

## EXAMPLES OF PARSIMONIOUS DECONVOLUTION

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### *Abstract*

Two tests were made of the parsimonious deconvolution algorithm. The single trace synthetic data test worked very well even with included noise. A second trial done on a profile of 48 hydrophones recording a marine source worked very well for some choices of parameters but other parameters led to unstable behavior outside the signal frequency band.

### *Synthetic Data Test Case*

A source waveform was defined by a sequence of numbers to resemble the explosion-implosion sequence of a marine bubble seismic source. The sequence of 23 numbers is

6,10,-1,-3,-4,-4,-3,-1,6,-1,-2,-2,-1,0,4,-1,-2,-1,0,2,0,-1,-1

A synthetic spike train is defined (on program listing bunch/pard0.f subroutine job) as

[zeros, 1.01, zeros, .5, -.5, zeros]

After convolution of the spike train with the bubble, then pseudo random noise is added. The result is defined to be the filter output  $y_t$ . The noise amplitude is one-half percent of the maximum signal value. The noise, however, is added at every time point but innovations occur only once in a while. On a root mean square basis, the signal-to-noise ratio is about thirty. Figure 1 shows the results of the parsimoneous deconvolution algorithm. Fourteen iterations were done. Before each iteration a display is made of the estimated input  $x_t$  and the estimated filter

$b_t$  which when convolved together give the known synthetic data  $y_t$ . At the first iteration, we see the input  $x$  looks like a bubble function followed by a differentiated bubble function. The presumed filter  $b_t$  is a delta function. The first eight displays are minimization of  $S_{5/2}$  and the final six displays are of the subsequent minimization of  $S_2$ . The numerical value of  $S_{5/2}$  and  $S_2$  is displayed along the left edge. Also displayed are the successive filter perturbations  $db_t$ , the unconstrained gradients  $g_t$  and constrained gradients  $dx_t$ .

We did not have a varimax program available for comparison. Furthermore, the varimax procedure as described by Wiggins and Larner is a multichannel process. And furthermore as it was described, it had no facility for imposing causality on the forward filter  $b_t$ . Nevertheless, we wanted to make some kind of comparison to evaluate the importance of the concept of using norms of low order. What was done was to take the pard0 program and reset  $n = 4$  (by the program statement  $en = 4$ ). The result is the minimization of

$$\min = S_4 = \frac{\|x\|_4 - \epsilon}{\|x\|_4}$$

which is displayed in figure 2. The result is judged to be subjectively inferior to the results of minimizing  $S_2$  in figure 1.

Finally, I have included figure 3 which has been taken from the Western Geophysical Company's pamphlet *Minimum Entropy Deconvolution (MED)*. It shows a varimax result. I must most emphatically assert that I am not sure it is valid to compare this result to figures 1 and 2. The wavelet is different, the constraints are different, and the number of channels is different. Supposing that all calculations were done with single precision ( $10^{-6}$ ) accuracy, it seems reasonable to expect  $(10^{-6})^{1/4} = 3\%$  noise from the computation alone in figure 3. This is roughly what we see in figure 3. In figure 2 the noise by the same crude theoretical argument should be  $(.005)^{1/4} = 26\%$ , which is roughly what the figure shows. Another peculiarity of figure 2 is that the doublet on the

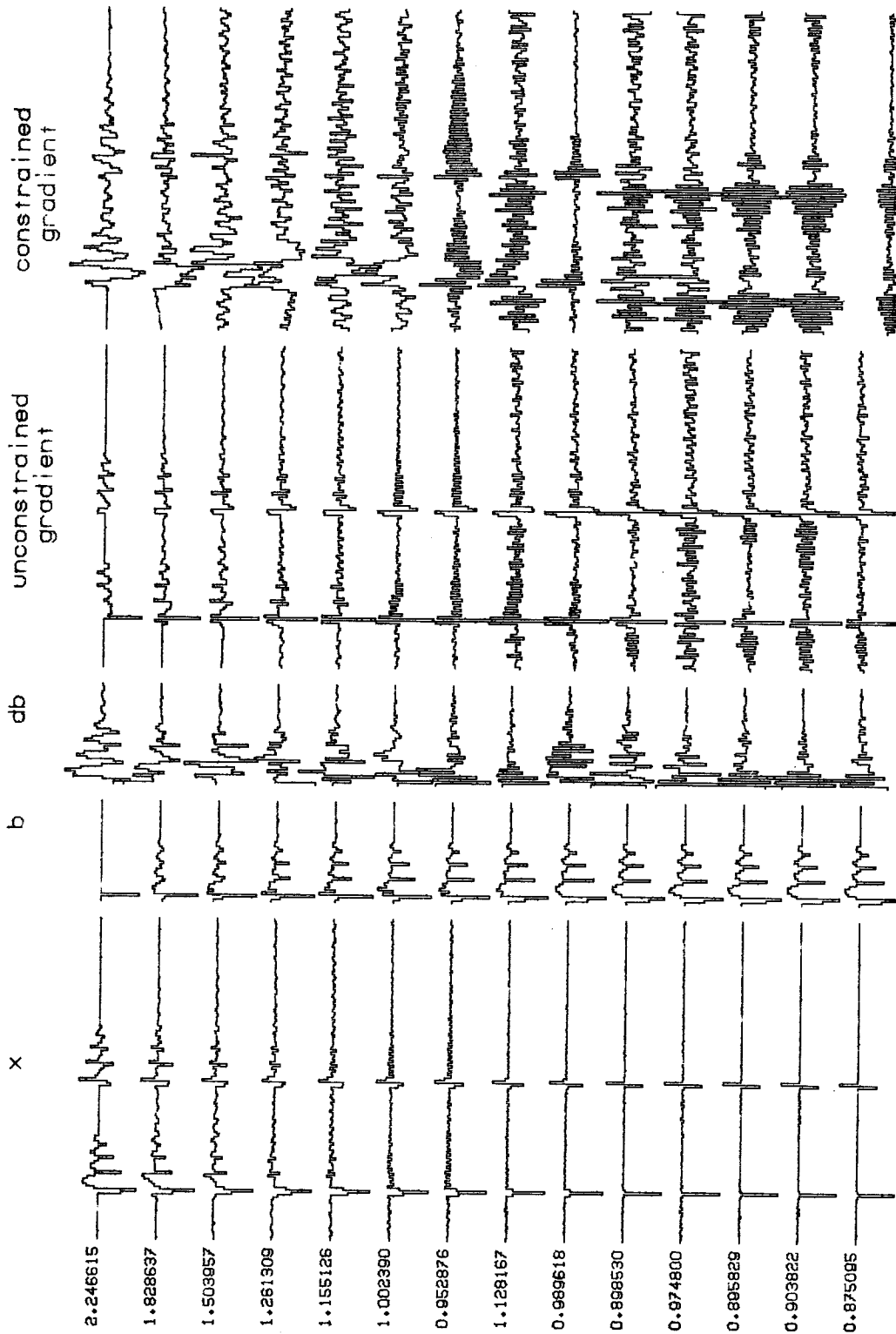


Figure 1.—Test of the parsimonious deconvolution program bunch/pard0.f. After 14 iterations, a subjectively favorable decomposition of the output  $y$  into the input  $x$  and filter  $b$  has been achieved.

