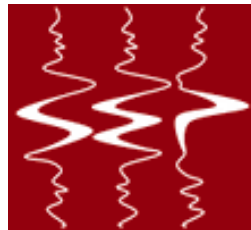


Wave-equation migration Q analysis

Yi Shen

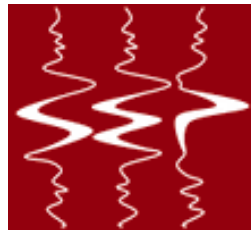
Thesis Defense – Nov 29th, 2016



Wave-equation migration Q analysis

Quality factor that quantifies seismic attenuation

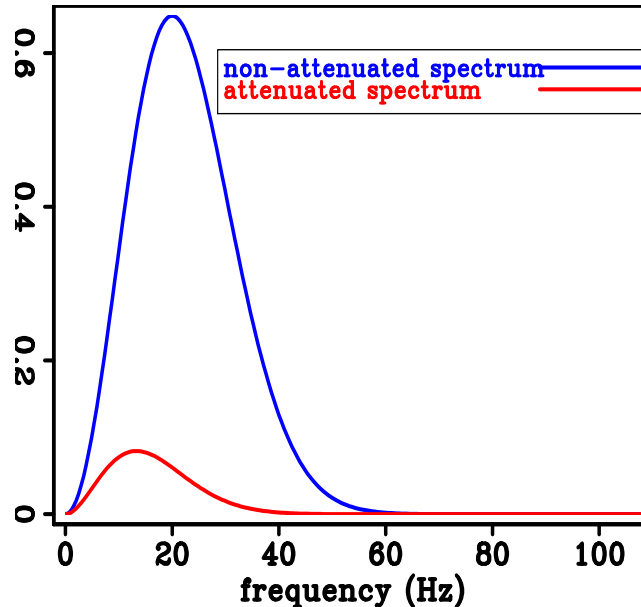
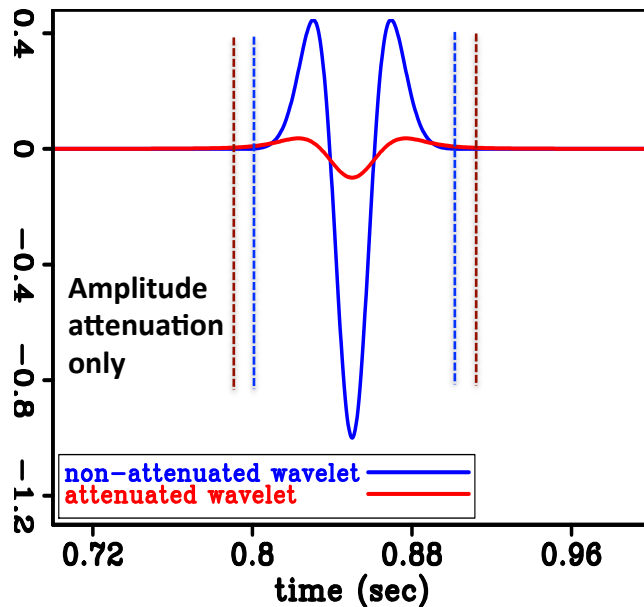
- Small Q means large attenuation
- Strong attenuation: $Q \sim 10-50$
- Nearly no attenuation: $Q > 5000$



Effect of attenuation on amplitudes

Amplitudes

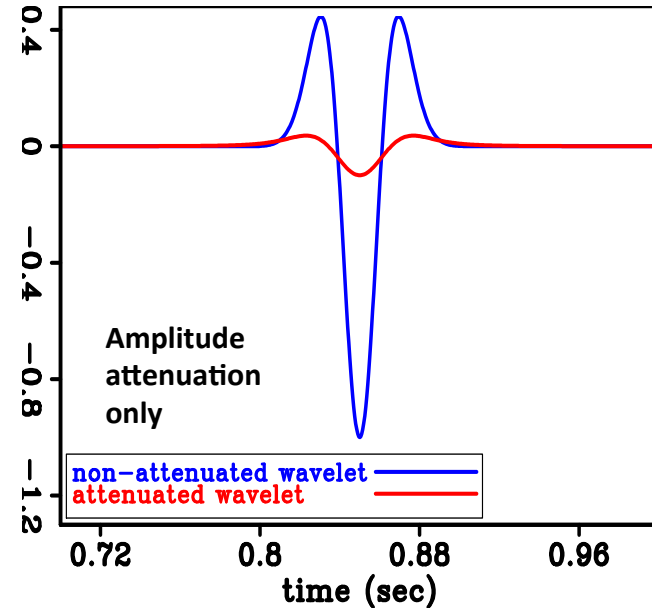
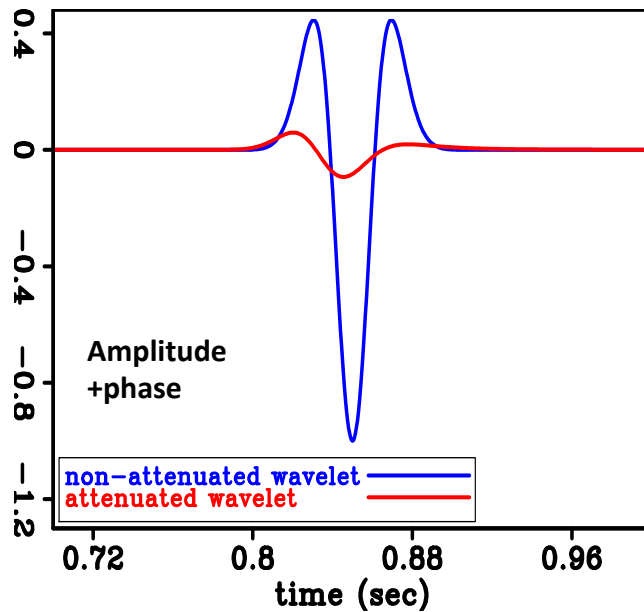
- The **higher** frequencies of a wave are attenuated more than its lower frequencies



Effect of attenuation on phase

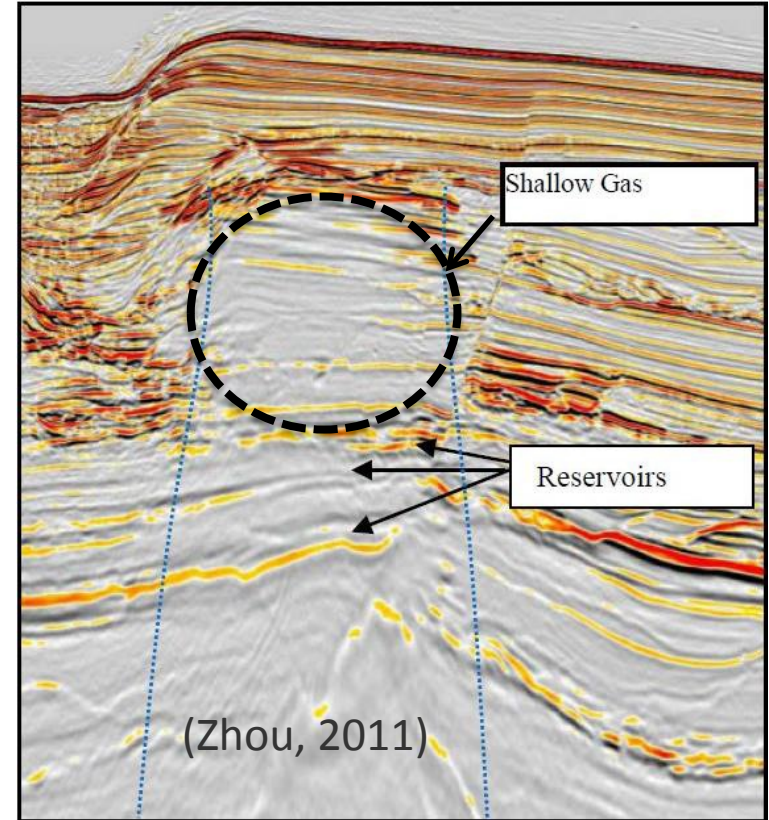
Phase

- The **higher** frequencies of a wave travel faster than its lower frequencies

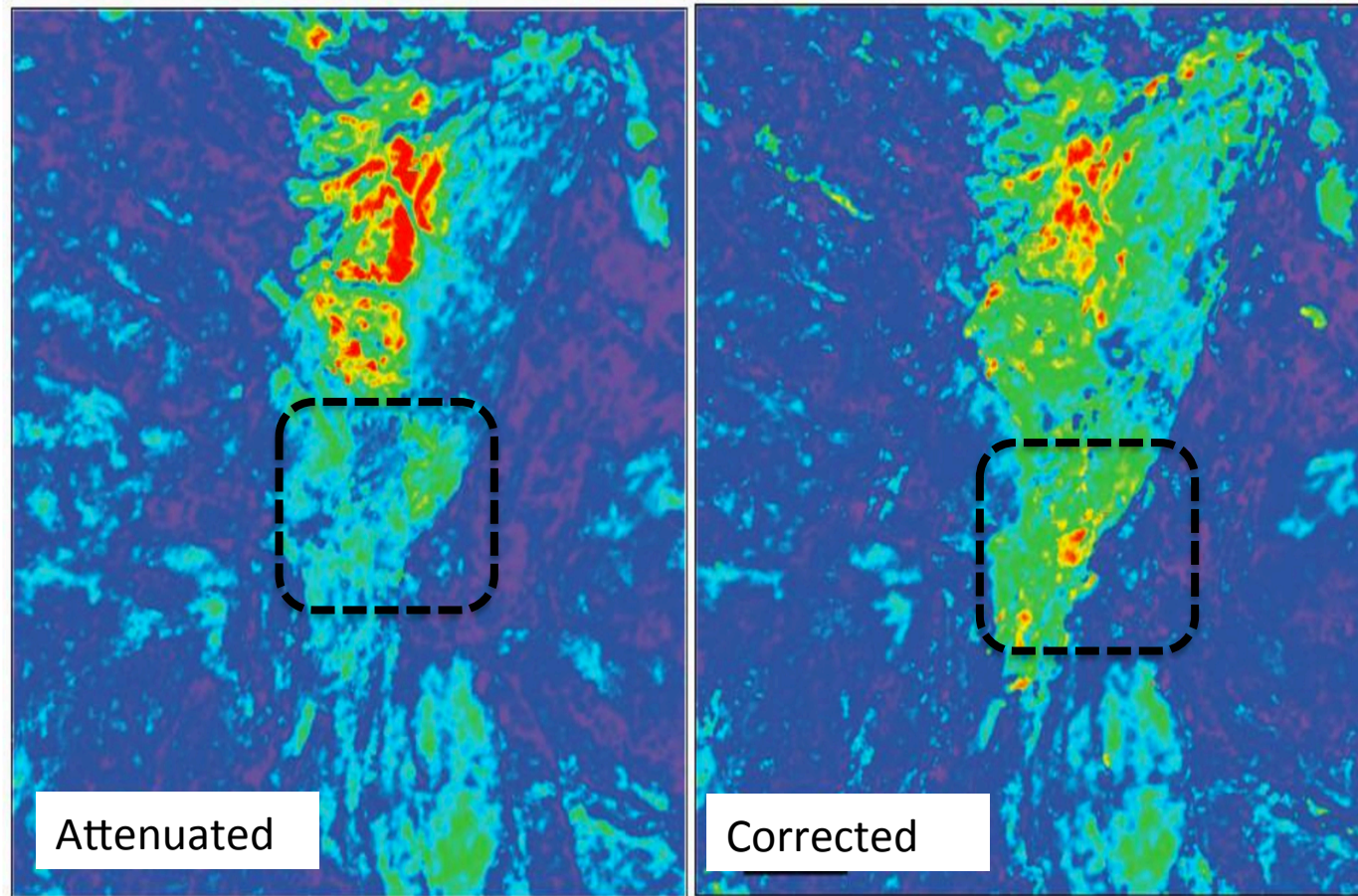


Effect of attenuation on image

- **Migration without Q compensation**
 - Damps amplitudes
 - Lowers resolutions
 - Disperses phases
- ***e.g.*, Gas trapped in sediments**
 - Degrades image quality
 - Makes identification and interpretation inaccurate

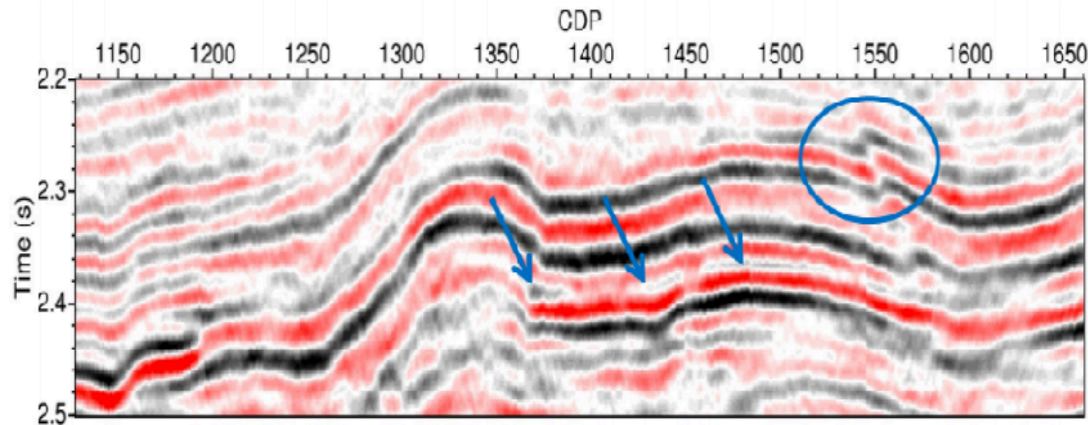


Effect of attenuation on reservoir characterization

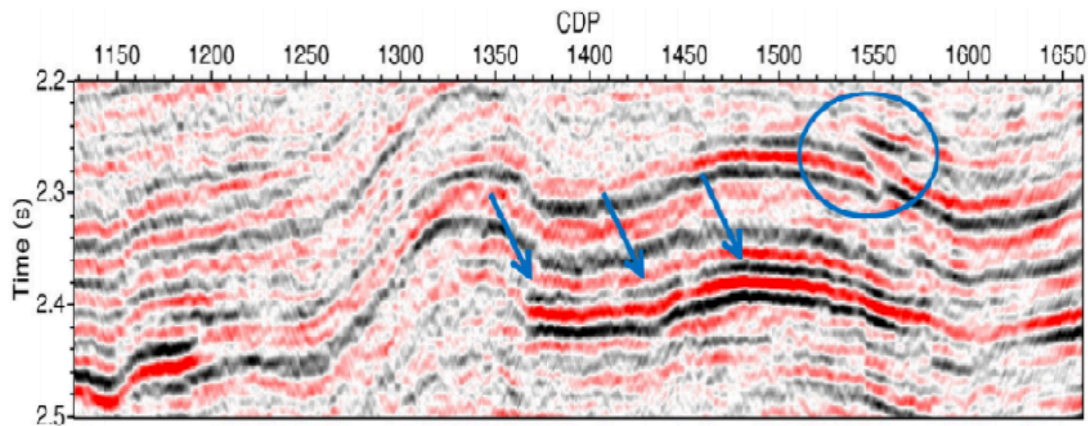


(Francis, 2016)

Effect of attenuation on reservoir characterization



Attenuated



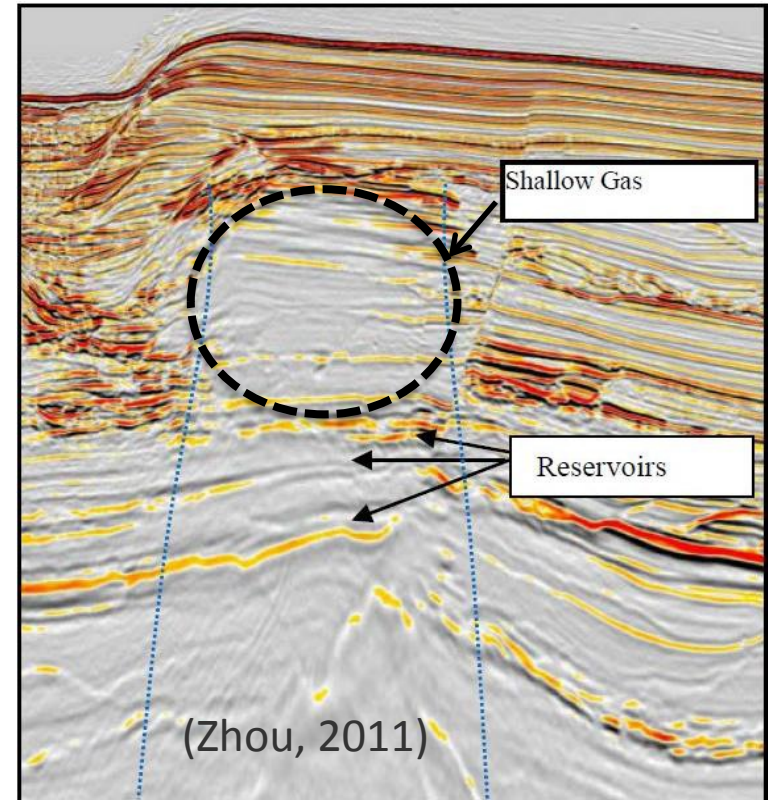
Corrected

(Chen et al., 2016)

(b)

Motivation

- **Goal of my study**
 - Target the attenuation caused by clouds/pockets
 - Understand and quantify the attenuation effects
 - Create and accurate Q model
 - Use the Q estimates to enhances seismic image quality



Thesis chapters

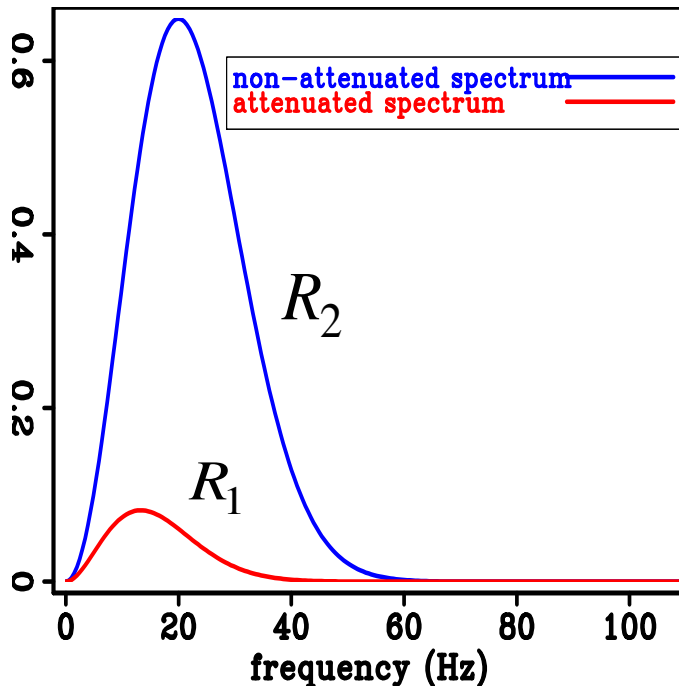
- **Chapter 1:** Introduction
- **Chapter 2:** Wave-Equation Migration Q Analysis
- **Chapter 3:** Rock physics constrained WEMQA
- **Chapter 4:** Multi-parameter inversion of velocity and Q using wave-equation migration analysis
- **Chapter 5:** Field data application
- **Chapter 6:** Conclusions

