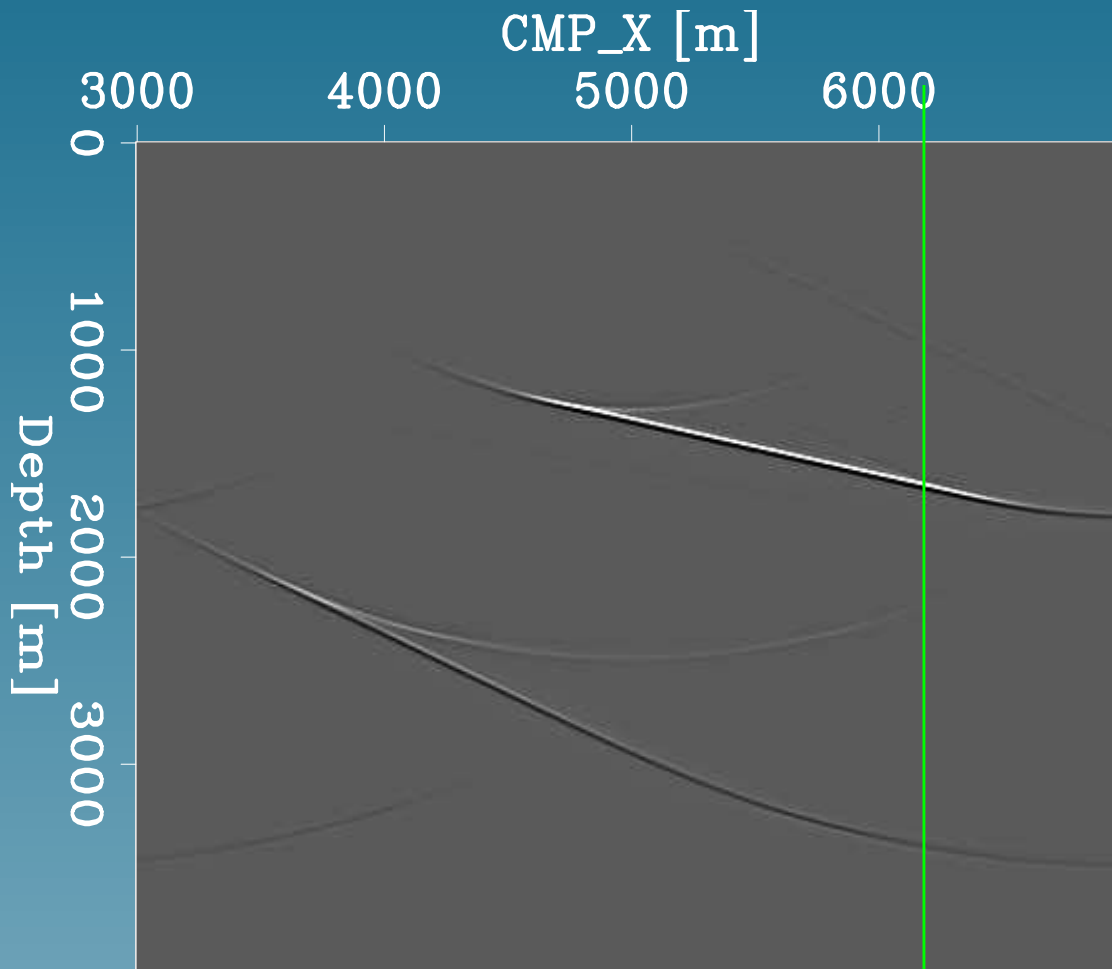


Angle stack

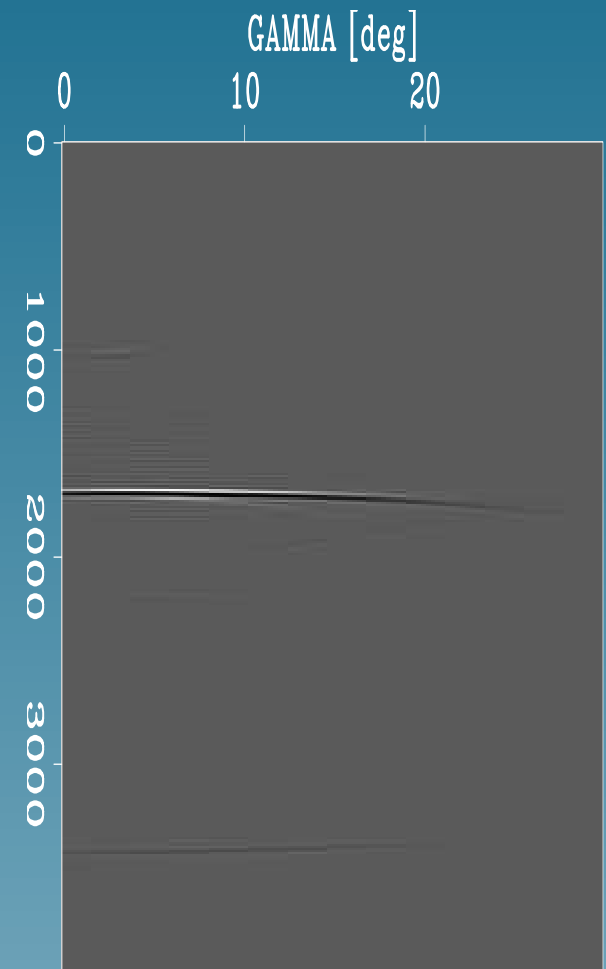


ADCIG ($x=3600$)