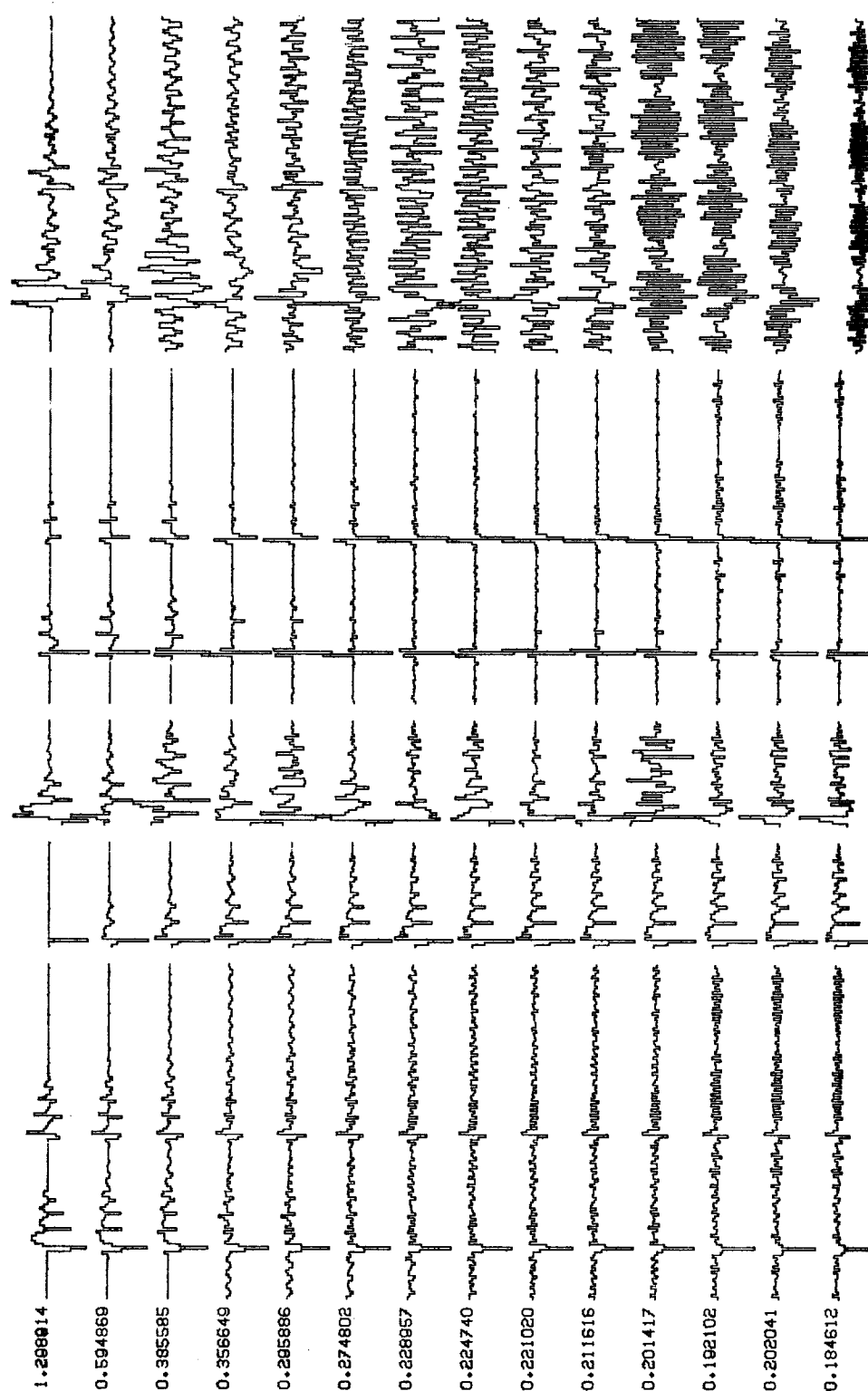


Figure 2.—In figure 1, the norm ratio  $N_2^{2-\epsilon}$  was minimized. In this figure, the norm ratio  $N_4^{4-\epsilon}$ , which has some similarity to varimax, is minimized.

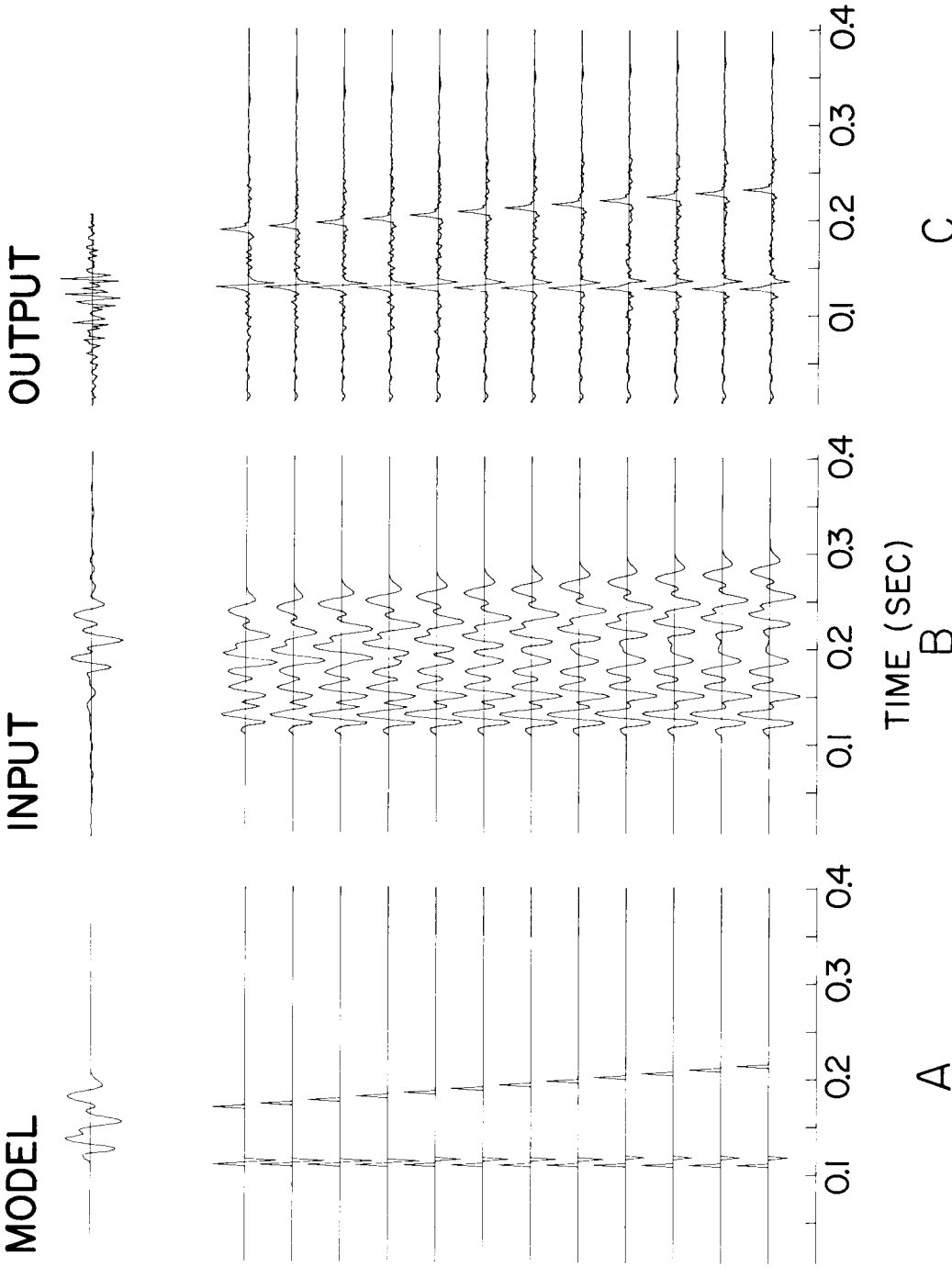


Figure 1. Synthetic data example  
 a. A hypothetical CDP gather of twelve spike-series traces. The three spike "events" on each trace experience differential moveout from "near trace" to "far trace." The input wavelet is shown above.  
 b. Each trace is the convolution of the corresponding spike trace with the non-minimum-phase input wavelet. The effective wavelet resulting from MED processing is shown above.  
 c. Traces resulting from MED processing. The optimum MED operator is shown above.