Thesis chapters

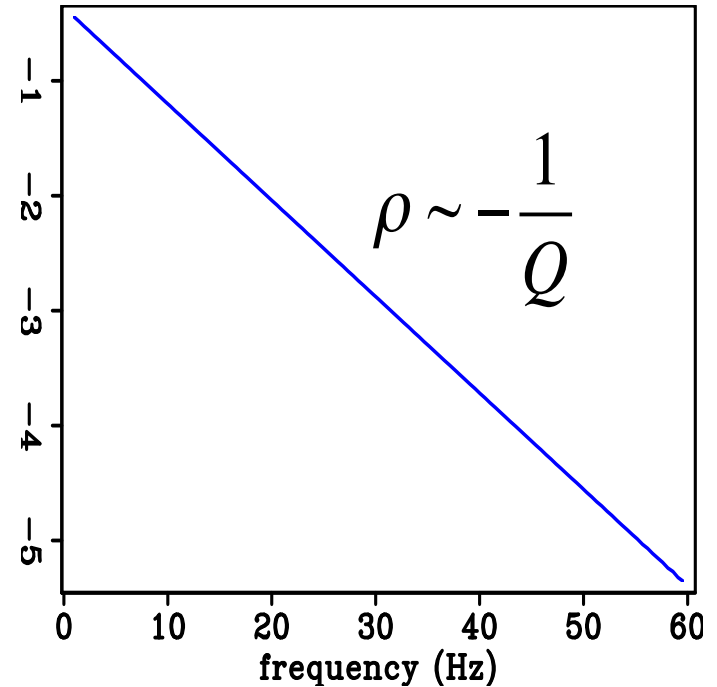
- **Chapter 1:** Introduction
- **Chapter 2:** Wave-Equation Migration Q Analysis
- **Chapter 3:** Rock physics constrained WEMQA
- **Chapter 4:** Multi-parameter inversion of velocity and Q using wave-equation migration analysis
- **Chapter 5:** Field data application
- **Chapter 6:** Conclusions

- Background
- Theory of wave-equation migration Q analysis
- Numerical examples
 - Synthetic examples
 - 3D field data examples
- Conclusions

Spectral ratio method



$$\ln\left(\frac{R_1}{R_2}\right)$$

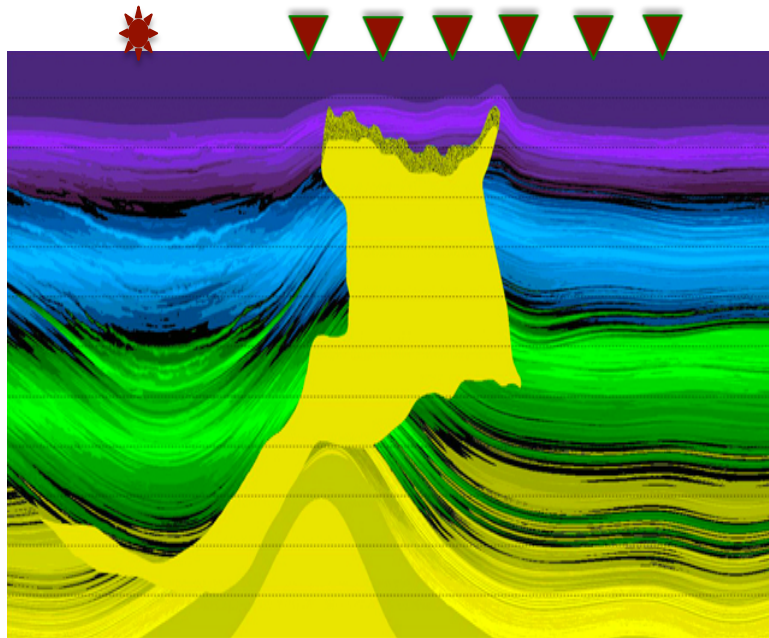


(Tonn, 1991)

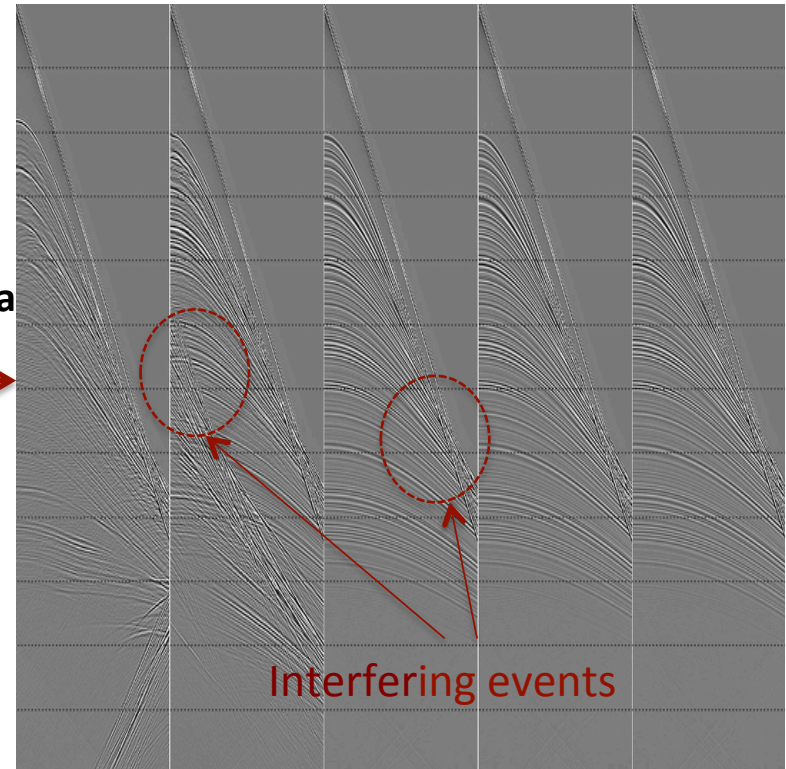
Traditional approach

- Quantify attenuation effects in **data space** before seismic migration
- Update Q model using **ray-based** tomography

Seismic data: 5 shot gathers



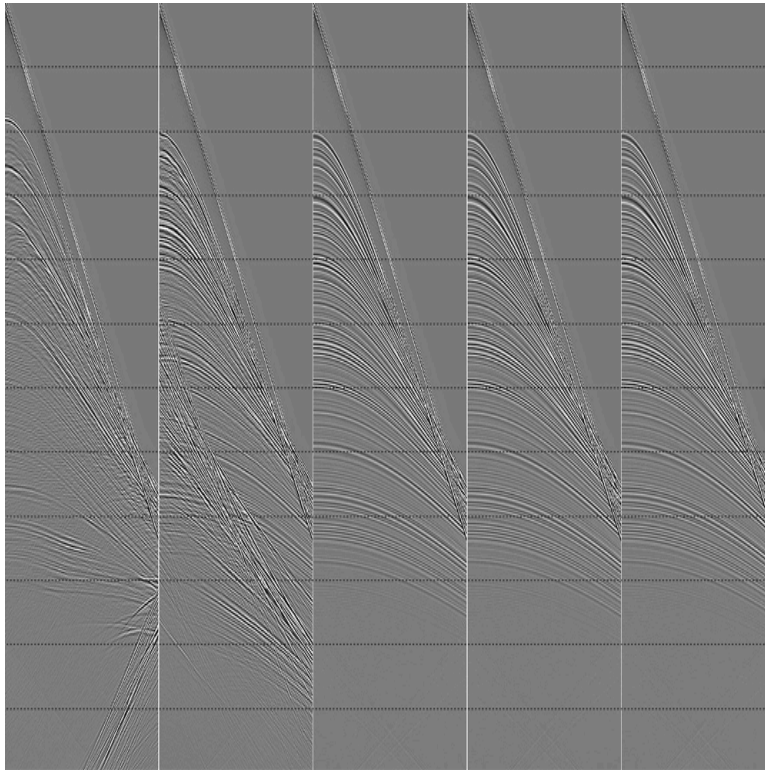
Recorded
seismic data



Synthetic examples:

<http://www.spectrumgeo.com/imaging-services/land-environment/depth-processing/pre-stack-depth-migration>

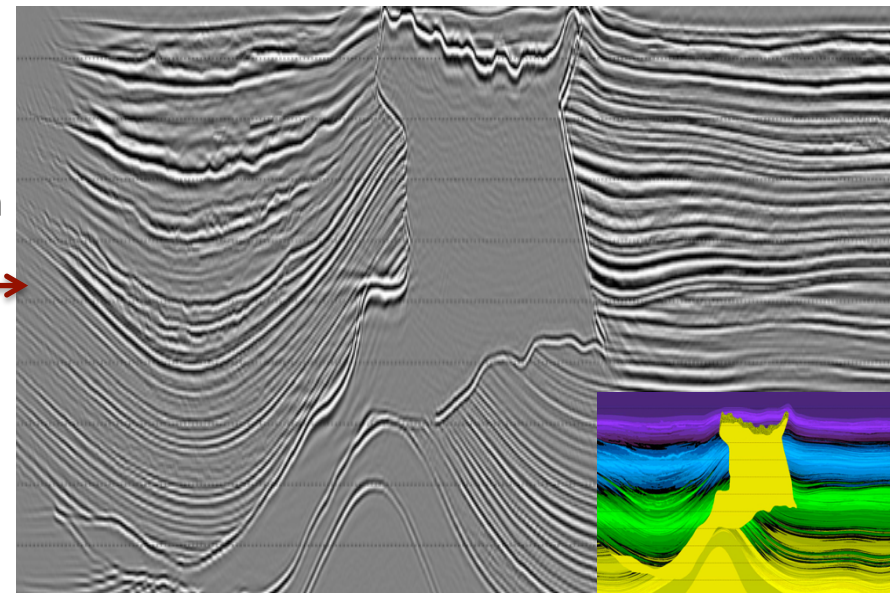
Seismic data: shot gathers



Seismic
migration

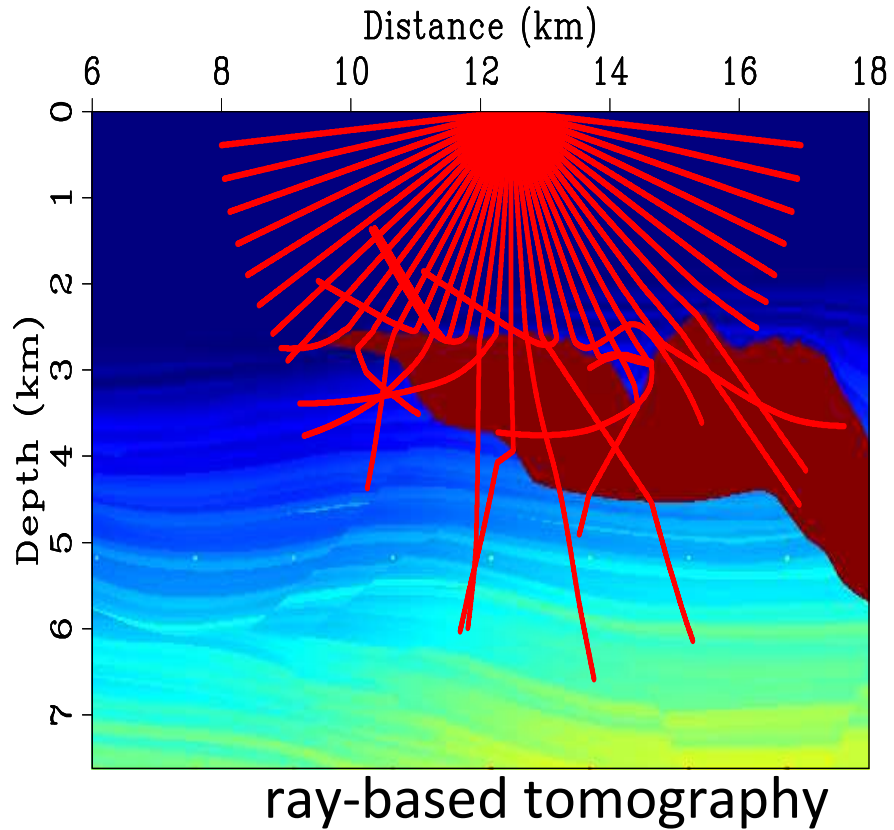


Seismic migrated image



Synthetic examples:

<http://www.spectrumgeo.com/imaging-services/land-environment/depth-processing/pre-stack-depth-migration>

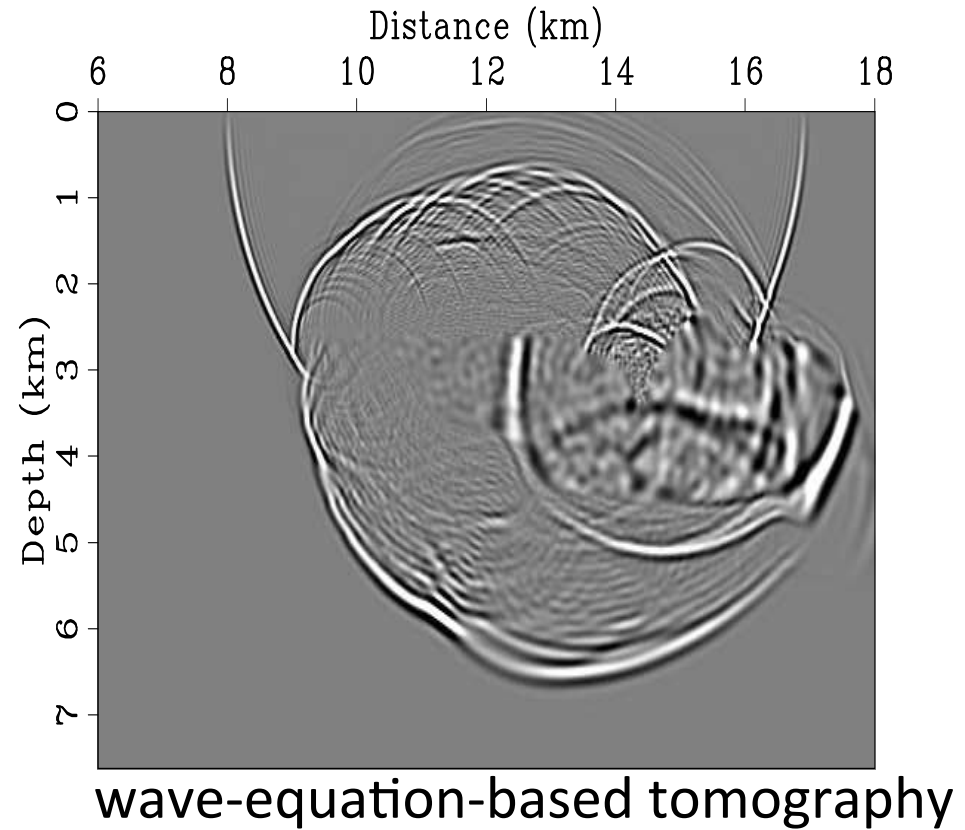
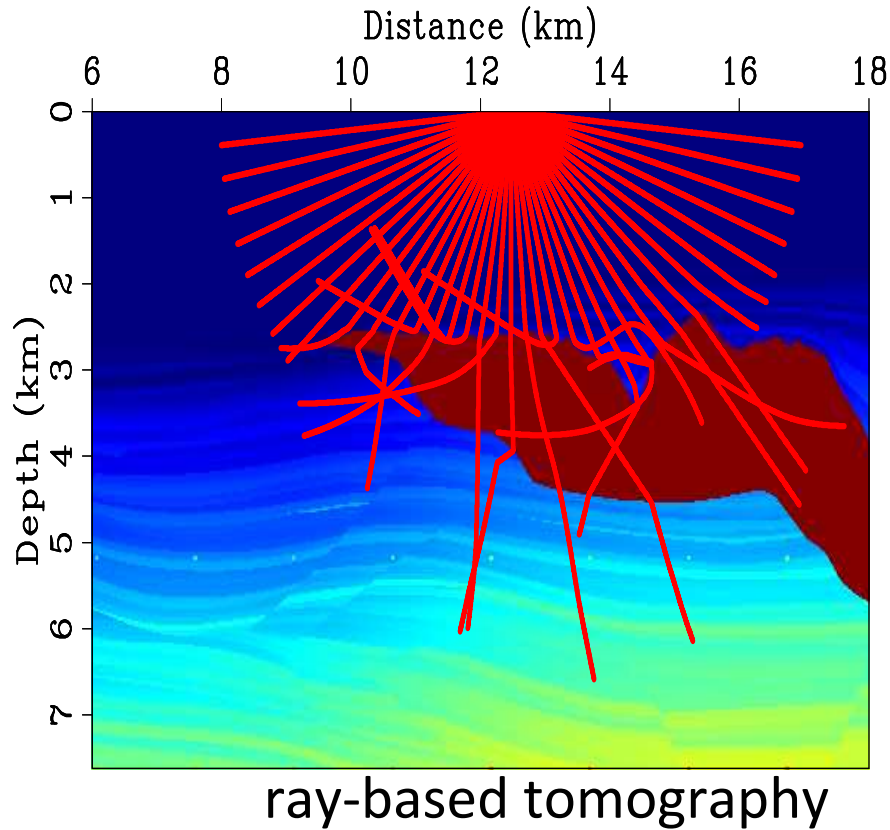


- High-frequency approximation
- Oversimplifies multi-pathing

(Tang, 2011)

New approach: wave-equation-based tomography

- Background
- Theory
- Synthetic and field data examples
- Conclusions



(Tang, 2011)

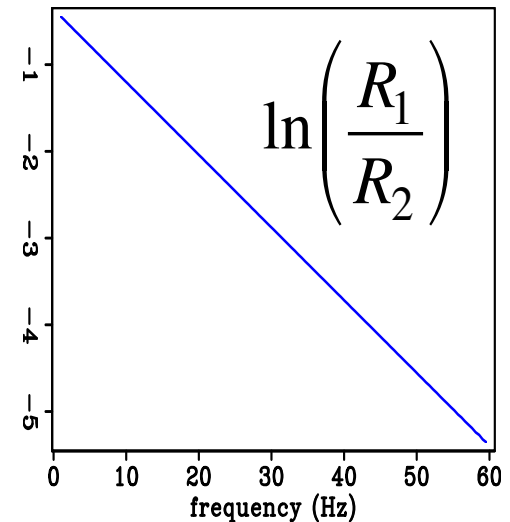
- **Quantify attenuation effects in **image space** after seismic migration**
 - Suppresses the noise
 - Simplifies and focuses the events
 - Can be implemented in a target-oriented fashion
- **Update Q model using **wave-equation based tomography****
 - Handle strong heterogeneities in the subsurface (e.g., salt body)
- ****Wave-equation migration** Q analysis (WEMQA)**

Objective function

- Define ρ as the effect of attenuation (**effect of Q**) on seismic **migrated images**

$$J = \frac{1}{2} \sum_{\mathbf{x}} |\rho(\mathbf{x}; Q)|^2$$

\mathbf{x} is each a spatial location in the image space
 Q is the current model for quality factor