Primary. No Diffraction. Two Velocities

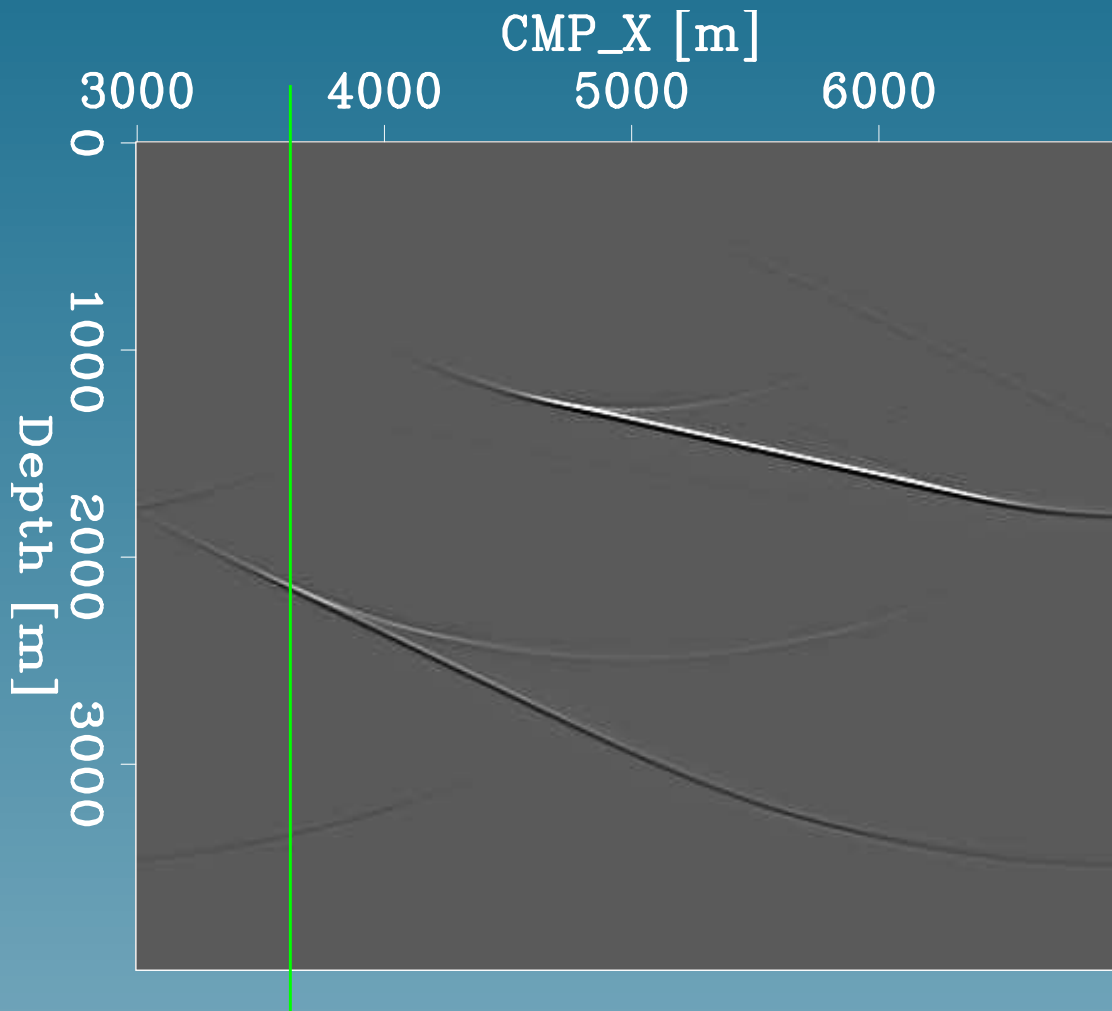