Figure 3.—Example of the Western Geophysical MED process.

deconvolved data looks smaller than it should be, even though the forward filter is constrained to be shorter than the interval between the pulse and the doublet.

Finally, I have included the computer program used to generate figure 1 and figure 2.

#### *Field Data Test Case*

Forty eight seismic traces from the same source (a common shot profile) were selected from a marine seismic section. The complete section is displayed in SEP 12 page 77. The shotpoint was very near to the left edge of that section. The common shot point profile is displayed in figure 4. After deconvolution, it was found that the frequency content of the data was significantly higher. This led to a data viewing problem because the stepout from trace to trace caused spatial aliasing. A more satisfactory presentation of the data is to perform time shifts which reduce the stepout. Hence, the traces were time shifted so that a theoretical first water bottom multiple would have no stepout. The raw field data with these time shifts and spherical divergence correction is displayed in figure 5. A prominent event labeled "bubble" is seen to be parallel to the sea floor arrival. Figure 6 shows the data after deconvolution by the waveform determined from the parsimonious deconvolution algorithm. The bubble event has virtually disappeared. The frequency content has changed too. In order to effect a more appropriate comparison, Larry Morley performed a conventional Wiener-Levinson deconvolution. It is displayed in figure 7. It happens to have about the same spectrum as figure 6. It is clear from these figures that the parsimonious deconvolution has done a much better job of bubble suppression than the conventional deconvolution. The most obvious case is the bubble event at small offsets. Bubble suppression is also notable on the refracted wave at wide offsets and to a lesser extent on the sea floor multiple reflection about  $2/3$  of the way out the cable. A single bubble function  $b_t$  was determined for the entire gather. It is displayed on figure 8 at the same time scale as the profile. The many replicas of this waveform in figure 8 are shown to exhibit the waveform at

both polarities and various gains. Because figures 4 through 7 have gain increasing with time according to spherical divergence, the bubble will appear more strongly on those figures than on 8.

Figure 9 shows a superposition of two different bubble waveform estimates. One was based on traces 2,3,4,5, and 6, that is to say, the far end of the streamer cable. The other is based on traces 2,6,10,14, 18,22,26,30,34,38,42, and 46, that is to say, a uniform distribution of 12 of the 48 traces. Not only are the estimated waveforms very similar but it is also possible to see clearly where  $t = 0$  should be. The noise level can be estimated from the failure of the waveforms to vanish completely before  $t = 0$ .

### *Bugs, Instabilities*

Unfortunately, the program sometimes exhibits resonant instabilities. A typical example of this is shown in figure 10. It might be a program bug. More likely, the algorithm needs some kind of explicit stabilization procedure. The Levinson algorithm, for example, often needs a bit of white noise. Here we have not yet devised the appropriate stabilizing procedure. Nevertheless, the results are *sufficiently good* that the computer program has been included. The next thing I'm going to try is to restrict the *relative* variation of the Fourier transform of the filter from one iteration to the next.

\* \* \* \* \*

*Einstein's Second Theory of Relativity:*

*Your chances of getting along with your relatives increases directly in proportion to the distance you keep away from them.*

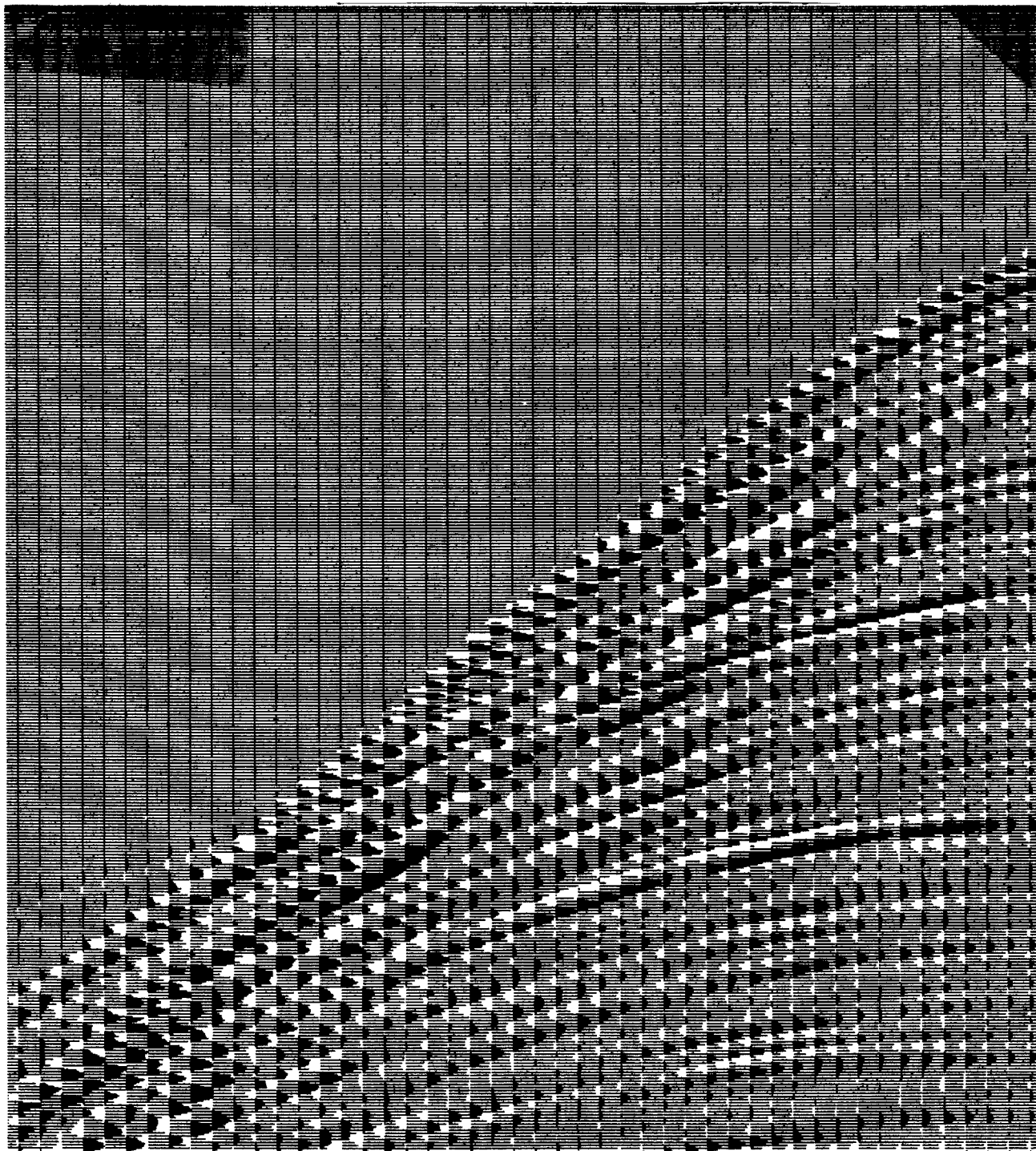


FIGURE 4.—The common shot gather which was used for the first field data test of parsimonious deconvolution. Displayed is the field tape with spherical divergence correction.