Spectral ratio method

Reference migrated image

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

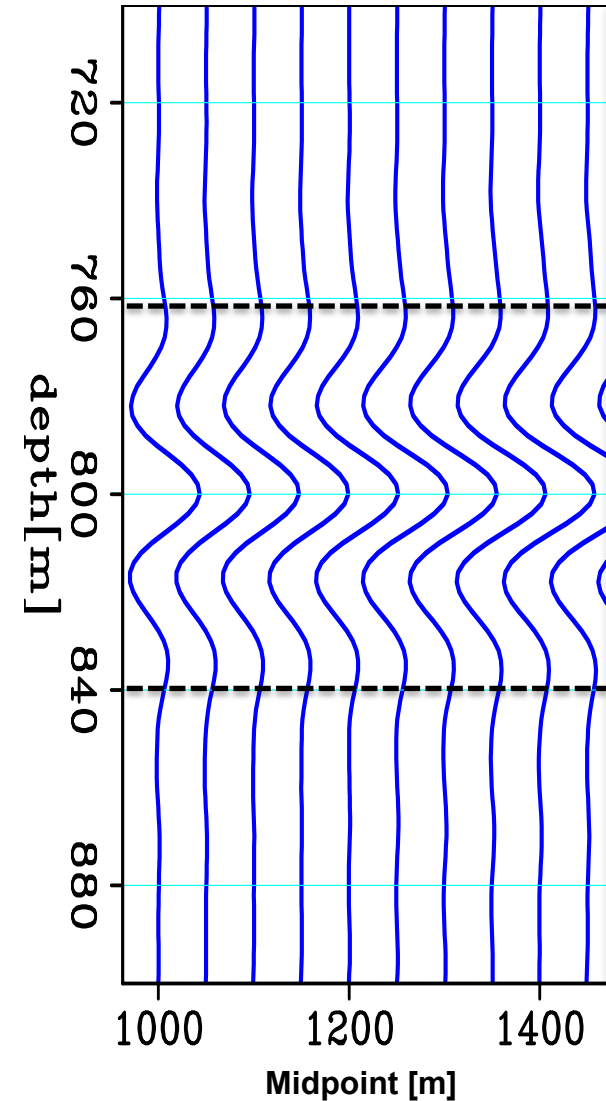
Reference image (spectrum R_2)

True model: $Q_2=30$

RMS amplitudes:
1.5

Events at $z=800$ m

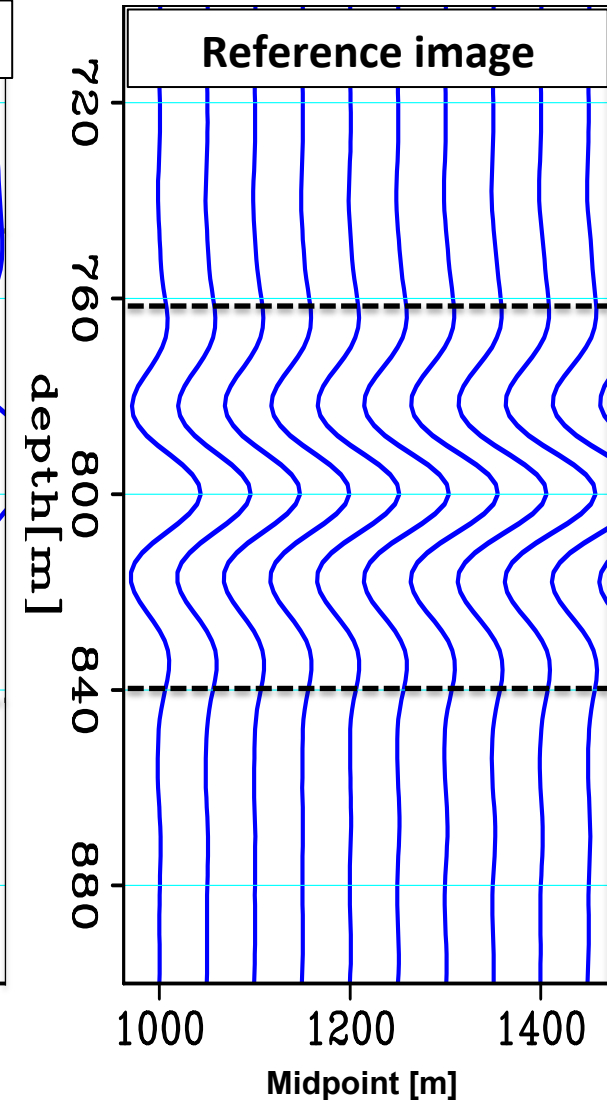
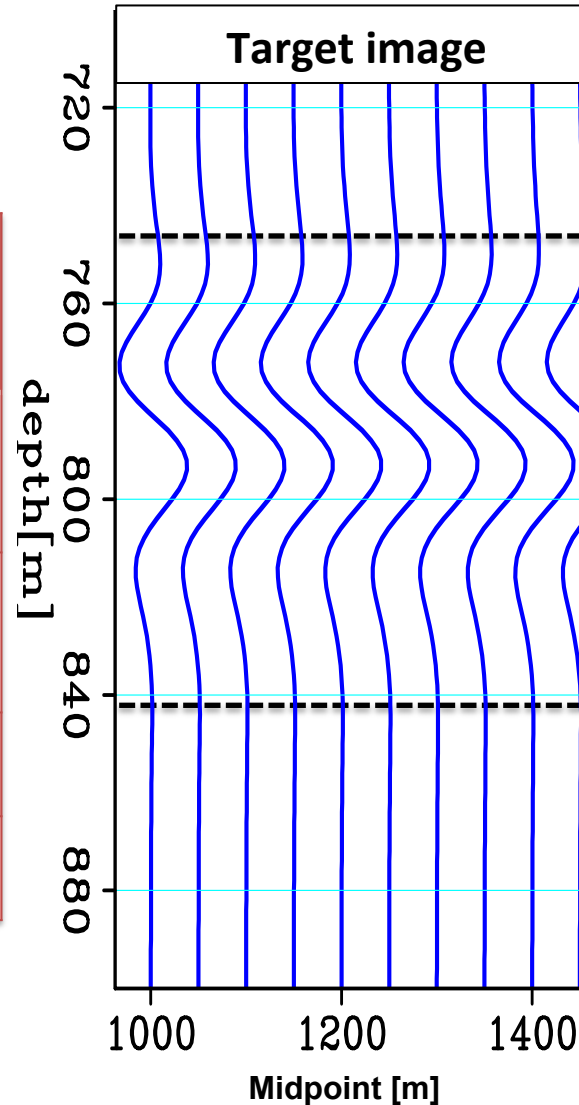
Symmetric wavelets



Migrated image using **inaccurate** Q

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

Target image (spectrum R_1)
Current model: $Q_1=10,000$
RMS amplitudes: 0.13
Up-shifted events
Stretched wavelets



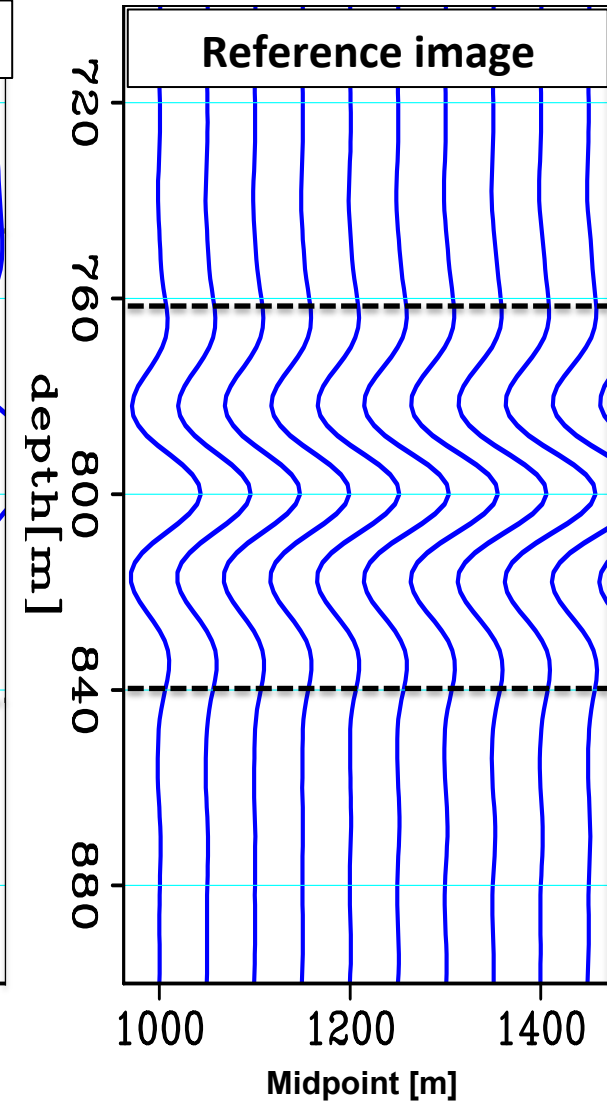
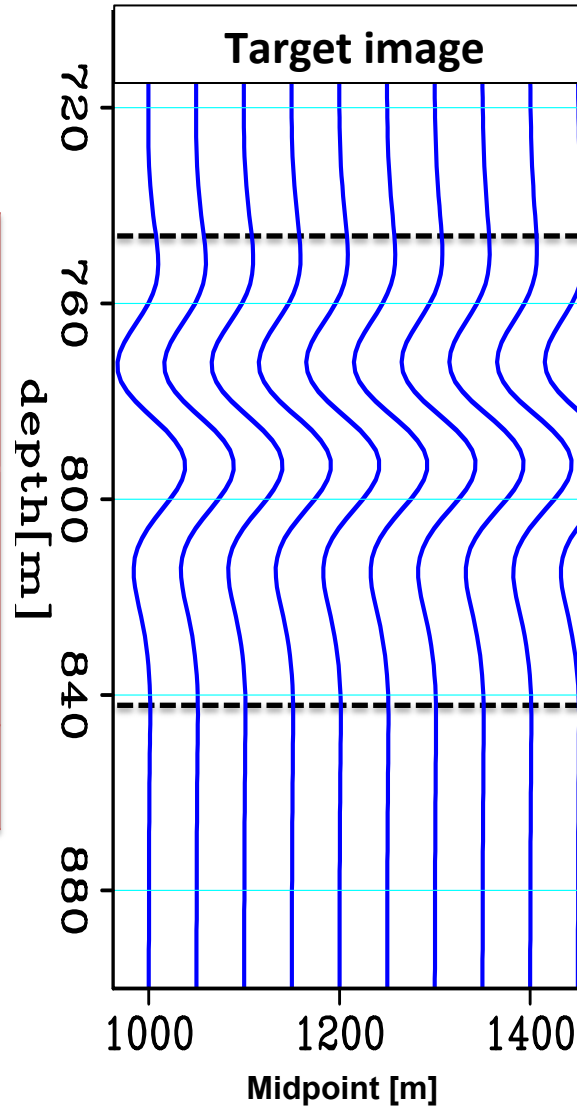
Migrated image using **inaccurate** Q

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

Under-
compensated
($Q_1 > Q_2$)

Higher
frequencies are
attenuated

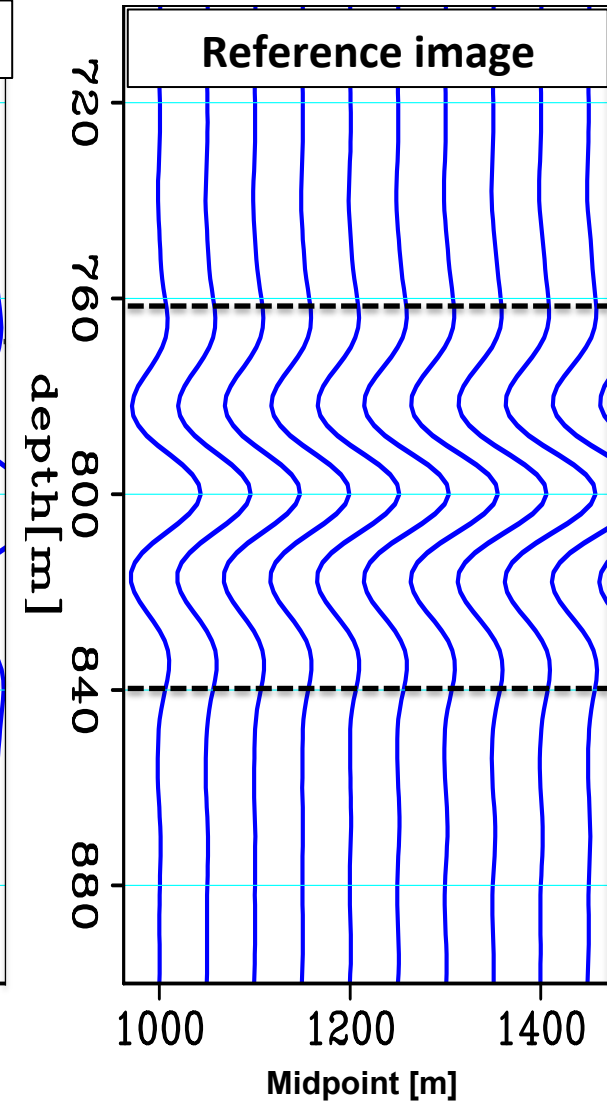
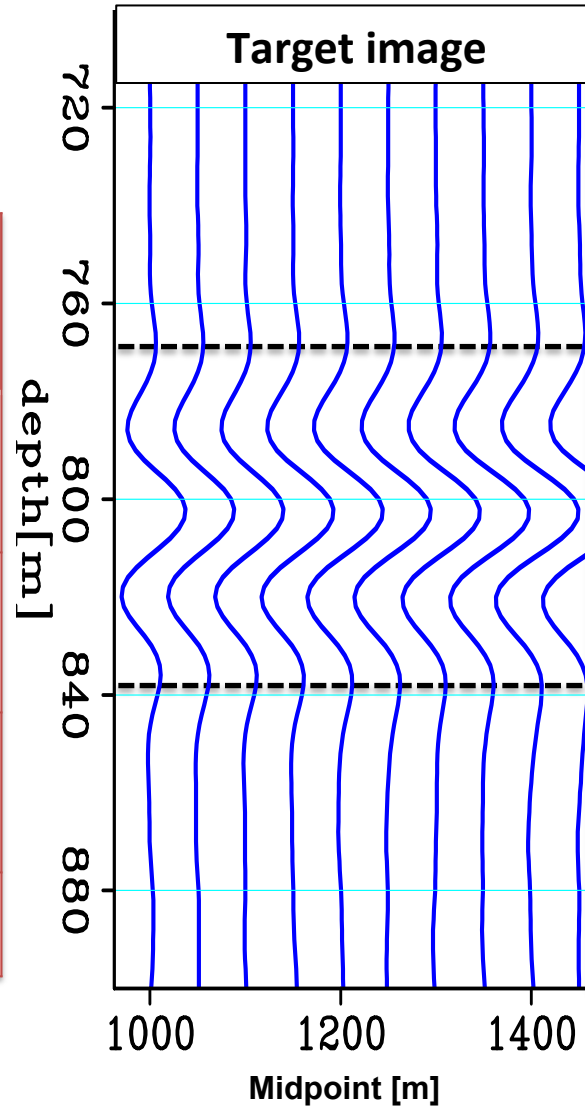
$\ln(R_1/R_2) \Rightarrow \rho < 0$



Migrated image using **inaccurate** Q

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

Target image (spectrum R_1)
Current model: $Q_1=25$
RMS amplitudes: 3.2
Down-shifted events
Squeezed wavelets



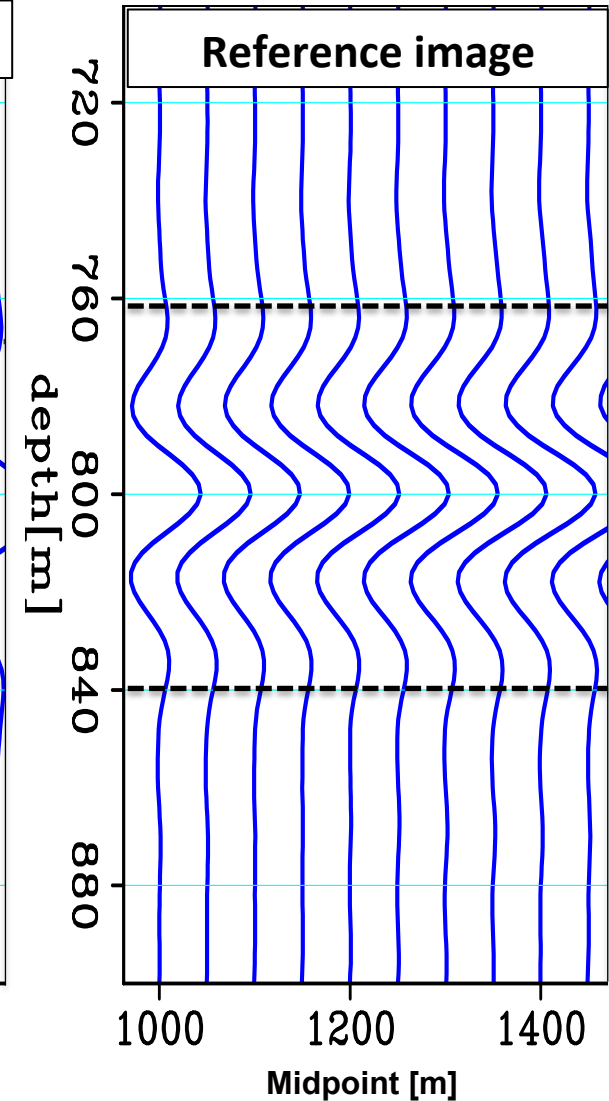
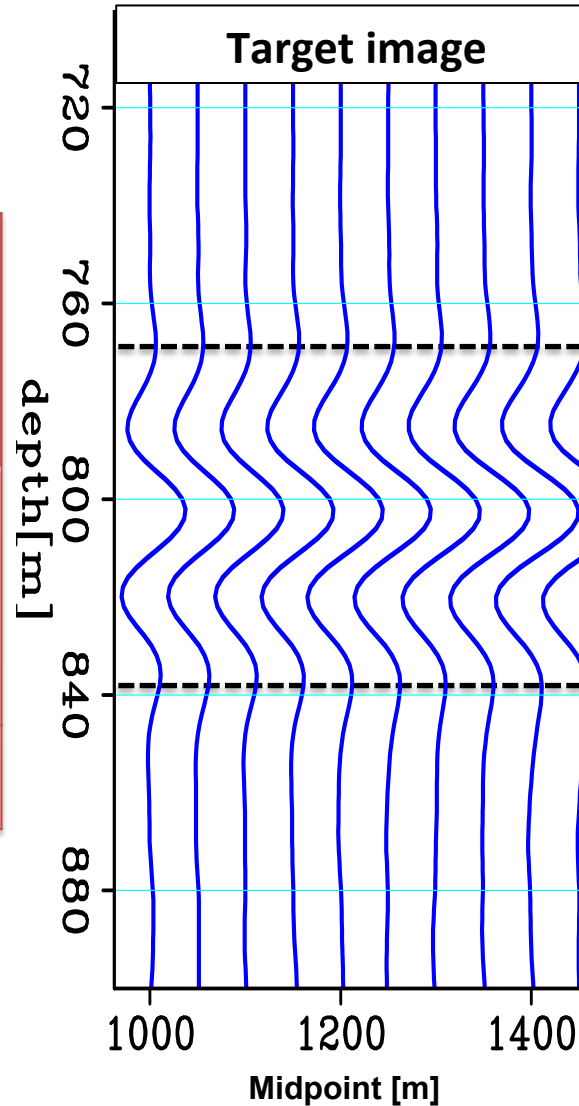
Migrated image using **inaccurate** Q

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

Over-
compensated
($Q_1 < Q_2$)