Angle stack

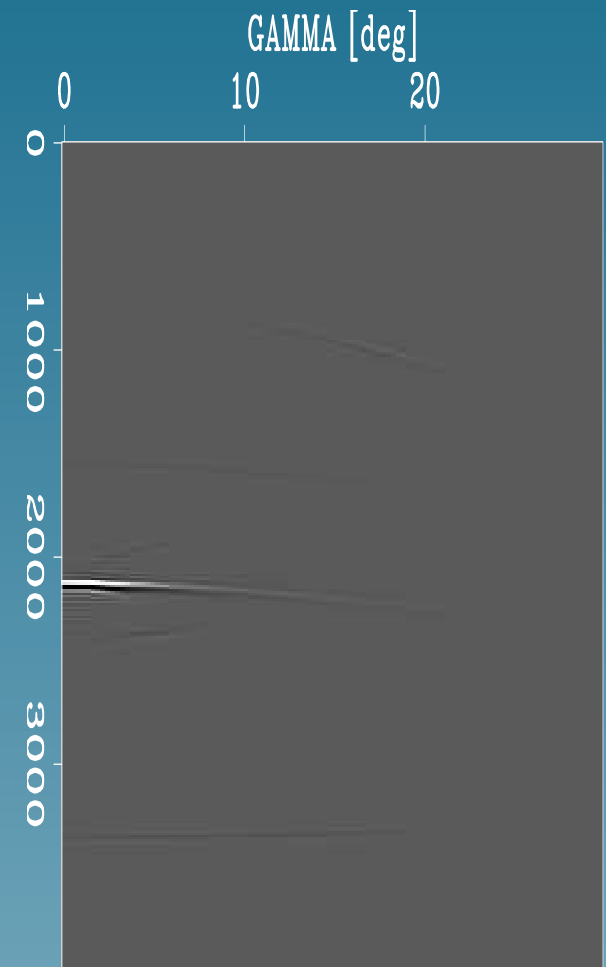


ADCIG ($x=6280$)