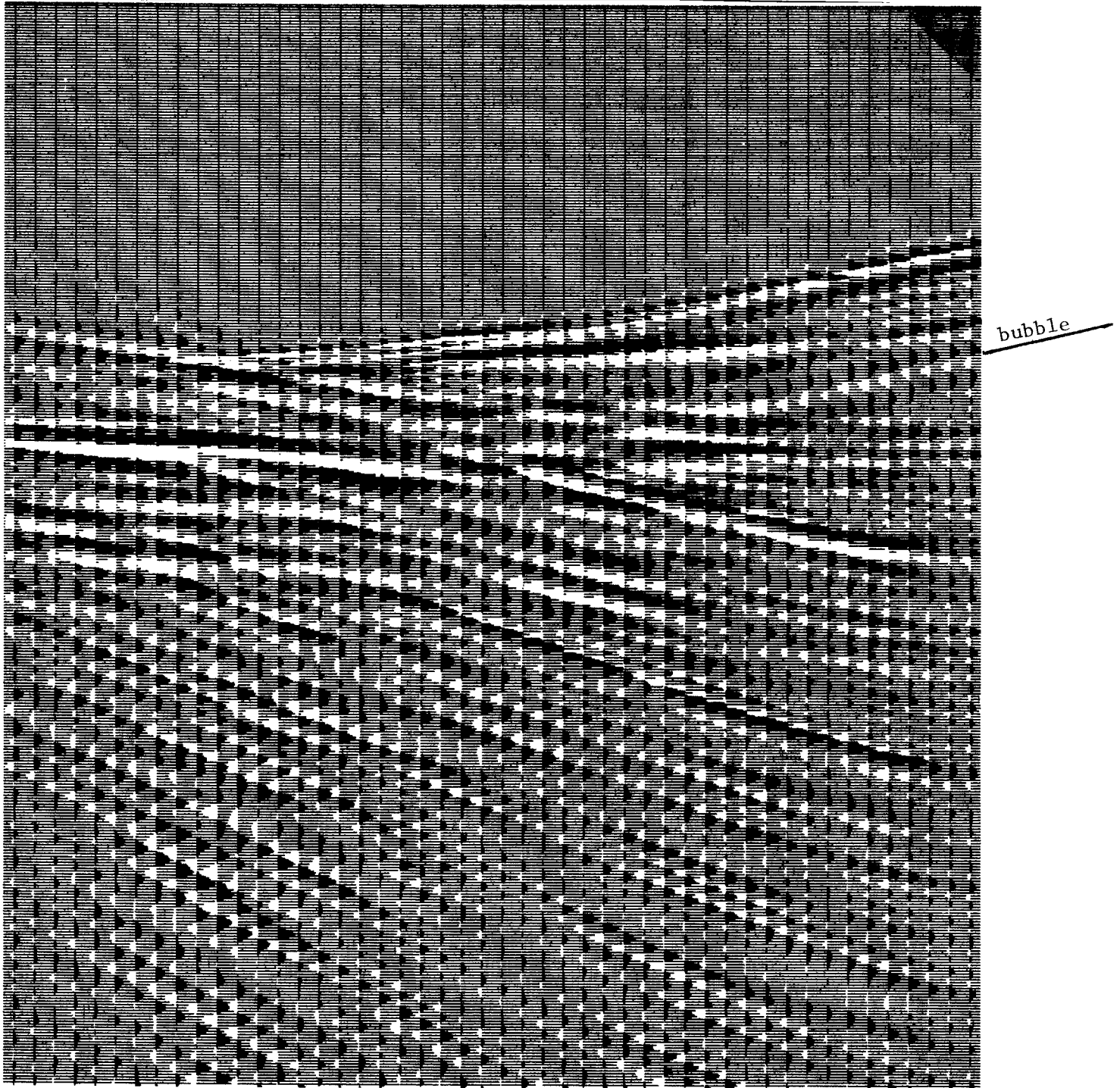


FIGURE 5.—The data of figure 4 were time shifted so as to flatten the first multiple reflection.

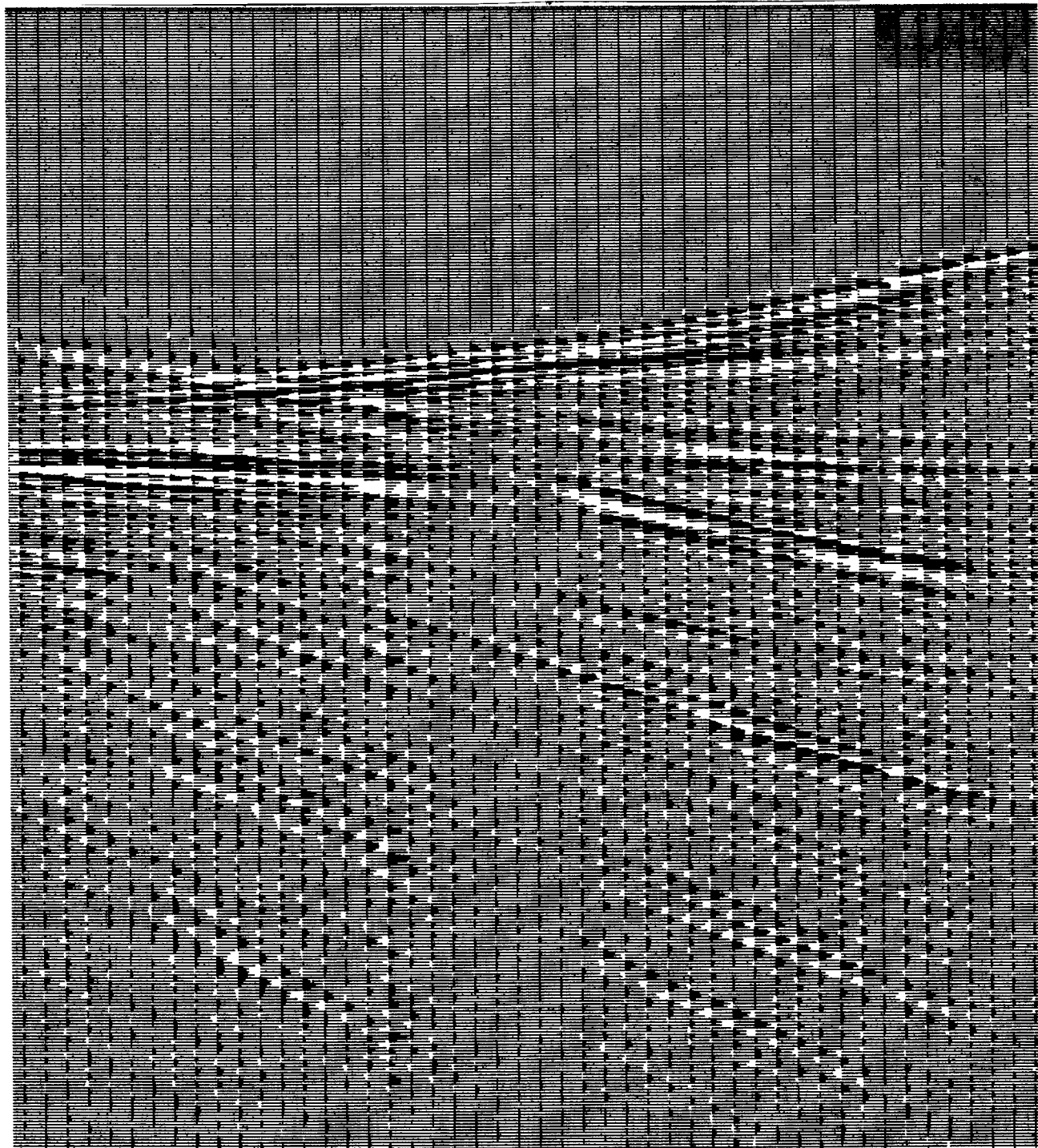


FIGURE 6.—The data of figure 5 after parsimonious deconvolution, spherical spreading, and trace equalization. Compare to figure 5 and 6 to note absence of bubble events.