Higher
frequencies are
over-gained

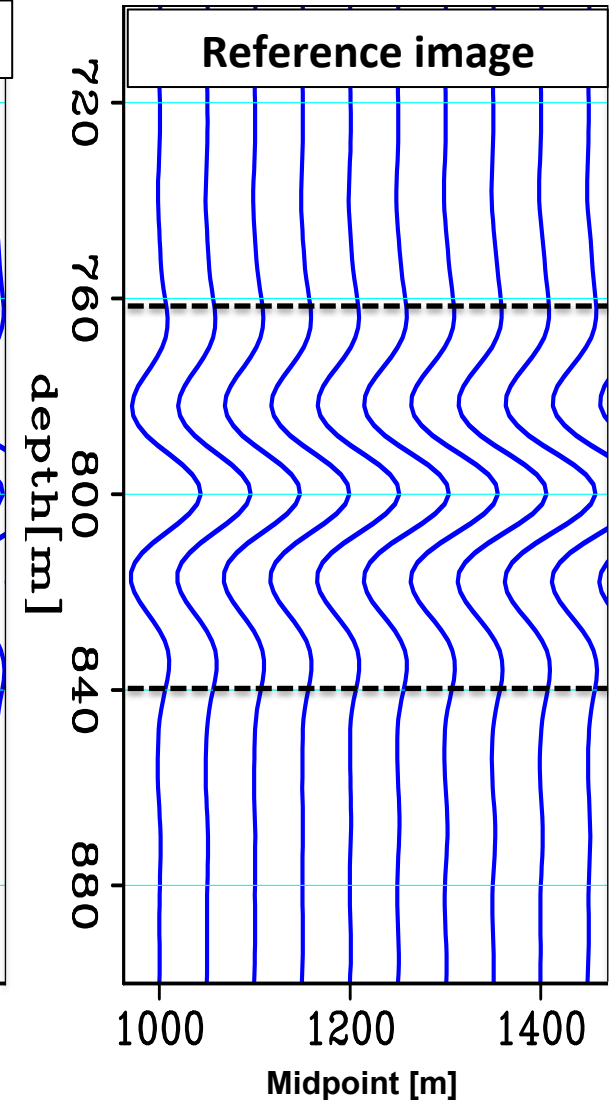
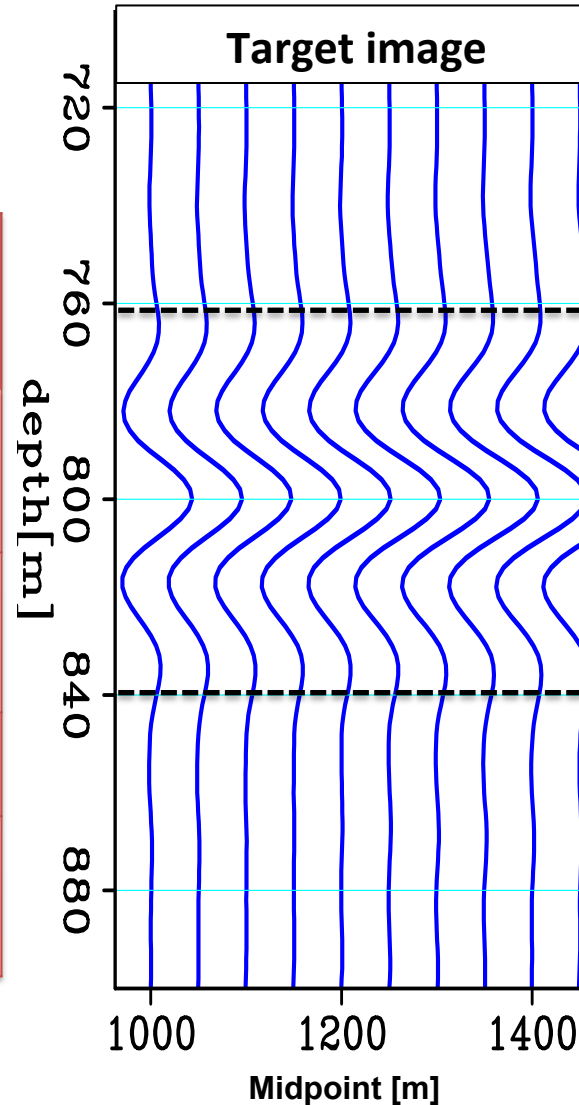
$\ln(R_1/R_2) \Rightarrow \rho > 0$



Migrated image using **inaccurate** Q

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

Target image (spectrum R_1)
Current model: $Q_1=30$
RMS amplitudes: 1.5
Non-shifted events
Non-deformed wavelets

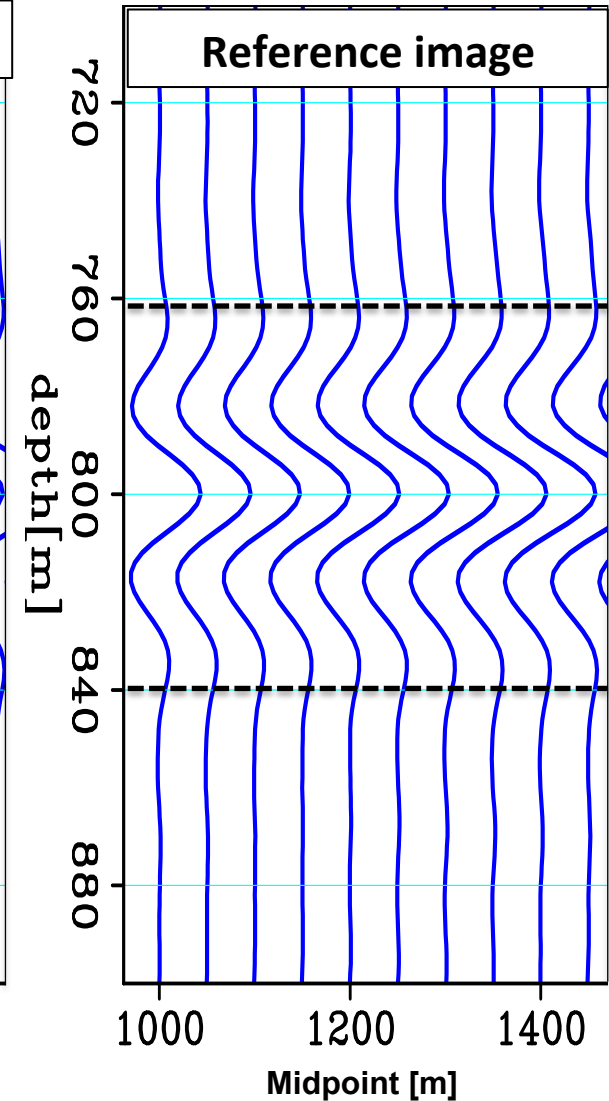
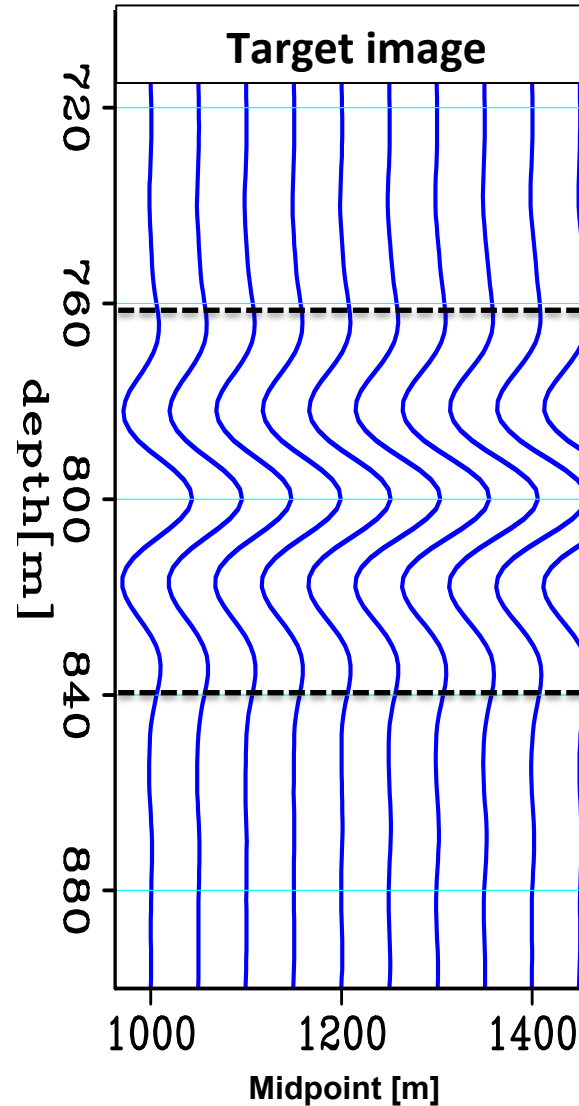


Migrated image using **inaccurate** Q

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

Adequately-
compensated
($Q_1 = Q_2$)

$$\ln(R_1/R_2) \Rightarrow \rho = 0$$



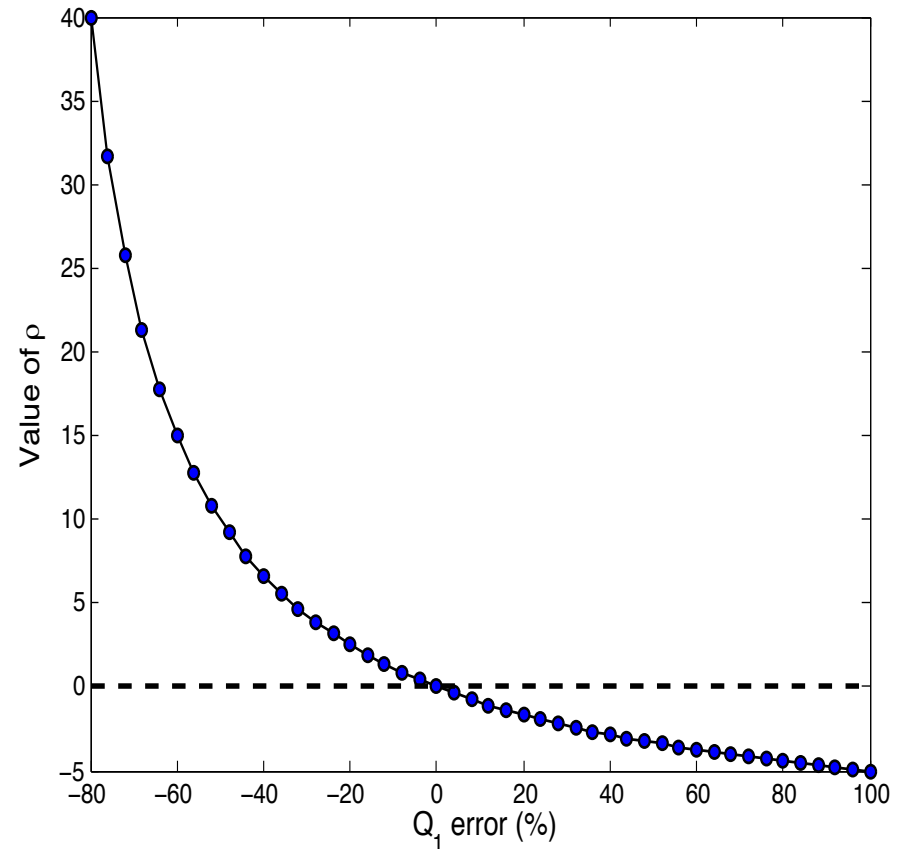
Objective function:

$$J = \frac{1}{2} \sum_{\mathbf{x}} \left| \rho(\mathbf{x}; Q) \right|^2$$

Slope

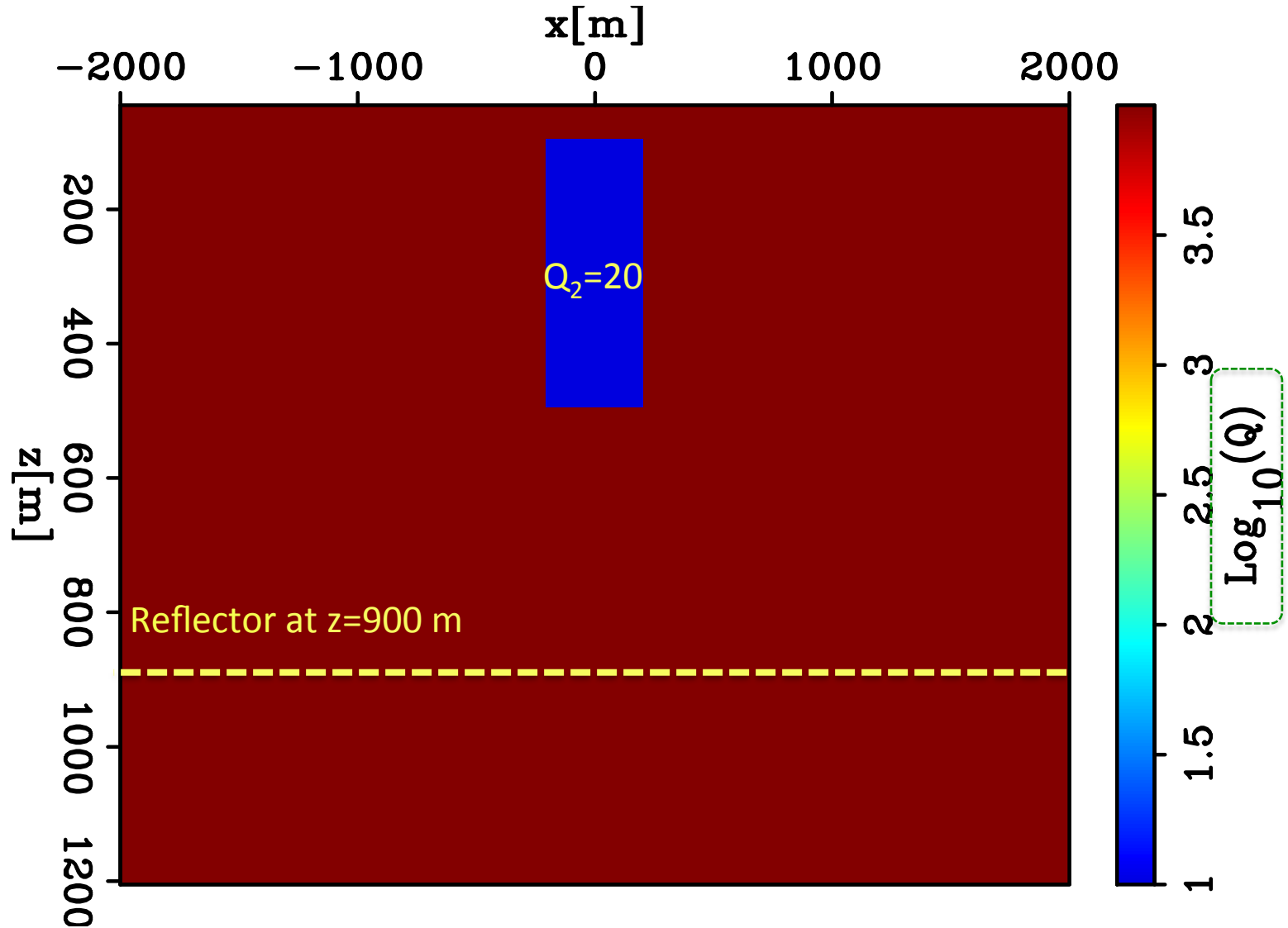
$$\ln \left(\frac{R_1}{R_2} \right)$$

Reference spectrum



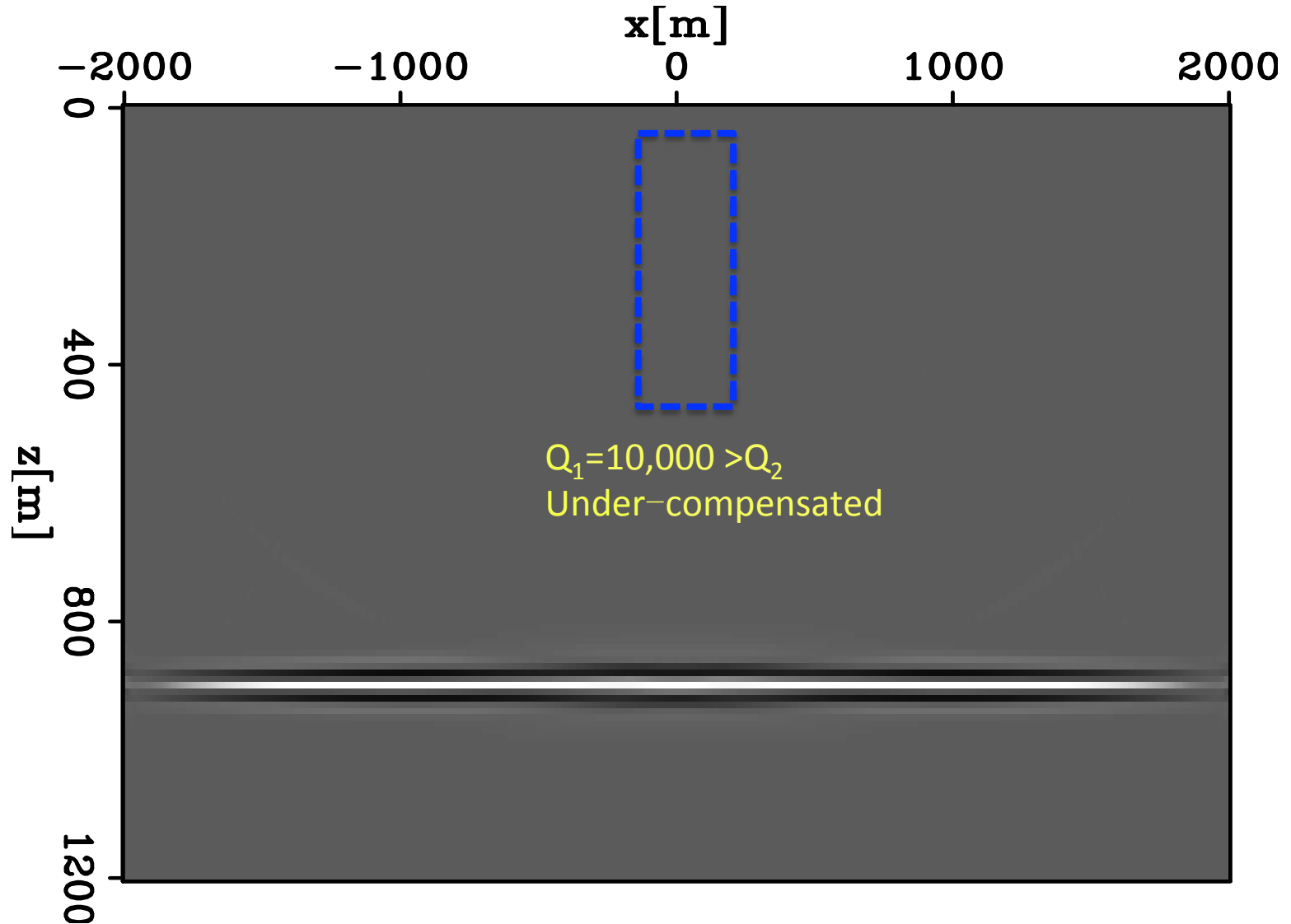
True Q model

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



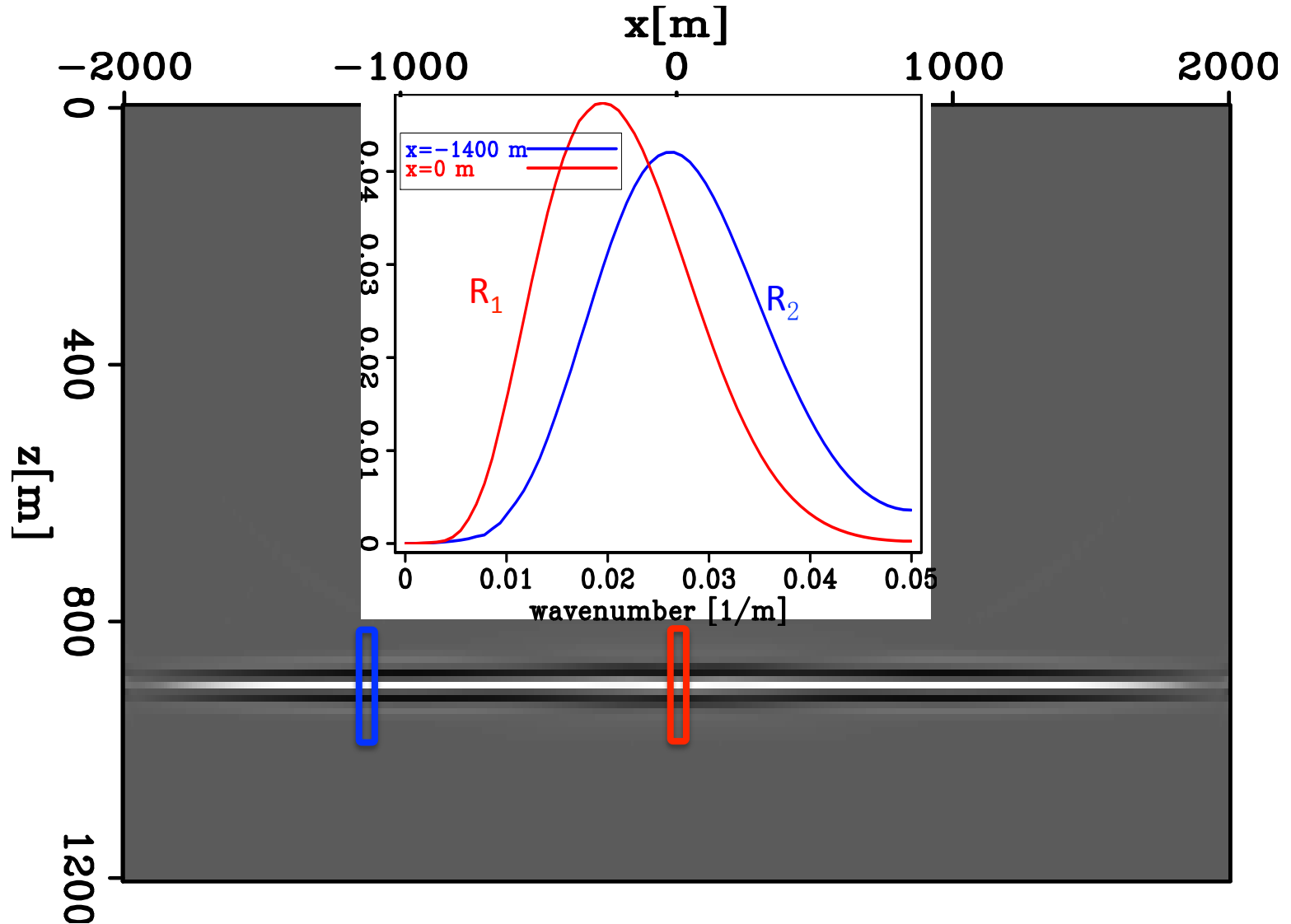
Attenuated image: migrated image at zero subsurface offset (stacked image)

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

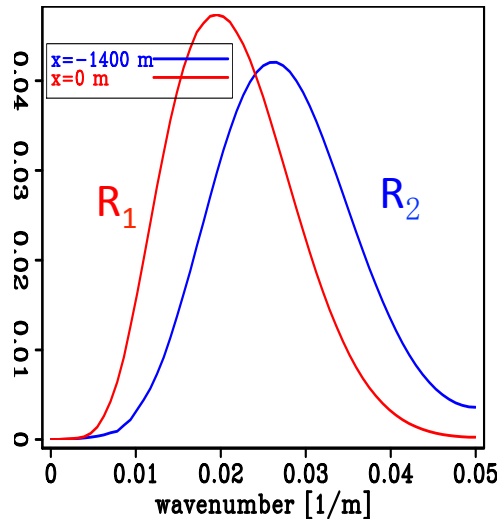


Stacked method

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

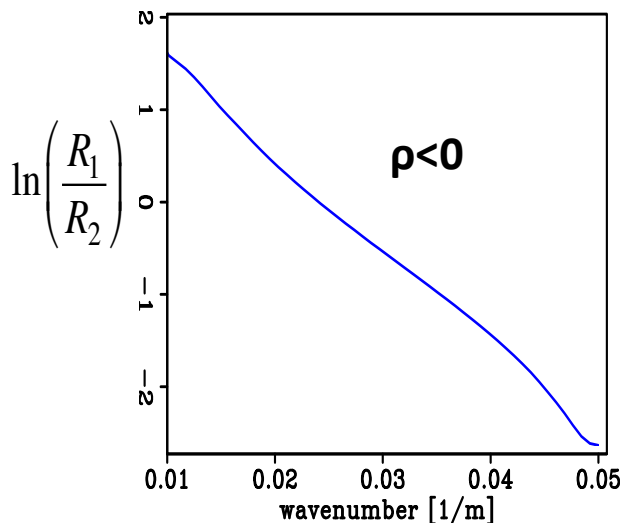


Stacked method

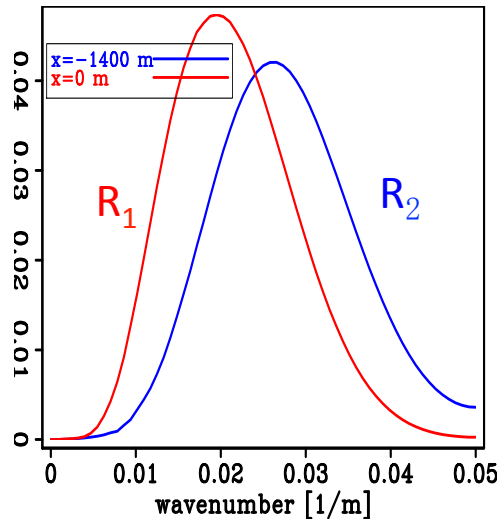


$$\ln \left(\frac{R_1(\mathbf{k}')}{R_2(\mathbf{k}')} \right) = \rho \left| \mathbf{k}' \right| + G_0$$

- Wavenumber domain

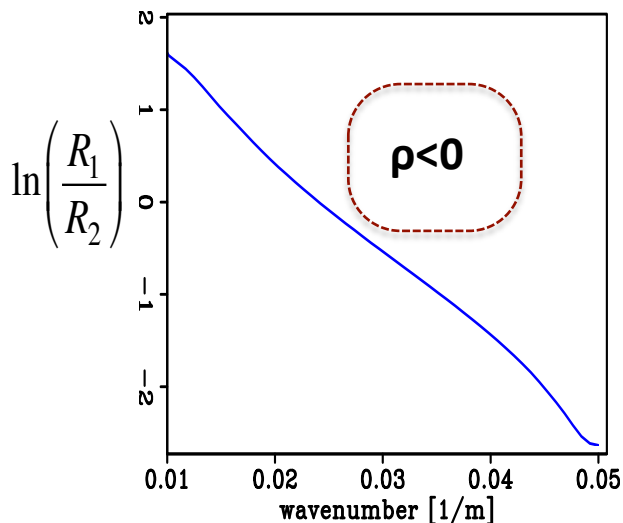


Stacked method

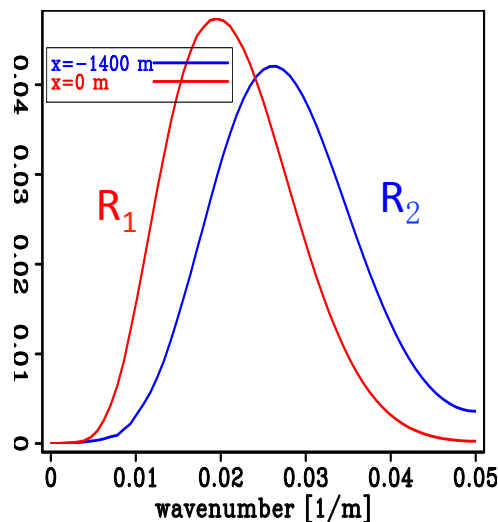


$$\ln \left(\frac{R_1(\mathbf{k}')}{R_2(\mathbf{k}')} \right) = \rho |\mathbf{k}'| + G_0$$

- $Q_1=10,000 > Q_2$
- The image is under-compensated (attenuated)
- $\rho < 0$

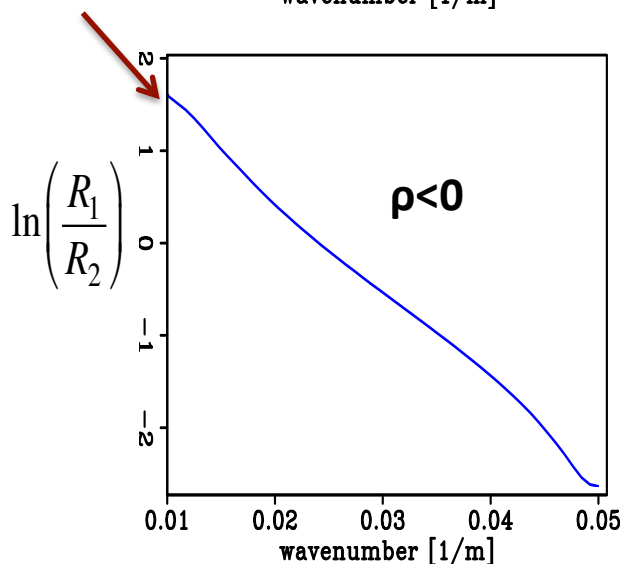


Stacked method



$$\ln \left(\frac{R_1(\mathbf{k}')}{R_2(\mathbf{k}')} \right) = \rho |\mathbf{k}'| + G_0$$

- Frequency-independent factors
 - Different illumination caused by acquisition limitations
 - Different reflection coefficients of different reflectors
 - Different geometrical spreading because of different wave-paths.



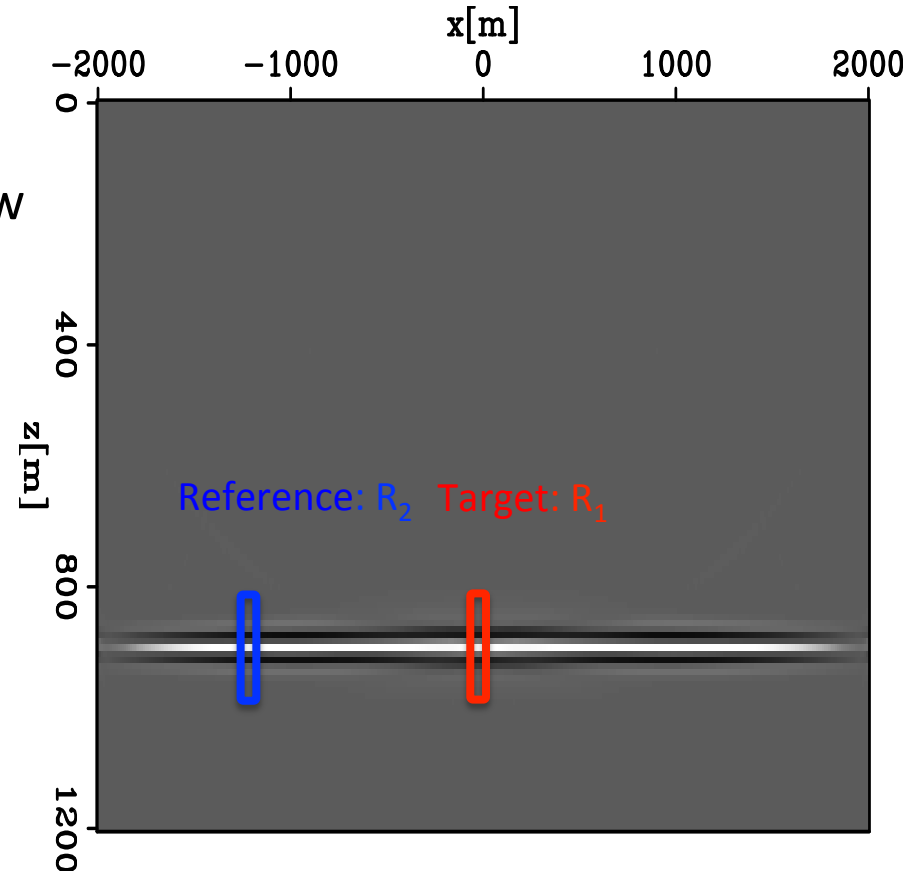
Stacked method

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

- Select one or more surface locations as reference traces
- At each image point x , I use a window of which the center is x
- Compare the windowed spectra for ρ : reference spectra and target spectra

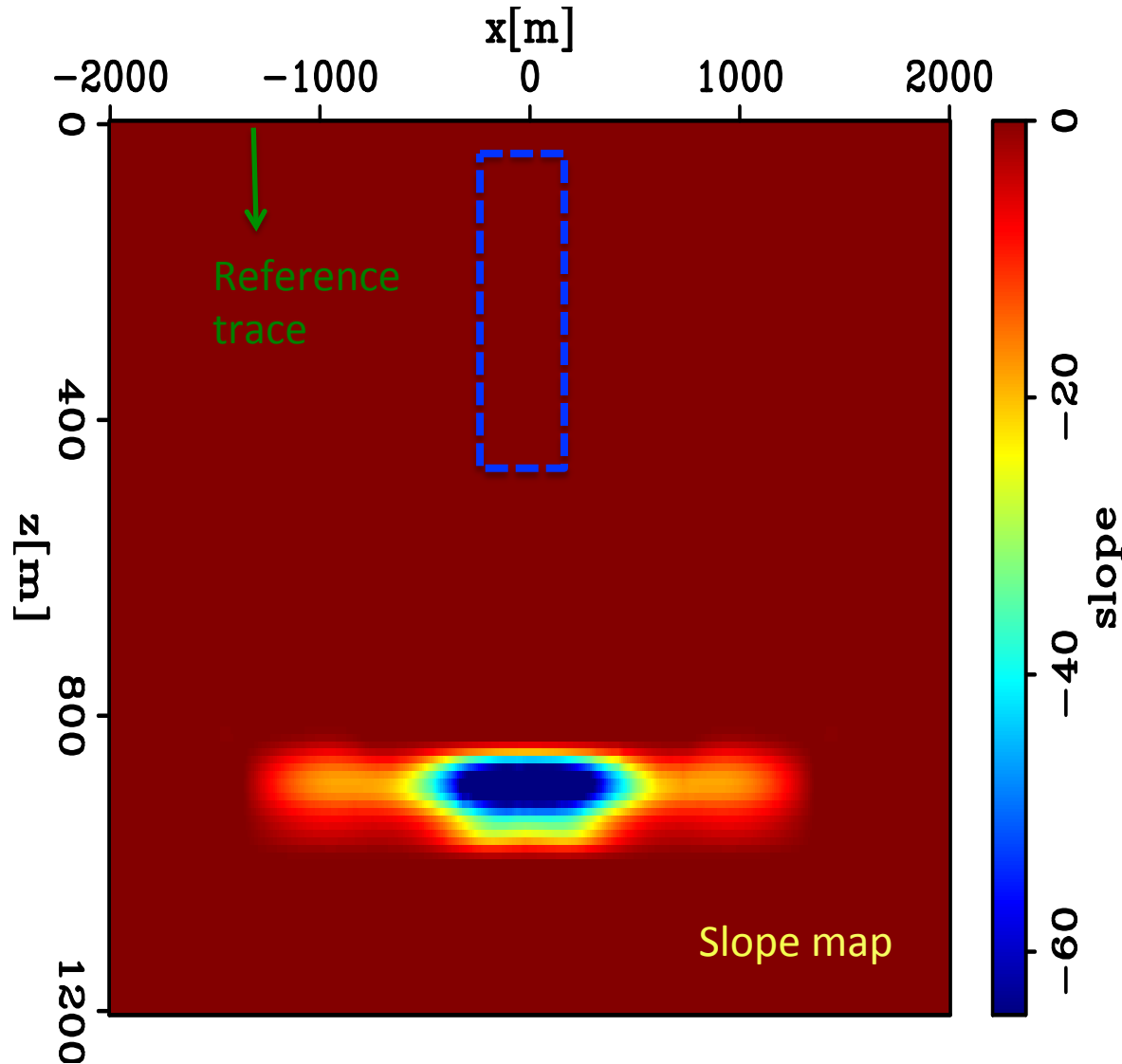
$$\ln\left(\frac{R_1(\mathbf{k}')}{R_2(\mathbf{k}')}\right) = \rho|\mathbf{k}'| + G_0$$