WB Multiple. No Diffraction. Two Vels

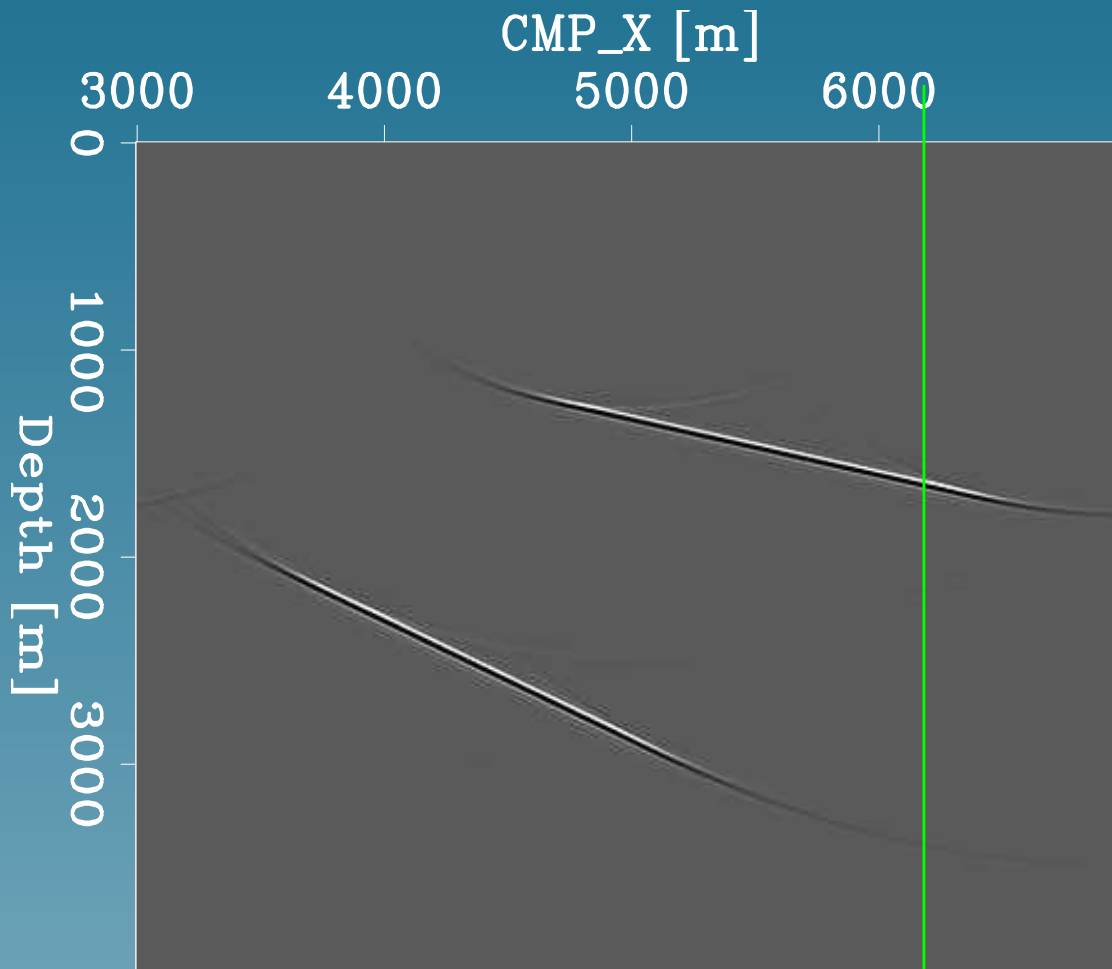


Angle stack

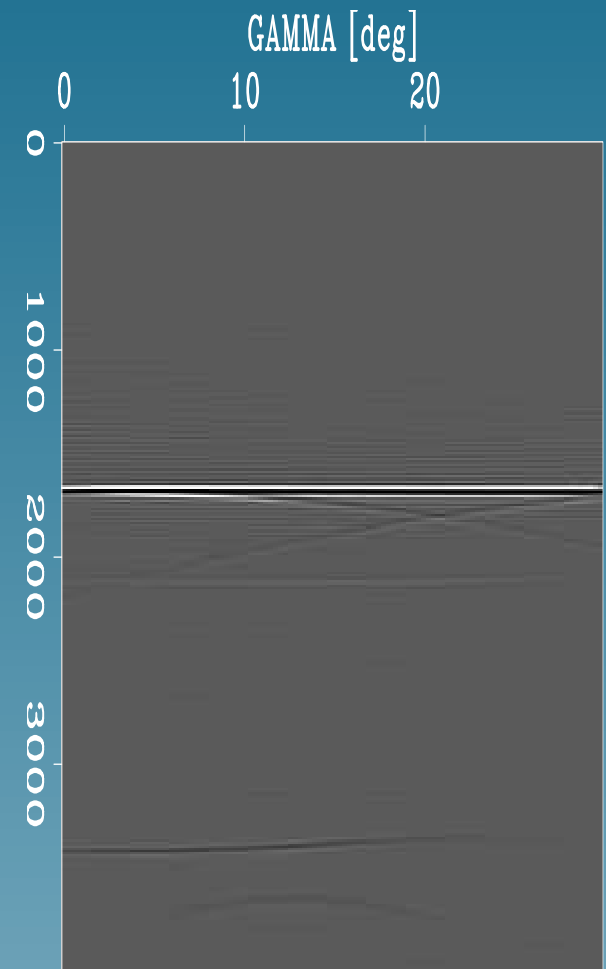


ADCIG ($x=6280$)