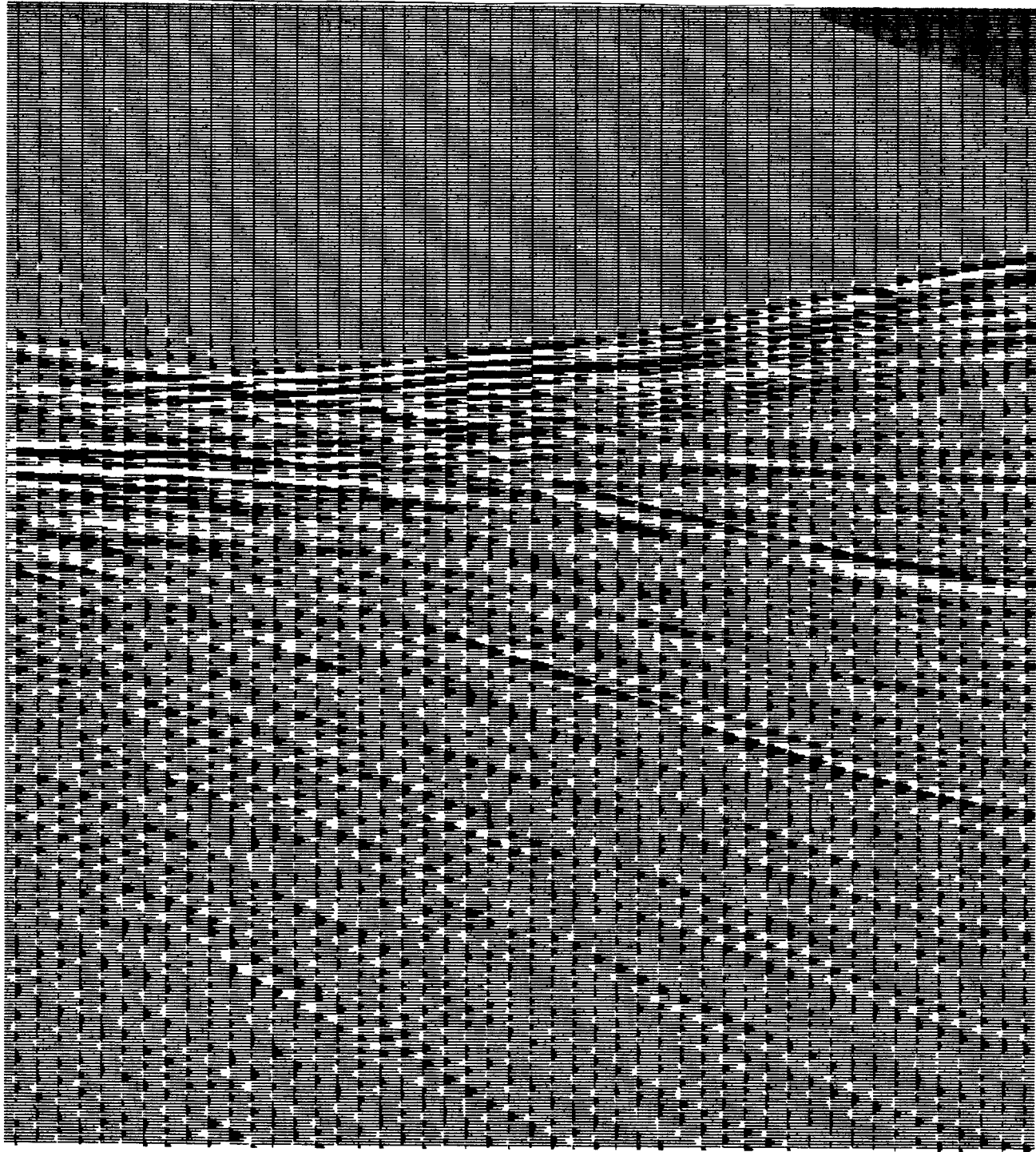


FIGURE 7.—The data of figure 5 after conventional deconvolution.

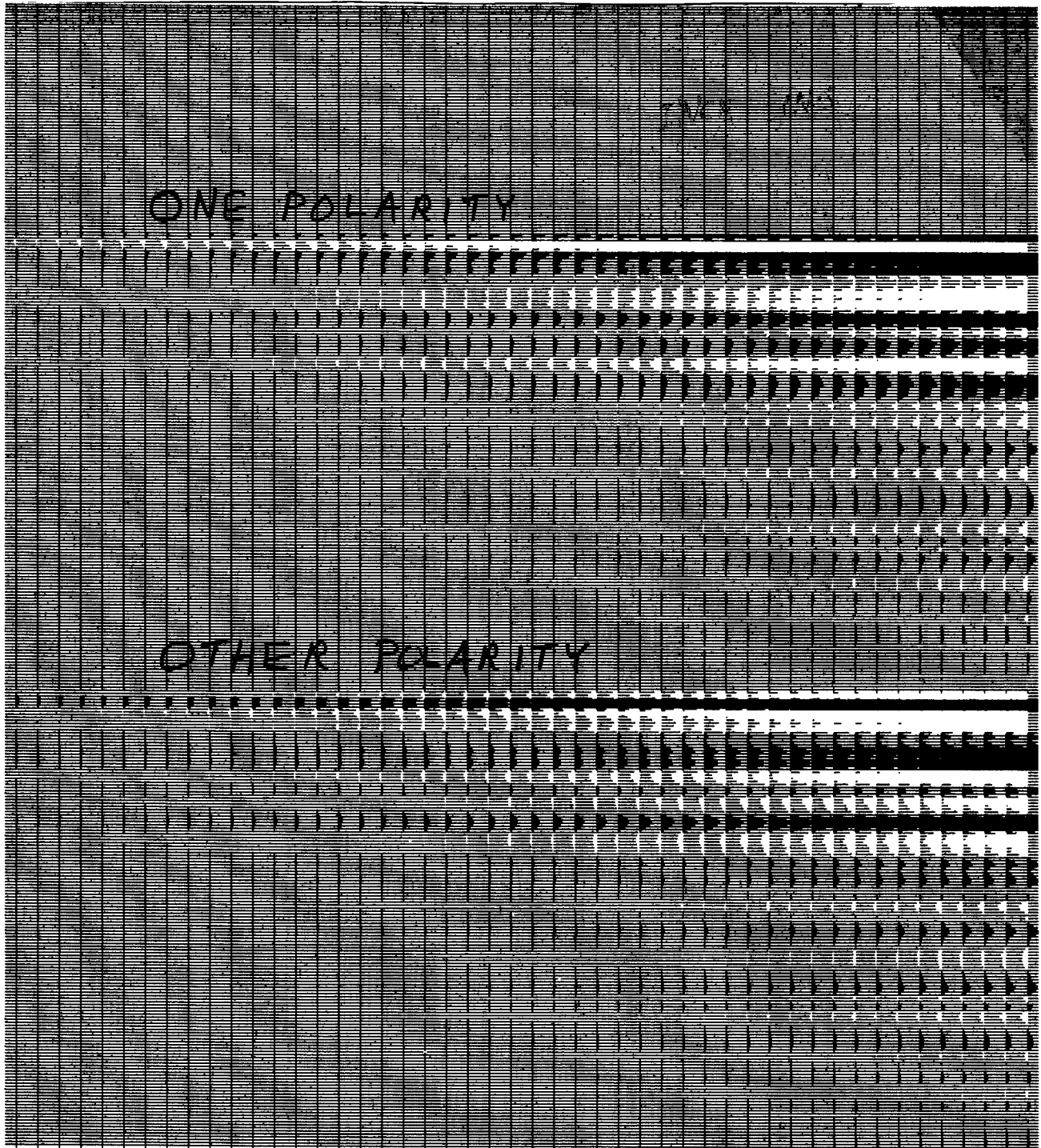


FIGURE 8.—Display of the bubble function which was determined by parsimonious deconvolution. Gain increases to the right. Both polarities displayed. Bubble tails will be larger on figures 4-7 than here because of spherical divergence.