- The windows are compared at the same depth



Stacked method

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

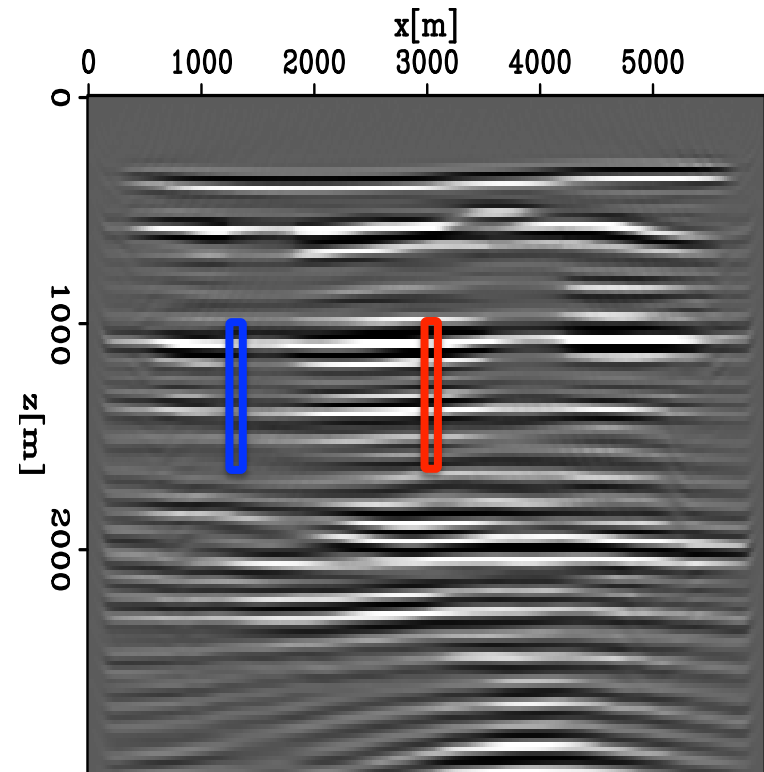


Red: non-attenuated regions
Blue: attenuated regions

Stacked method

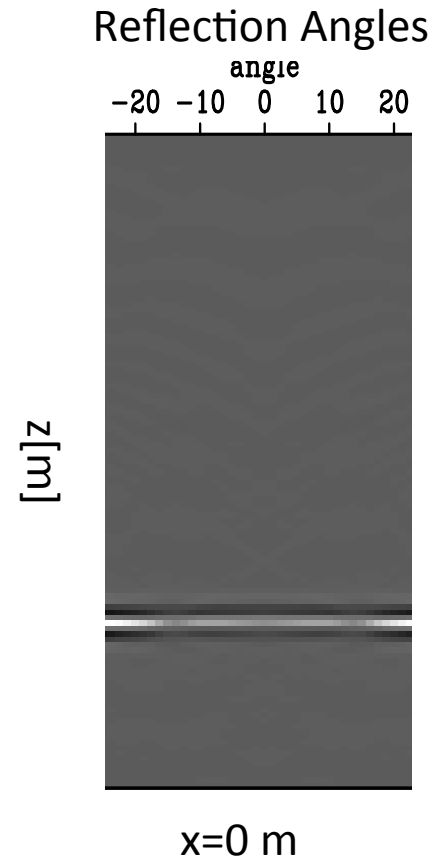
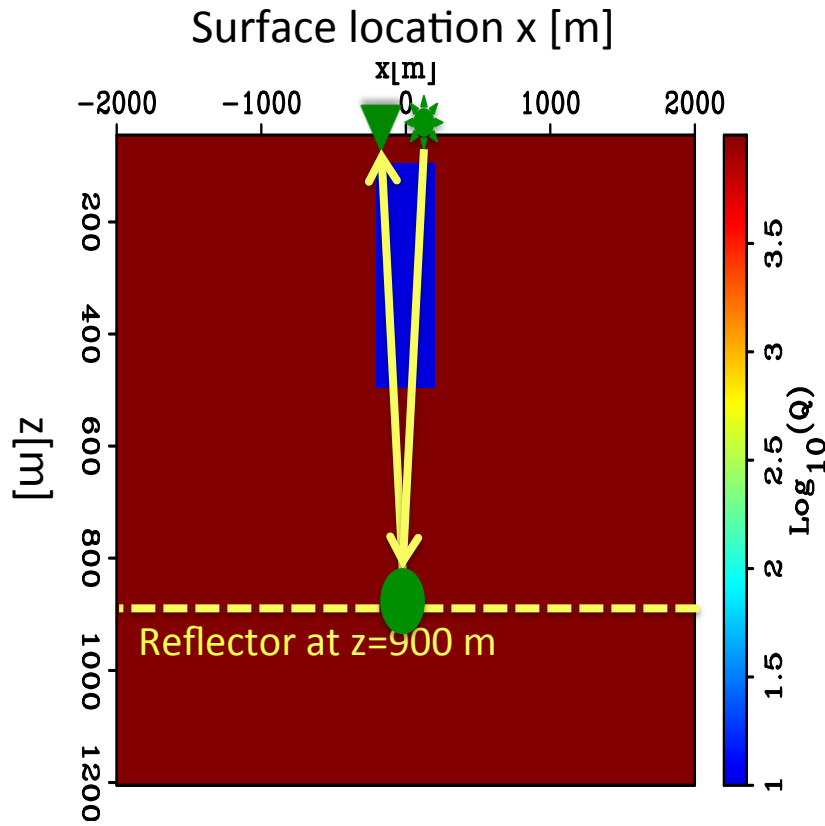
Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

- **Stacked method using windows wide in depth**
 - The spectral variations caused by structure differences in each window are statistically the same
 - Does not represent the effect of Q on its image point
 - Mixes the Q effects from different reflection angles
- **Prestack method: angle domain common image gather (ADCIG)**



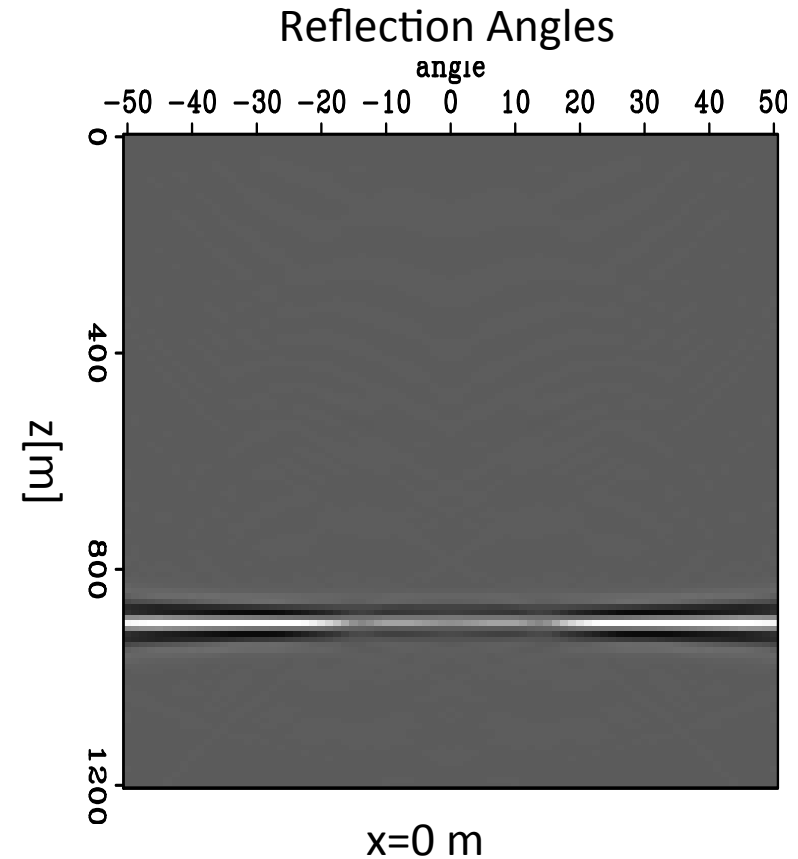
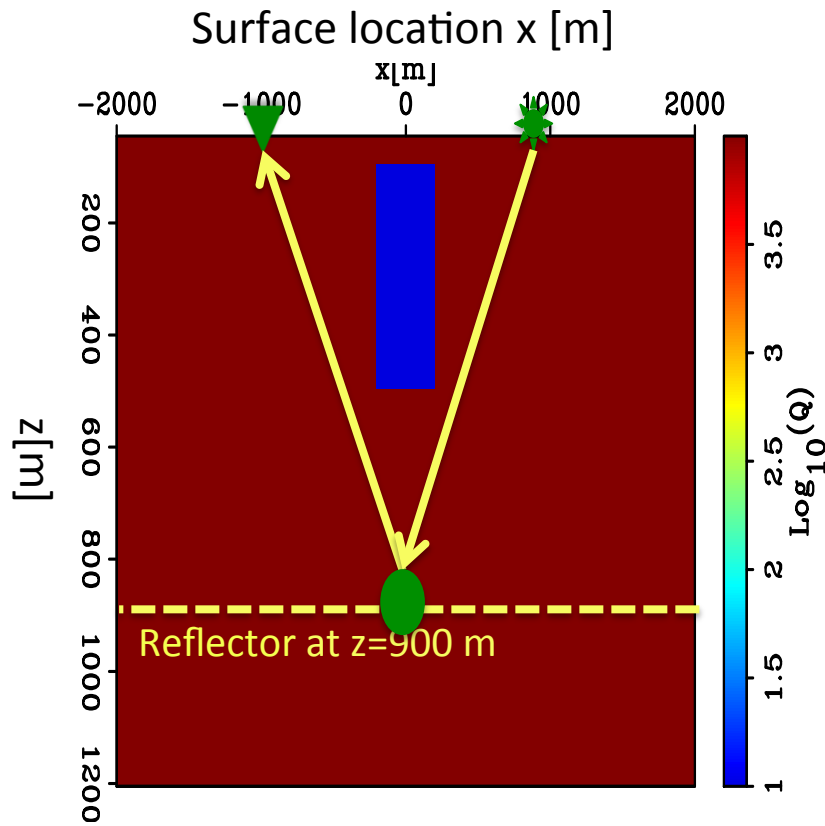
Prestack method: Angle domain common image gather (ADCIG)

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



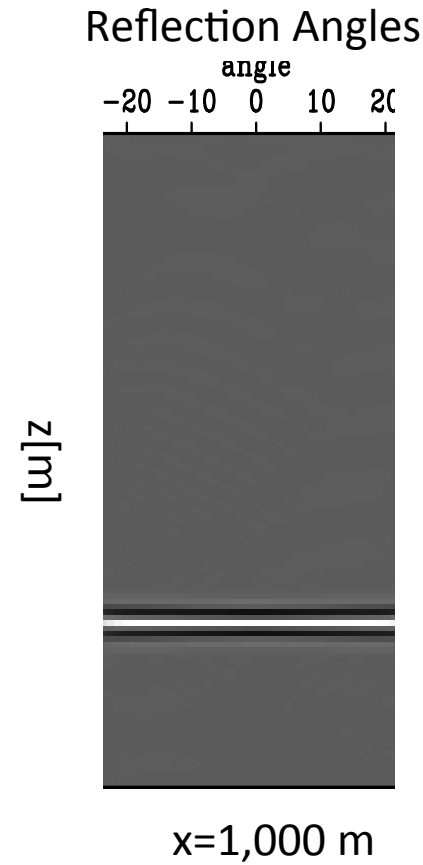
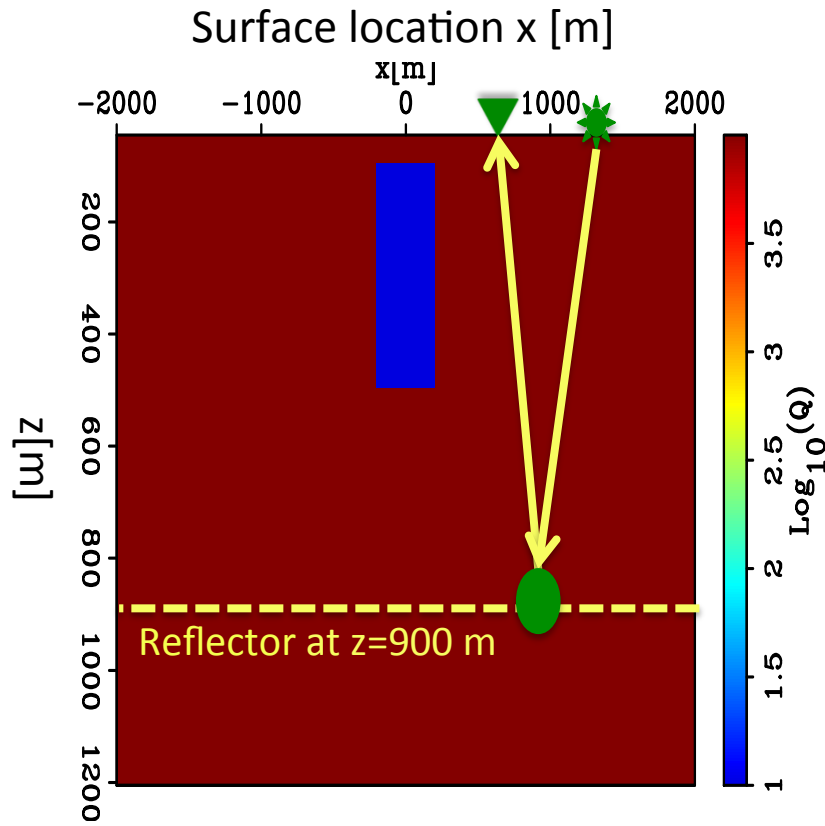
Prestack method: Angle domain common image gather (ADCIG)

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



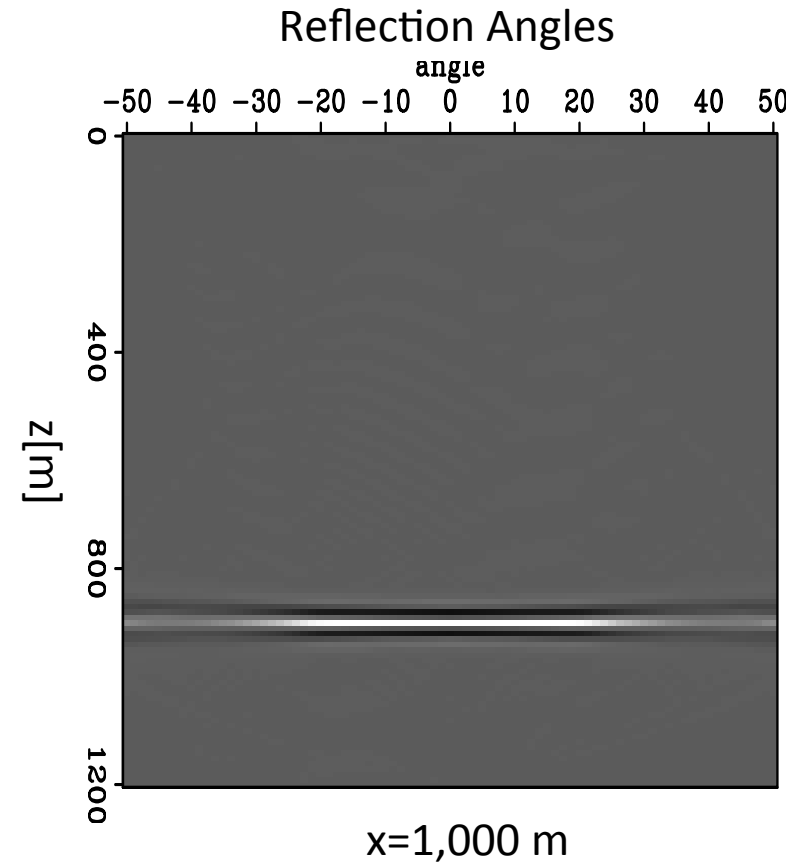
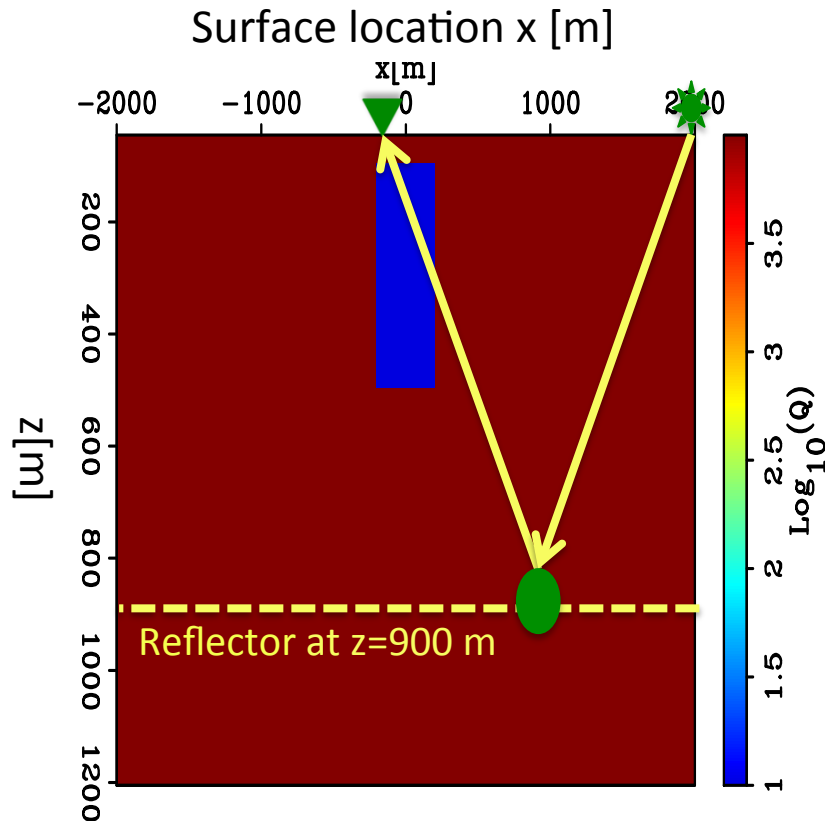
Prestack method: Angle domain common image gather (ADCIG)

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



Prestack method: Angle domain common image gather (ADCIG)

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



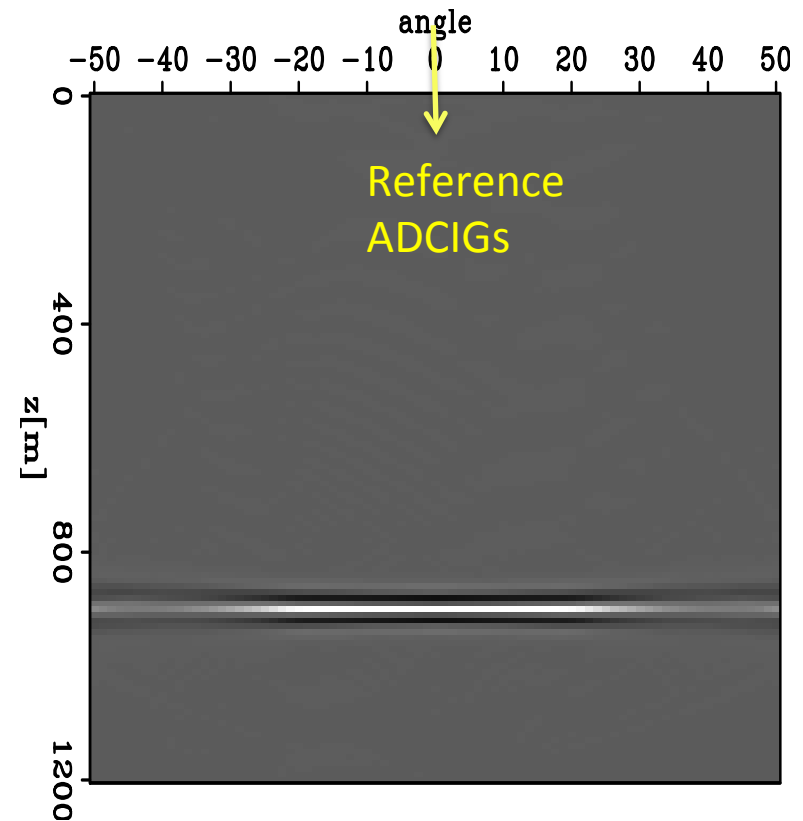
Prestack method: Angle domain common image gather (ADCIG)

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

- Select near angles as the reference angles for each ADCIG
- Or select the reference ADCIGs
- Compare the windowed spectra for ρ : reference spectra and target spectra