Primary. No Diffraction. One Velocity

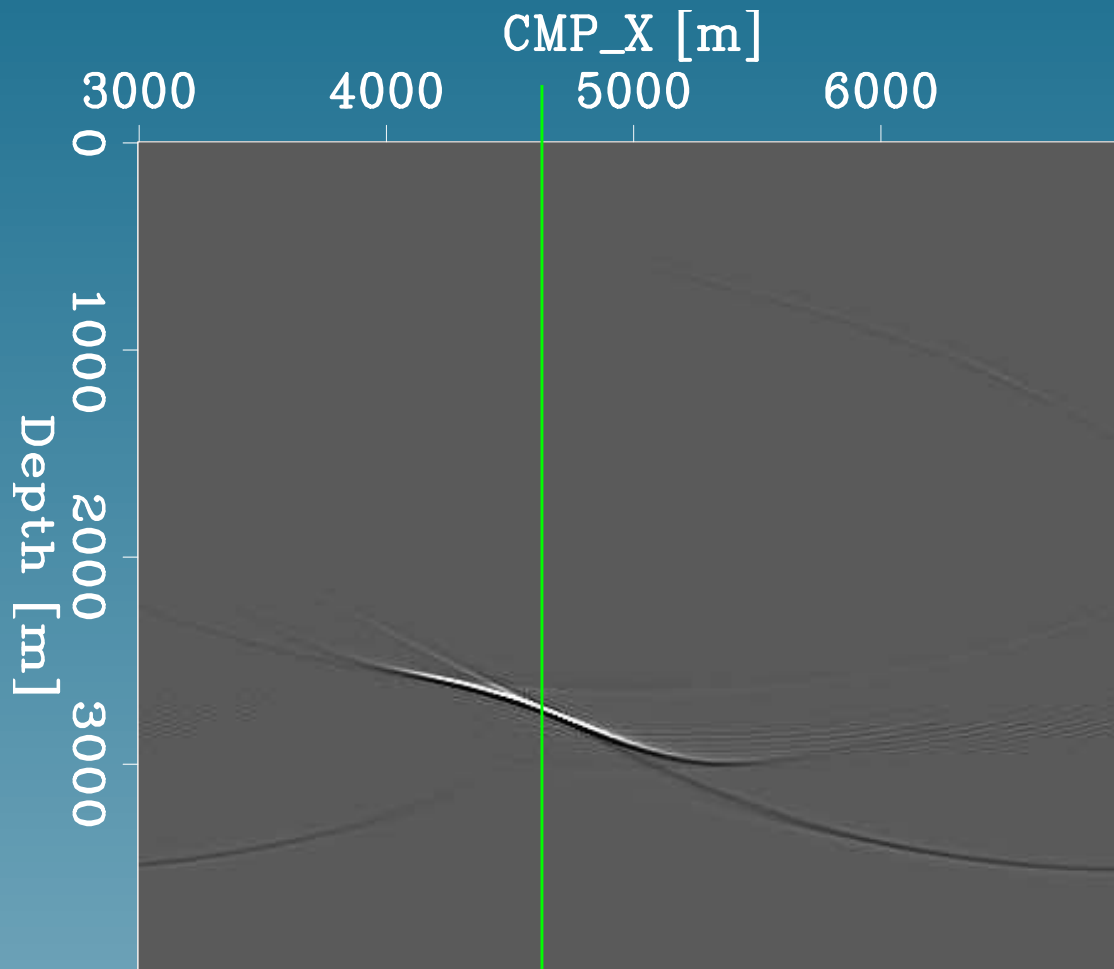


Angle stack

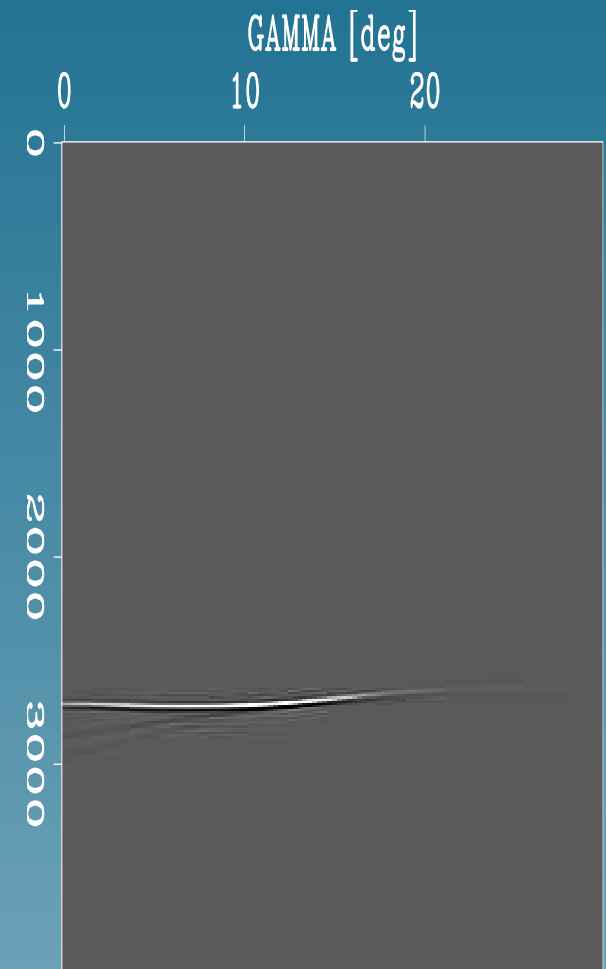


ADCIG (x=6280)