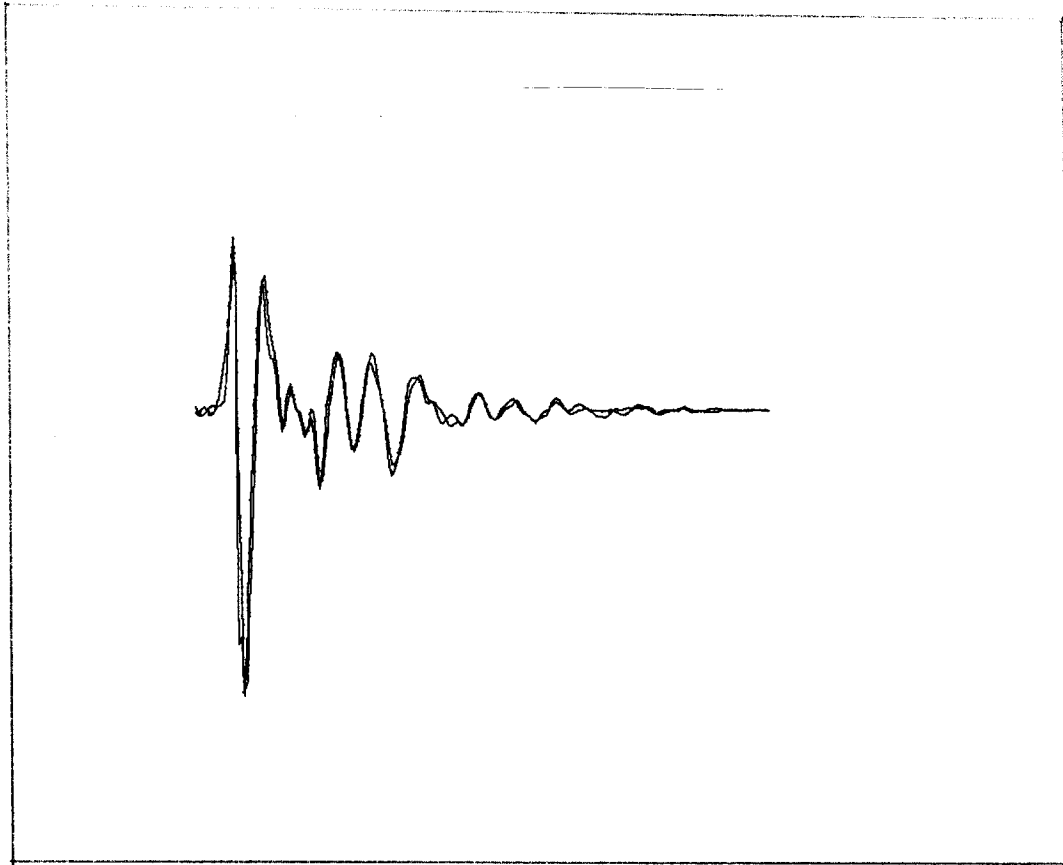


FIGURE 9.—A superposition of two different bubble waveform estimates. One was based on traces 2,3,4,5,6, that is to say, the far end of the streamer cable. The other is based on traces 2,6,10,14,18,22,26,30,34,38,42, and 46, that is to say, a uniform distribution of 12 of the 48 traces. Not only are the waveforms very similar, but it is also possible to see clearly where  $t = 0$  should be. The noise level can be estimated from the failure of the waveforms to vanish completely before  $t = 0$ .