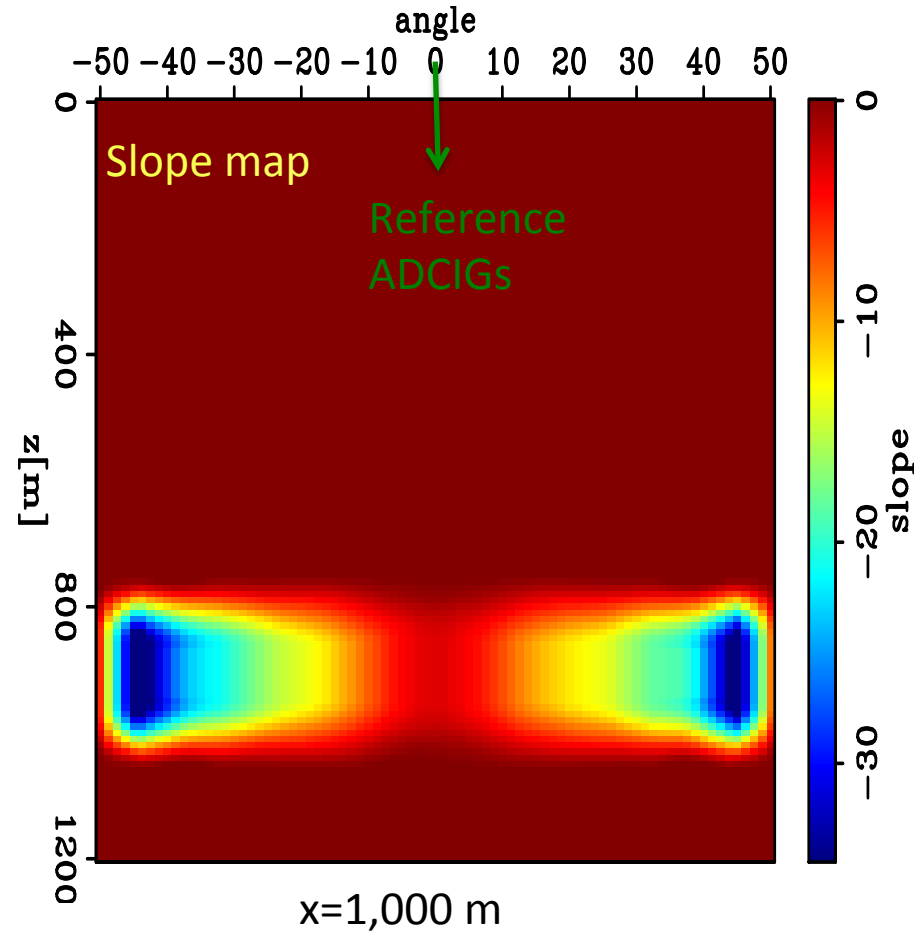
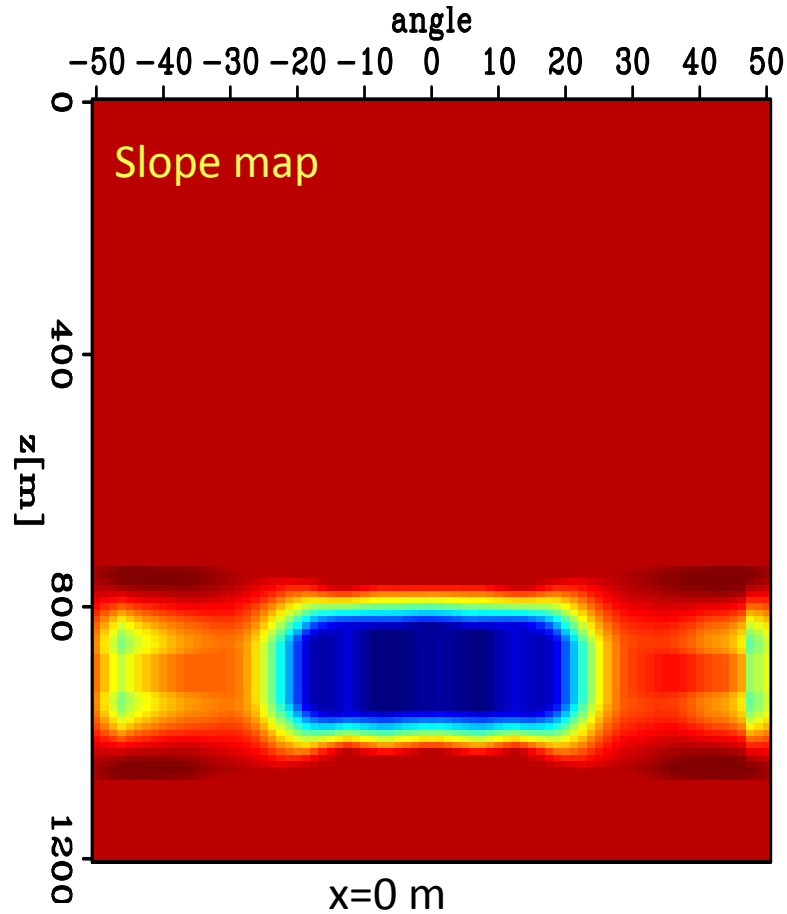
$$\ln\left(\frac{R_1(\mathbf{k}')}{R_2(\mathbf{k}')}\right) = \rho|\mathbf{k}'| + G_0$$

- The windows are compared at the same depth



Prestack method: Angle domain common image gather (ADCIG)

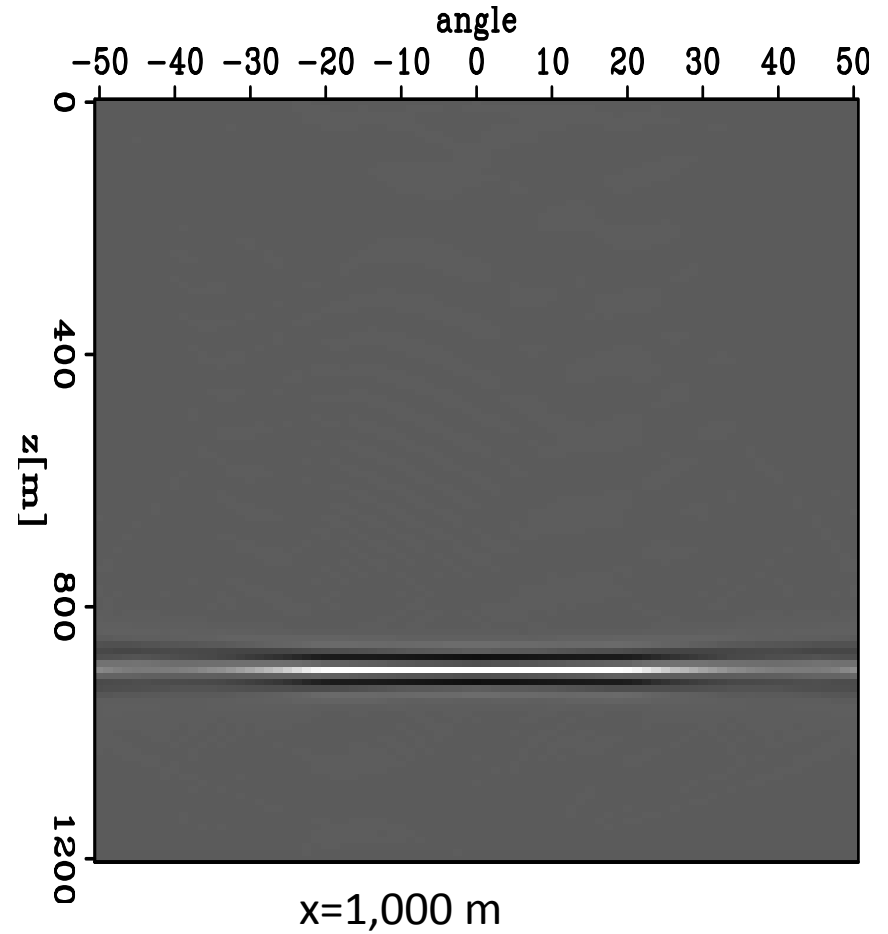
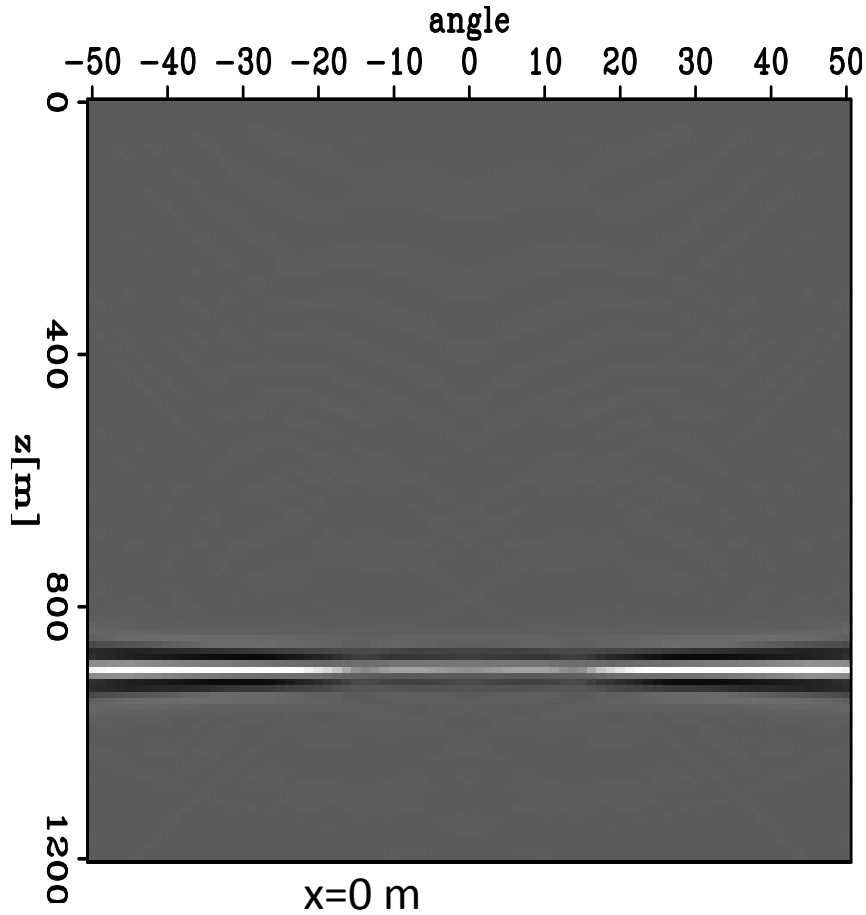
Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



Red: non-attenuated regions
Blue: attenuated regions

Prestack method: Angle domain common image gather (ADCIG)

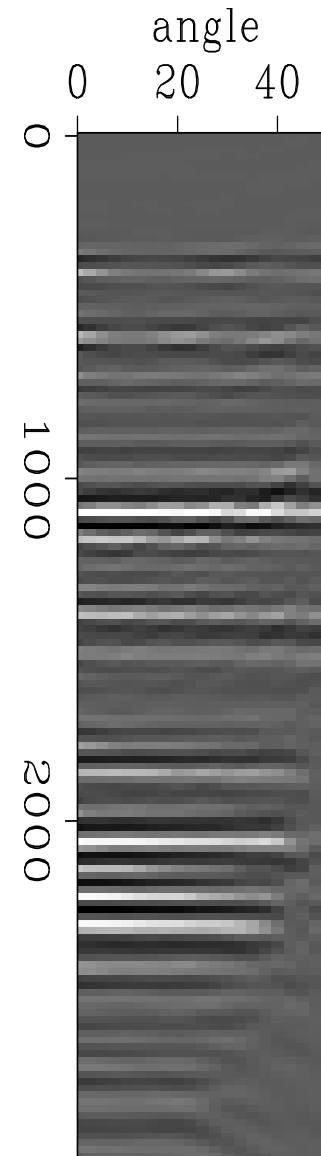
Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



Prestack method

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

- **Prestack method using narrower windows in depth, If the velocity model is correct**
 - Improve results resolutions



Q gradients

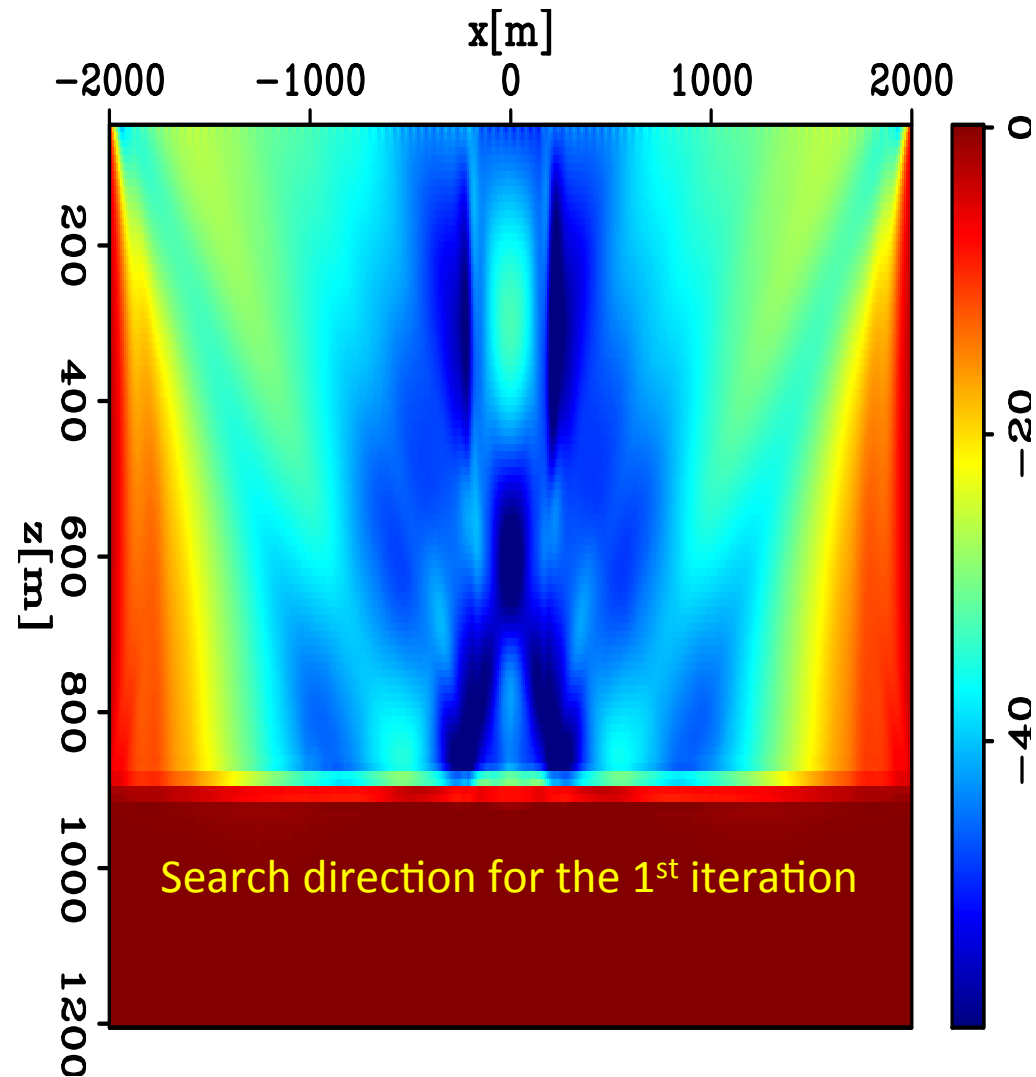
Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

- Gradients of the objective function with respect to Q

$$\left(\frac{\partial J}{\partial Q}\right)^* = \sum_{\mathbf{x}} \left(\frac{\partial \rho}{\partial Q}\right)^* \rho$$

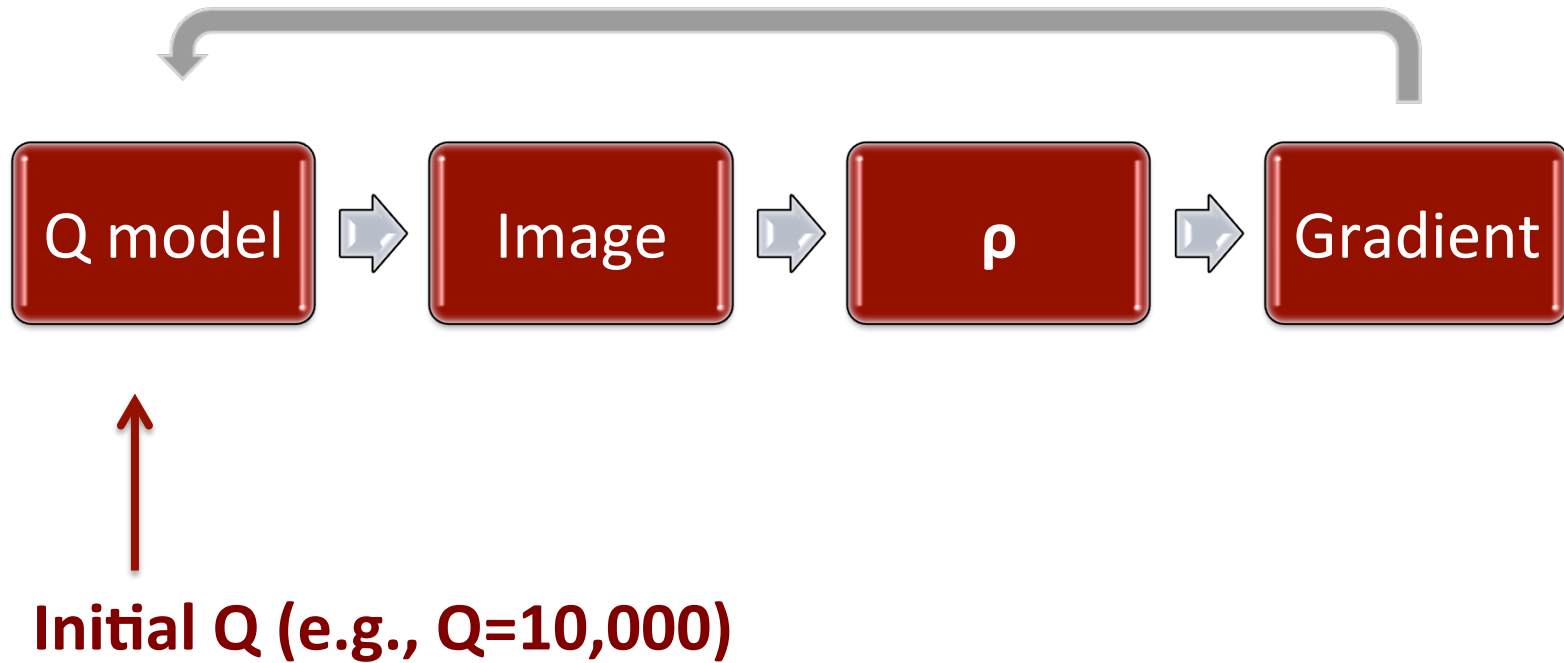
- Search direction for the 1st iteration

$$-\left(\frac{\partial J}{\partial Q}\right)^*$$



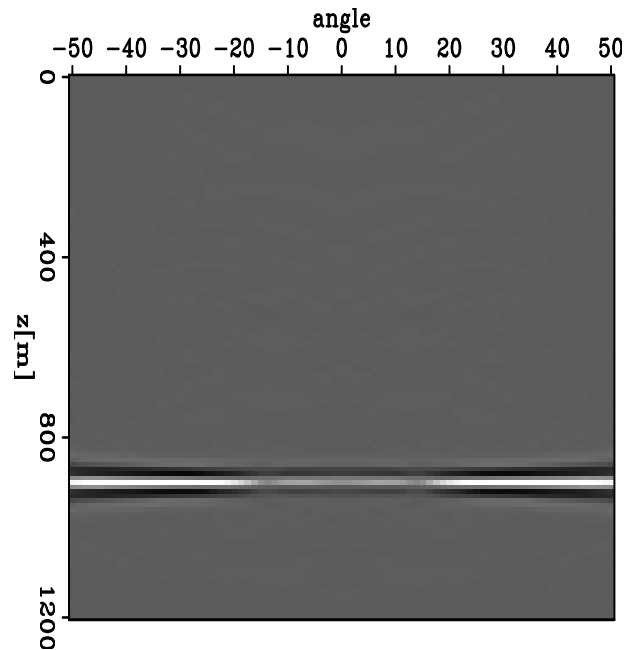
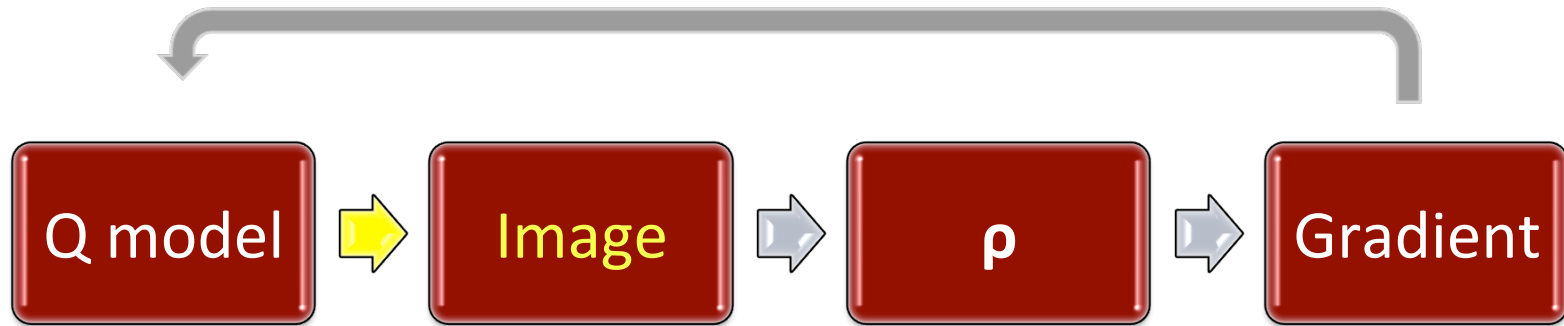
WEMQA workflow