Diffracted Multiple Only. Two Velocities

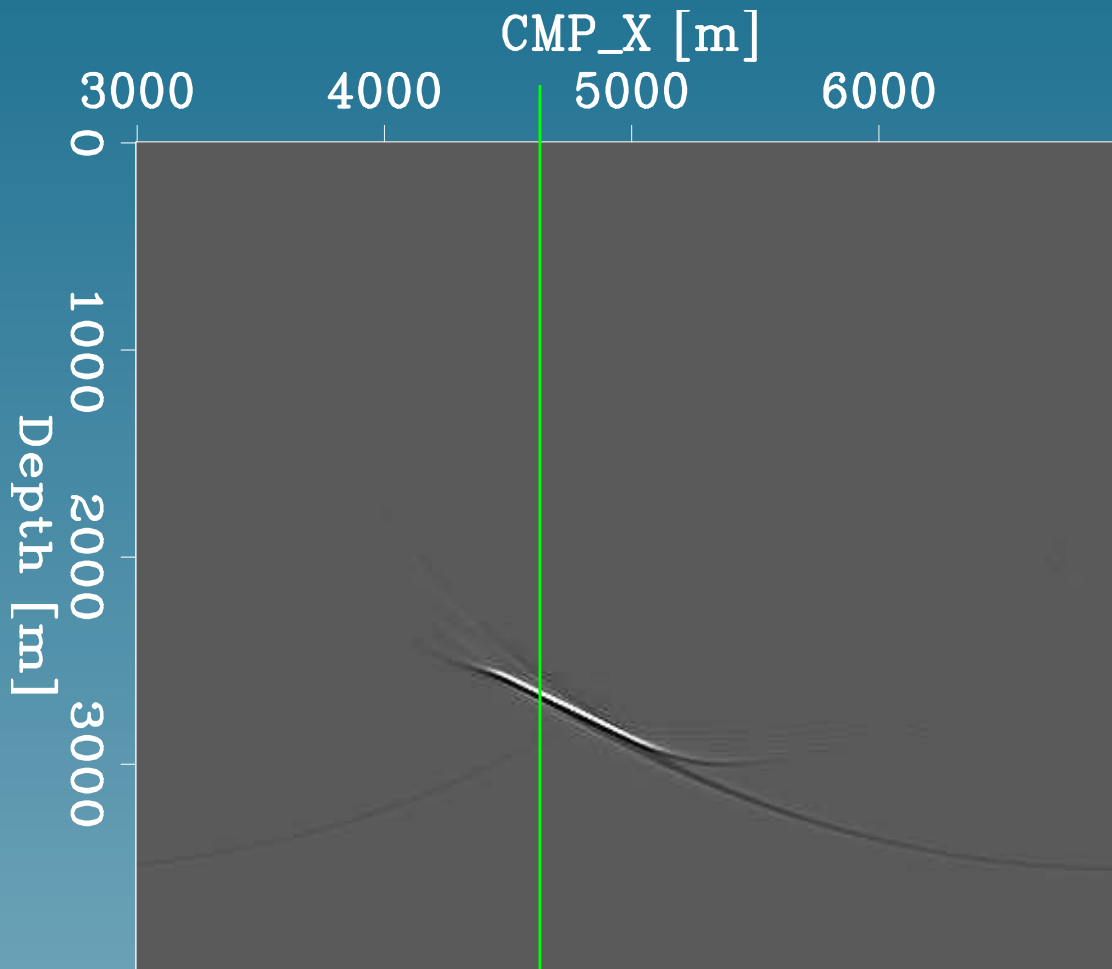


Angle stack

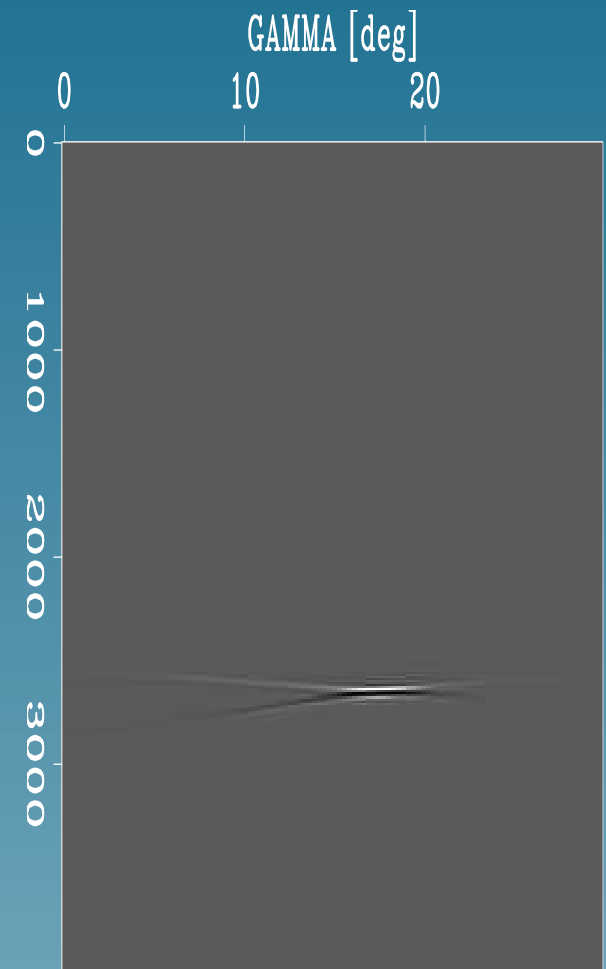


ADCIG ($x=4600$)

Diffacted Multiple Only. One Velocity



Angle stack



ADCIG ($x=4600$)

Conclusions

- Water-bottom multiples from a dipping interface behave kinematically as primaries from an interface with twice the dip at twice the depth.

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- Water-bottom multiples from a dipping interface behave kinematically as primaries from an interface with twice the dip at twice the depth.
- Diffracted multiples do not behave like primaries and are not properly migrated even if the correct velocity is used.
- Understanding the correct moveout of the multiples in the image space (diffracted multiples in particular) is critical to the design of the proper Radon transform.

Future Work

- Formalize the residual moveout issue for the multiples in the image space.

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- Design the Radon transform that best focuses the multiples in the image space.

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- Design the Radon transform that best focuses the multiples in the image space.
- Apply to synthetic and real 3D data.