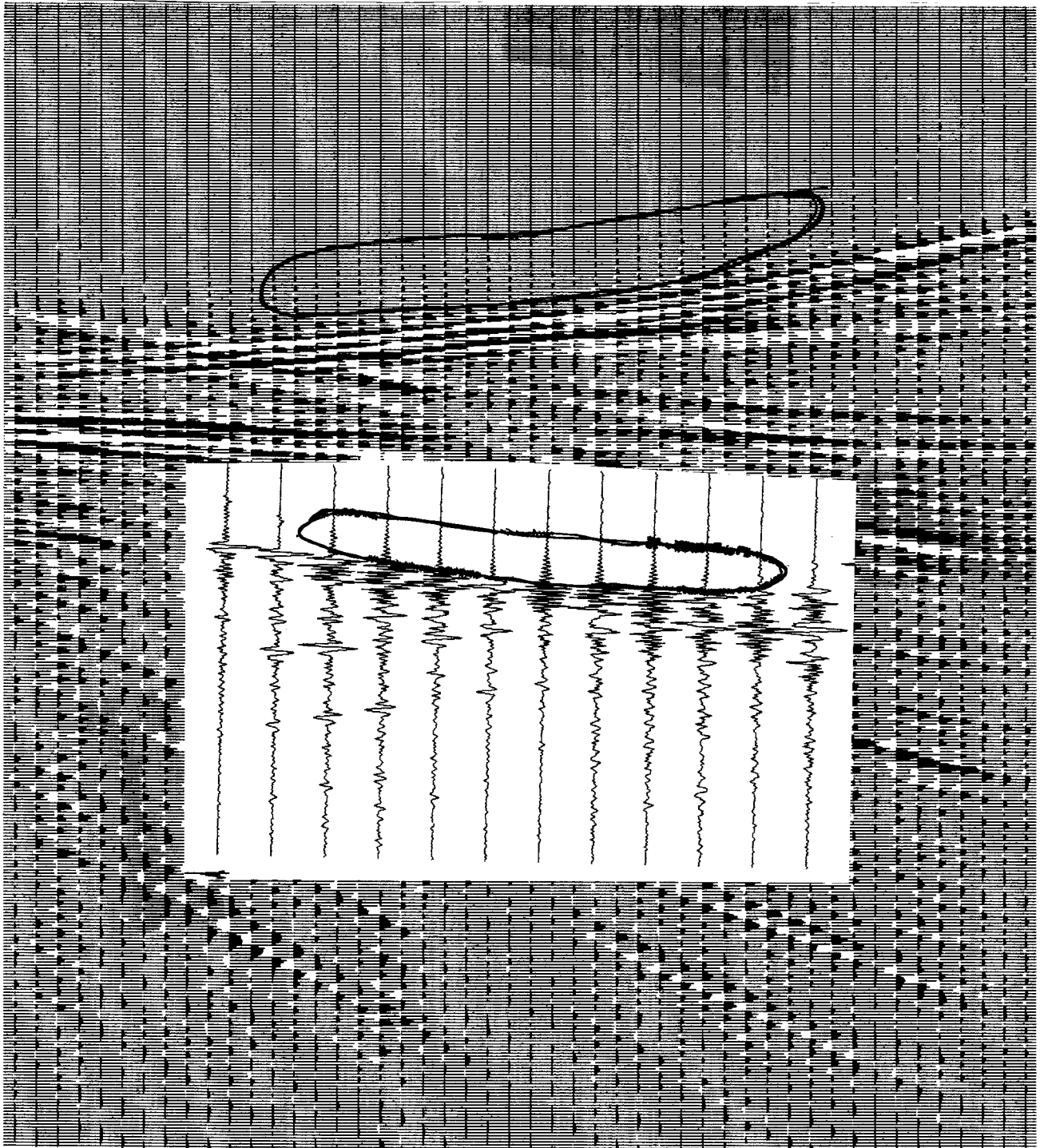


FIGURE 10.—A resonant instability which was not understood at the time of this report's printing deadline.

```

real x(130),y(130),g(130),b(130),db(130),dx(130)
complex cx(65),cy(65),cg(65),cb(65),cdb(65),cdx(65)
equivalence(y,cy),(db,cdb),(dx,cdx)
complex conjg
call setmod(11,128) OUTPUT ON UNIT 11
nt=128 trace length
nth=nt/2
nthp=nth+1
nb=40 filter length
amb=1./200. half percent noise
call job(nt,x,y,23,b,amb,rmsn) set up test case
call fftr(nth,y,+1.) fourier transform input data
call move(nt,b,cb)
call fftr(nth,cb,+1.) fourier transform initial filter
niter=14
do 400 iter=1,niter basic iterative loop
alpha=.20*(niter-iter+.5)/niter alpha decreases linearly
en=2.5-.5*((iter-1)/((niter+1)/2)) n starts at 2.5 then becomes 2.0
elog=grad(en,nt,x,g) gradient computation
call scale(-1.,nt,g) scale grad negative (for display)
write(11,25)iter,alpha,elog
25 format(i4,f5.2,f12.8)
call move(nt,g,cg)
call fftr(nth,cg,+1.) G ← g
call move(nt,x,cx)
call fftr(nth,cx,+1.) X ← x
do 50 i=1,nthp
50 cdb(i)=-cg(i)*cb(i)*conjg(cx(i)) dB = X̄GB
call fftri(nth,cdb,-1.) ab ← dB
do 75 i=nb,nt restrict deviation of filter
75 db(i)=0.
do 100 i=1,nb
100 db(i)=db(i)*(nb-i) taper filter perturbation db
sc=dot(nb,b,db)/dot(nb,b,b)
do 125 i=1,nb
125 db(i)=db(i)-sc*b(i) remove projection of b from db
nskip=1
if(mod(iter-1,nskip).ne.0)go to 150
idy=3
ink=1+(iter-1)/nskip
call plot(ink,idy,100,nt,x)
call plot(ink,idy,120+idy*nt,nb,b)
call plot(ink,idy,140+idy*(nt+nb),nb,db)
call plot(ink,idy,160+idy*(nt+nb+nb),nt,g)
150 continue
ix=(iter-1)*70/nskip+70
iy=0
call number(elog,'(f10.6)',ix,iy,2,1,9) annotate plot
sc=bigest(nt,b)/bigest(nt,db)
do 175 i=1,nb
175 b(i)=b(i)+db(i)*alpha*sc b ← b + alpha b
call move(nt,b,cb)
call fftr(nth,cb,+1.) B ← b
sc=dot(nt+2,cb,cb)/nth
do 350 i=1,nthp
den=(amb*amb+alpha*alpha)*sc+conjg(cb(i))*cb(i) don't divide by zero

```

```

350 cdx(i)=conjg(cb(i))*(cy(i)-cx(i)*cb(i))/den
    call fftri(nth,cdx,-1.)
    call plot(ink,idy,180+idy*(2*nt+2*nb),nt,dx)
    do 375 i=1,nt

```

*dx ← DX*

```

375 x(i)=x(i)+dx(i)
400 continue

```

*x ← x + dx*

```

    stop
    end
    function grad(en,n,x,g)
    dimension x(n),g(n),v(128)
    su=0.
    sulax=0.
    do 10 i=1,n

```

*computes equation 18*

```

    xi=x(i)
    ax=abs(xi)+1.e-20
    alx=alog(ax)
    u=exp(en*alx)
    su=su+u
    sulax=sulax+alx*u
    deriv=(u*xi/ax)/ax
    g(i)=deriv
10  v(i)=alx*deriv
    scv=-en*en/su
    scg=en*en*sulax/(su*su)
    do 20 i=1,n
20  g(i)=g(i)*scg+v(i)*scv
    grad=alog(su)-en*sulax/su
    return
    end

```

```

    subroutine job(nt,x,y,nb,b,amb,rmsn)
    dimension x(nt),b(nt),y(nt),temp(200)
    read(17,17)(b(i),i=1,nb)
17  format(f5.1)

```

*setup test case*

*read synthetic bubble*

```

10  do 10 i=1,nt
    x(i)=0.
    x(nt/6)=1.01
    x(nt/2)=.5
    x(nt/2+1)=-.5

```

*set up spike series  
zeros, 1, zeros, .5, -.5, zeros*

```

    rock=grad(2.0,nt,x,y)
    write(11,77) rock
77  format('preconceived best answer =',f20.8)
    call conv(nt,x,nb,b,temp)
    call move(nt,temp,y)
    call scale(1./bigest(nt,y),nt,y)
    rmsn=sqrt(dot(nt,y,y)/nt)/amb
    do 38 i=1,nt
38  y(i)=y(i)+2.*(ran(i1,i2)-.5)*amb
    write(11,78)amb,rmsn

```

*add noise*

```

78  format('ambient=',f9.6,' rms s/n=',f7.1)
    do 40 i=1,nt
40  b(i)=0.
    b(3)=1.

```

*first filter guess*

```

    do 50 i=1,nt
50  x(i)=0.
    do 60 i=3,nt
60  x(i-2)=y(i)

```



```
return
end
subroutine plot(iter, idy, ishift, n, p)
dimension p(n)
logical*1 m, d, e
data m, d, e/'m', 'd', 'e'/
call setmod(9, 512)
b=0.
do 10 i=1, n
10  if(abs(p(i)).gt. b)b=abs(p(i))
do 20 i=1, n
iy=ishift+idy*i
ix=iter*70+p(i)*45./b+.5
if(i.eq.1)write(9)Ⓜ ix, iy
write(9)Ⓣ, ix, iy
iy=iy+idy
write(9)d, ix, iy
20  continue
return
end
```

*move pen to (ix, iy)*

*draw line to (ix, iy)*

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```

      subroutine conv(nf, f, nx, x, y)
      dimension f(nf), x(nx), y(1)
      l=nf+nx-1
      do 10 i=1, l
10      y(i)=0.
          do 20 i=1, nf
              do 20 j=1, nx
                  k=i+j-1
20      y(k)=y(k)+f(i)*x(j)
          return
      end
      real function biggest(n, x)
      dimension x(n)
      b=0.
      do 10 i=1, n
10      if(abs(x(i)).gt.b) b=abs(x(i))
          biggest=b
      return
      end
      function dot(n, x, y)
      dimension x(n), y(n)
      xy=0.
      do 10 i=1, n
10      xy=xy+x(i)*y(i)
          dot=xy
      return
      end
      subroutine cross(n, x, d, nf, g)
      dimension x(n), d(n), g(nf)
      do 10 j=1, nf
10      g(j)=g(j)+dot(n-j+1, x, d(j))
          return
      end
      subroutine zero(n, x)
      dimension x(n)
      do 10 i=1, n
10      x(i)=0.
          return
      end
      subroutine move(n, x, y)
      dimension x(n), y(n)
      do 10 i=1, n
10      y(i)=x(i)
          return
      end
      subroutine scale(sc, n, x)
      dimension x(n)
      do 10 i=1, n
10      x(i)=x(i)*sc
          return
      end
      subroutine fft(lx, cx, signi, scale)
c      Complex Fourier transform. (JFC 9/76)
c
c          lx          signi*2*pi*i*(j-1)*(k-1)/lx
c      cx(k) = scale * sum cx(j) * e

```

```

c          j=1          for k=1,2,...,lx=2**integer
c
      complex cx(lx), cmplx, cw, cdel, ctemp
      do 05 i=1, lx
05      cx(i)=cx(i)*scale
          j=1
          do 30 i=1, lx
              if(i.gt.j) go to 10
              ctemp=cx(j)
              cx(j)=cx(i)
              cx(i)=ctemp
10          m=lx/2
20          if(j.le.m) go to 30
              j=j-m
              m=m/2
              if(m.ge.1) go to 20
30          j=j+m
              l=1
40          istep=2*l
              cw=1.
              arg=signi*3.14159265/l
              cdel=cplx(cos(arg), sin(arg))
              do 60 m=1, l
                  do 50 i=m, lx, istep
                      ctemp=cw*cx(i+l)
                      cx(i+l)=cx(i)-ctemp
50                      cx(i)=cx(i)+ctemp
60                      cw=cw*cdel
                      l=istep
                      if(l.lt.lx) go to 40
              return
              end
              subroutine fftr(lx,cx,signi)
c  Fourier transform of a real time function.
c  inputs-
c      lx=2**integer
c      cx=x(1)...x(2*lx) , dimensioned as x(2*lx+2)
c      signi = +1. or -1.
c  output-
c      cx(1)...cx(lx+1) the spectrum on 0.le.omega.le.pi
      complex cx(lx), conjg, cmplx, cw, cdel, ca, cb
      call fft(lx, cx, -signi, .5)
      cx(lx+1)=cx(1)
      lxh=lx/2+1
      cw=(0., 1.)
      arg=signi*3.14159265/lx
      cdel=cplx(cos(arg), sin(arg))
      do 10 j=1, lxh
          jr=lx-j+2
          ca=conjg(cx(j))+cx(jr)
          cb=(conjg(cx(j))-cx(jr))*cw
          cx(j)=ca+cb
          cx(jr)=conjg(ca-cb)
10      cw=cw*cdel
      return
      end

```

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```

      subroutine fftri(lx,cx,signi)
c Inverse Fourier transform to a real time function.
      complex cx(lx),cmplx,cw,cdel,conjg,ca,cb
      nh=lx/2+1
      cw=(0.,-1.)
      arg=signi*3.14159265/lx
      cdel=cmplx(cos(arg),sin(arg))
      do 10 j=1,nh
      jr=lx-j+2
      ca=cx(j)+conjg(cx(jr))
      cb=cx(j)-conjg(cx(jr))
      cb=cb*cw
      cx(j)=conjg(ca+cb)
      cx(jr)=ca-cb
10     cw=cw*cdel
      call fft(lx,cx,-signi,1./(2.*lx))
      return
      end

```

```

      subroutine fit(nf,xx,xg,f)
      dimension xx(nf),xg(nf),f(nf)
      dimension a(200),b(200)
      do 10 j=1,nf
      f(j)=0.
      a(j)=0.
10     b(j)=0.
      f(1)=xg(1)/xx(1)
      a(1)=1.
      b(1)=1.
      v=xx(1)
      do 85 j=2,nf
      e=0.
      do 20 i=1,j
20     e=e+xx(j-i+1)*a(i)
      c=e/v
      do 30 i=1,j
30     a(i)=a(i)-c*b(j-i+1)
      do 40 i=1,j
40     b(i)=a(i)
      v=v*(1.-c*c)
      e=0.
      do 50 i=1,j
50     e=e+xx(j-i+1)*f(i)
      c=(e-xg(j))/v
      do 60 i=1,j
60     f(i)=f(i)-c*a(j-i+1)
      e=0.
85     continue
      return
      end

```

```

      subroutine number(fltnum,fmt,x,y,size,orient,iunit)
      real fltnum
      logical*1 fmt(12),null,blnk,num(21),e
      integer x,y,size,orient
      data null/z00/,blnk/' ',e/'e'
      encode(20,fmt,num) fltnum

```

*Levinson Shaper Program.*  
*Not actually used to generate Figs 1 + 2.*

*plot annotating program. Probably won't work on anything but PDP11 Fortran*

```

    ist=1
10   if(num(ist).ne.blk) go to 20
    ist=ist+1
    go to 10
20   iend=ist+1
30   if(num(iend).eq.blk.or.iend.gt.20) go to 40
    if(num(iend).eq.e) iend=iend+1
    iend=iend+1
    go to 30
40   num(iend)=null
    call symbol(num(ist), x, y, size, orient, iunit)
    return
    end
    subroutine symbol(string, x, y, size, orient, iunit)
    logical*1 string(41), t, m, null
    integer x, y, size, orient, ikey
    data t/'t'/, m/'m'/, null/'00'/
    ikey=size+32*orient
    n=1
10   if(string(n).eq.null) goto 20
    n=n+1
    go to 10
20   write(iunit) m, x, y, t, ikey, (string(i), i=1, n)
    return
    end
```

Like pard0 program but gets multichannel data from a disk

```

real x(514), y(514), g(514), b(200), db(514), elog(48)
complex cx(257), cy(257), cg(257), cb(257), cdb(257)
equivalence(x, cx), (y, cy), (db, cdb)
real space(514)
equivalence(g, cg)
complex conjg, cmplx
logical*1 filcy(50)
data filcy/'cy'/
call setmod(11, 128)
call setmod(5, 512)
call setfil(61, '/scr/jon/wavelet', 512+128)
nch=12
nt=512
nt2=nt+2
nth=nt/2
nt2h=nt2/2
idy=1
nb=200
niter=21
nskip=10
amb=1./200.
rmssn=1./amb
call zero(nb, b)
read(61) nbb, (b(i), i=1, nbb)
call zero(nt2, cb)
call move(nb, b, cb)
call fftr(nth, cb, +1.)
ifilcy=icreat(filcy, 6*64+4*8+4) create a disk file for cy
ncl=iclose(ifilcy) close it
nop=iopen(filcy, 2) open it again
do 60 ich=1, nch initialization loop over channels
read(5)(y(i), i=1, nt)
sc=bigest(nt, y)
call scale(1./sc, nt, y)
call taper(nt, y)
call fftr(nth, cy, +1.)
do 50 i=1, nt2h
50 cx(i)=cy(i)/cb(i)
cy(1)=cmplx(real(cy(1)), real(cy(nt2h))) pack folding frequency
nwrw=iwrite(ifilcy, cy, 4*nt) write FT of input data
call fftri(nth, cx, -1.)
elog(ich)=grad(2., nt, x, g)
60 continue
do 200 iter=1, niter iterative descent starts here
alpha=.10*(niter-iter+.5)/niter
en=2.5-.5*((iter-1)/((niter+1)/2))
call zero(nt2, cdb)
nseek=iseek(ifilcy, 0, 0) "rewind" unit containing FT of input data
do 100 ich=1, nch loop over channels
nread=iread(ifilcy, cy, 4*nt) read a channel
cy(nt2h)=aimag(cy(1)) } unpack folding freq
cy(1)=real(cy(1))
do 180 i=1, nt2h } get input from filter and output
180 cx(i)=cy(i)/cb(i)
call fftri(nth, cx, -1.)
elog(ich)=grad(en, nt, x, g)

```

job control language defining  
input unit 5 and output  
units 11 and 61

create a disk file for cy

close it  
open it again

initialization loop over channels

pack folding frequency

write FT of input data

iterative descent starts here

"rewind" unit containing FT of input data

loop over channels

read a channel

unpack folding freq

get input from filter and output  
CB  
CY

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```

if(mod(iter-1,nskip).ne.0)go to 80
ink=ich+nch*((iter-1)/nskip)
call plot(ink,idy,100,nt,cx)
call plot(ink,idy,160+idy*(nt+nb*2),nt,g)
ix=70*ink
iy=0
call number(ealog(ich),'(f10.6)',ix,iy,2,1,9)
80  continue
call fftf(nth,cg,+1.)
call fftf(nth,cx,+1.)  $dB = \sum_{\text{channels}} \bar{X} G B$ 
do 90 i=1,nt2h
90  cdb(i)=cdb(i)-cg(i)*cb(i)*conjg(cx(i))
100 continue
call fftri(nth,cdb,-1.)
do 140 i=1,nb
140 db(i)=(nb-i)*db(i) ) taper db
sc=dot(nb,b,db)/dot(nb,b,b)
do 150 i=1,nb
150 db(i)=db(i)-sc*b(i) ) remove projection on b
sc=bigest(nb,b)/bigest(nb,db)
do 160 i=1,nb
160 b(i)=b(i)-db(i)*alpha*sc ) modify update wavelet
call plot(ink,idy,120+idy*nt,nb,b)
call plot(ink,idy,140+idy*(nt+nb),nb,db)
write(11,170) (ealog(i),i=1,nch)
170 format(16f5.2)
rewind 61
write(61) nb,(b(i),i=1,nb) write wavelet
call zero(nt,cb) ) pad zeros
call move(nb,b,cb)
call fftf(nth,cb,+1.)
sc=(alpha*alpha+amb*amb)*dot(nt2,cb,cb)/nth
do 175 i=1,nt2h
175 cb(i)=(sc+conjg(cb(i))*cb(i))/conjg(cb(i)) ) remove zeros from B so we can divide by it
200 continue
stop
end

```