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



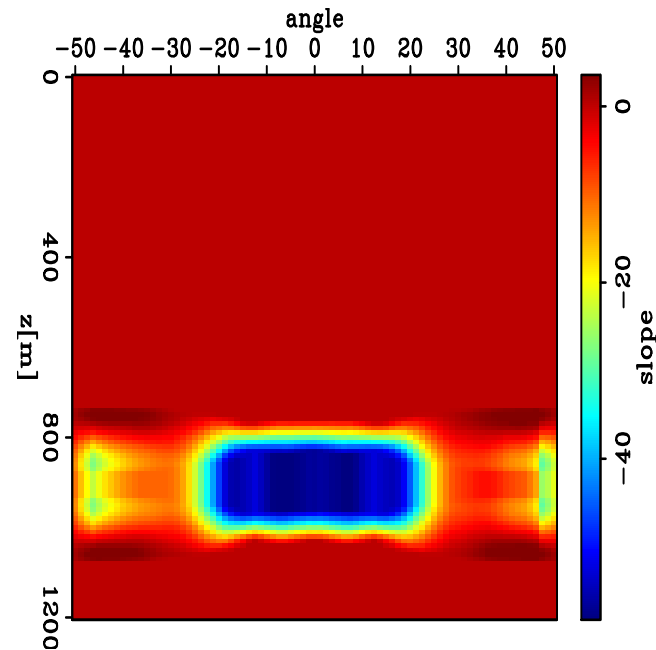
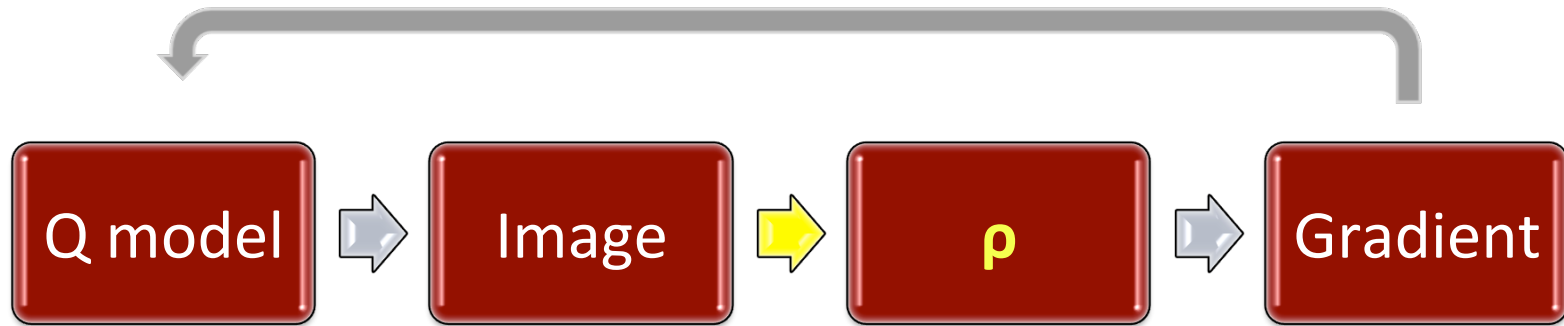
WEMQA workflow

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



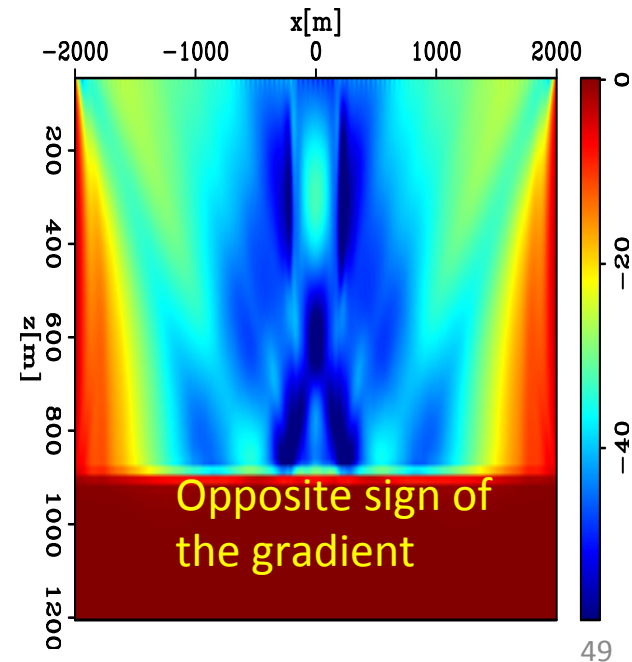
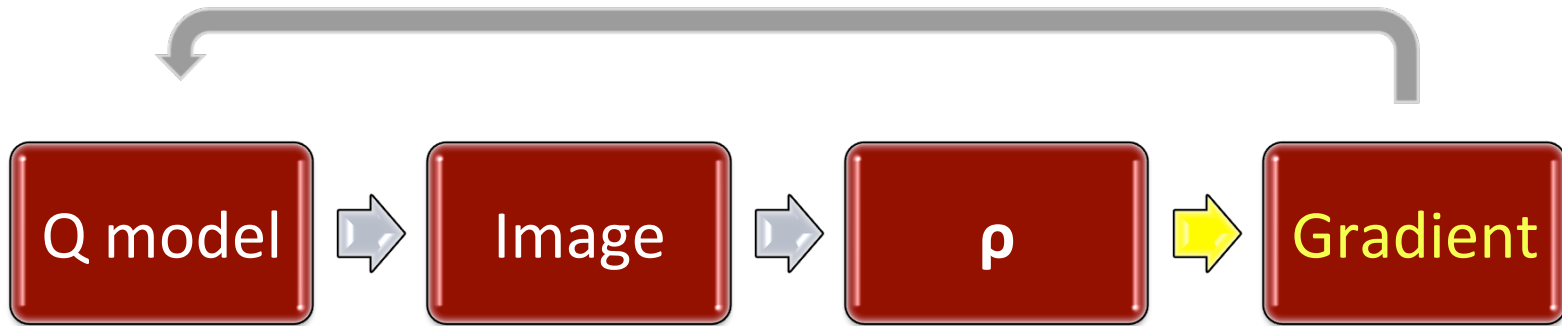
WEMQA workflow

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



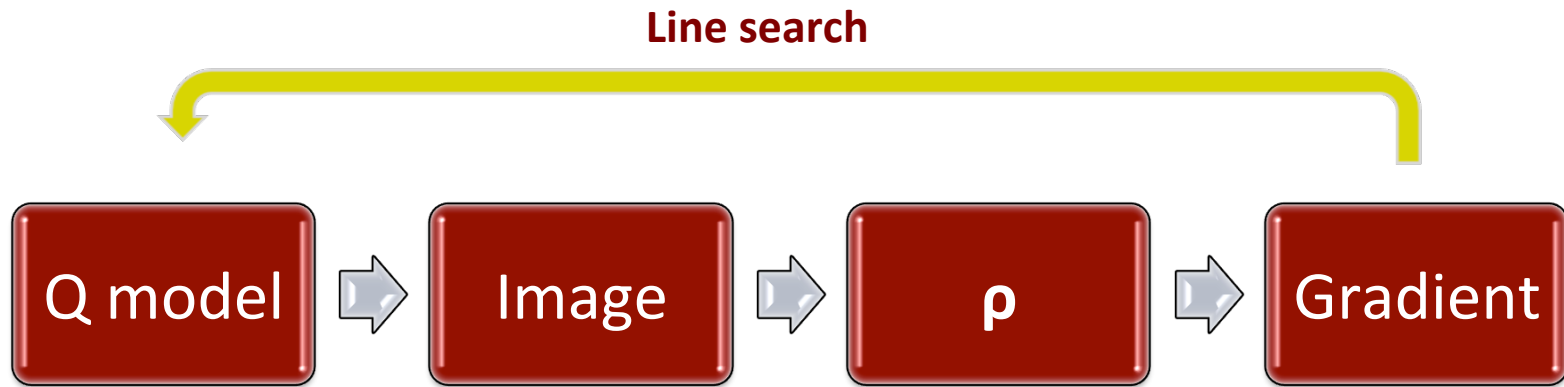
WEMQA workflow

Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow

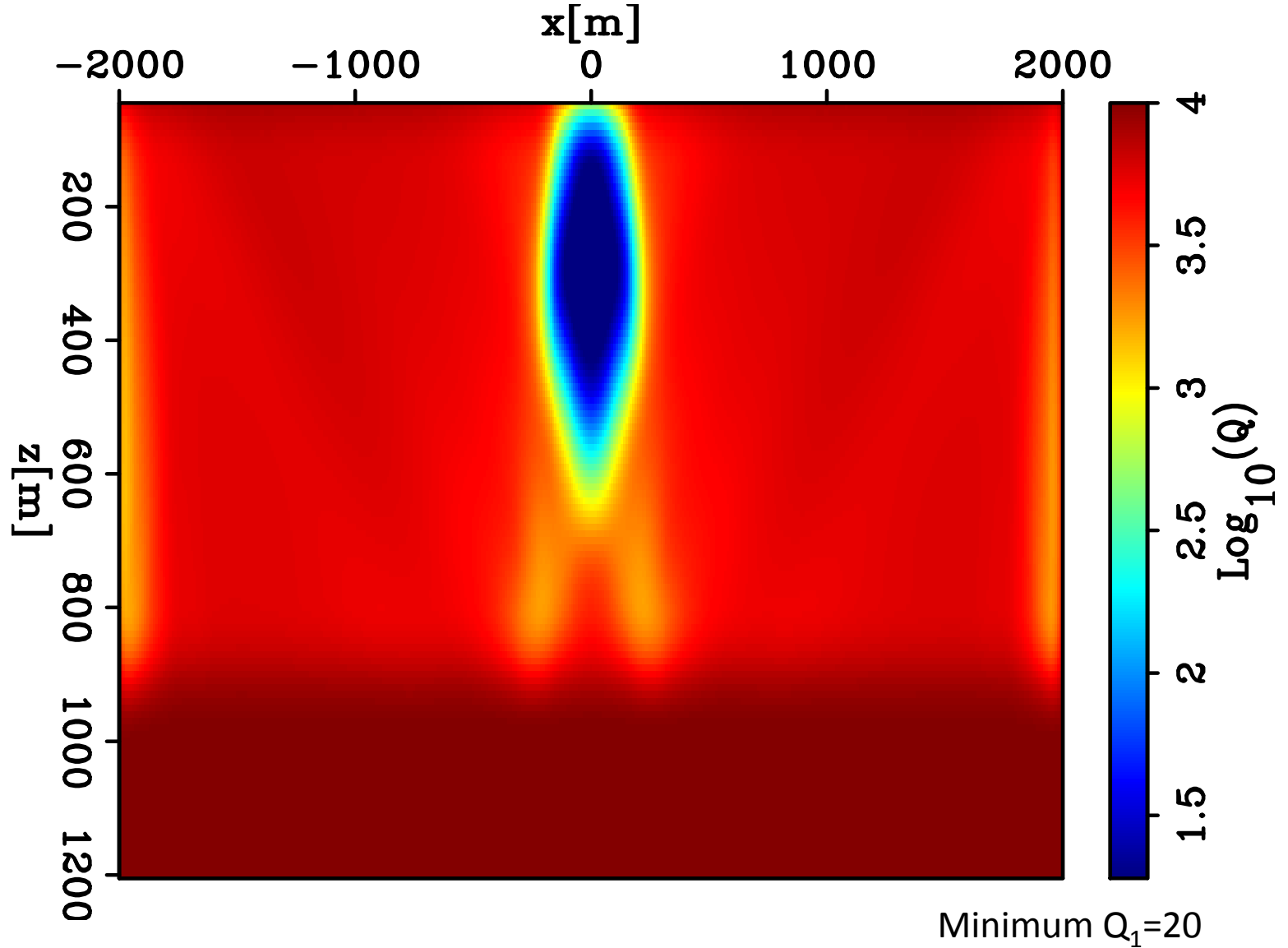


WEMQA workflow

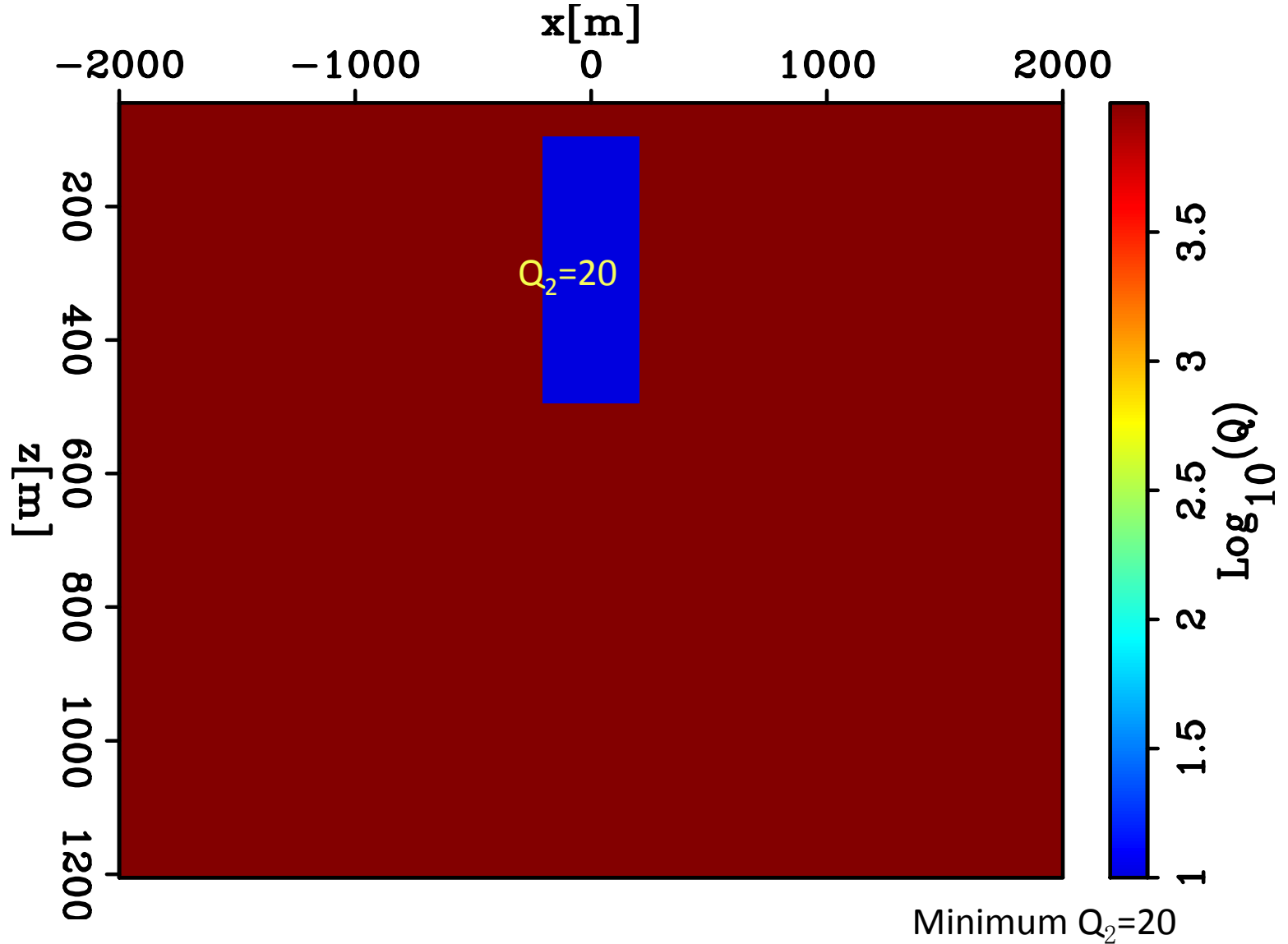
Defining ρ in the migrated image space
Computing ρ from a migrated image
Wave-equation based Q tomography
Inversion workflow



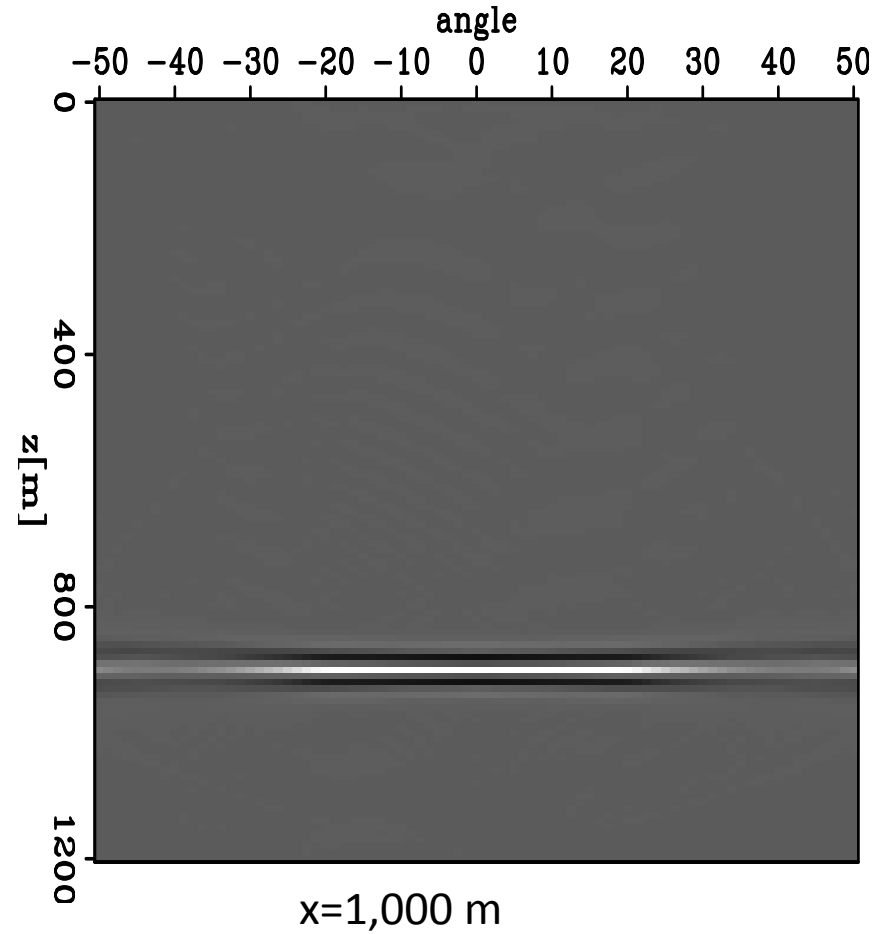
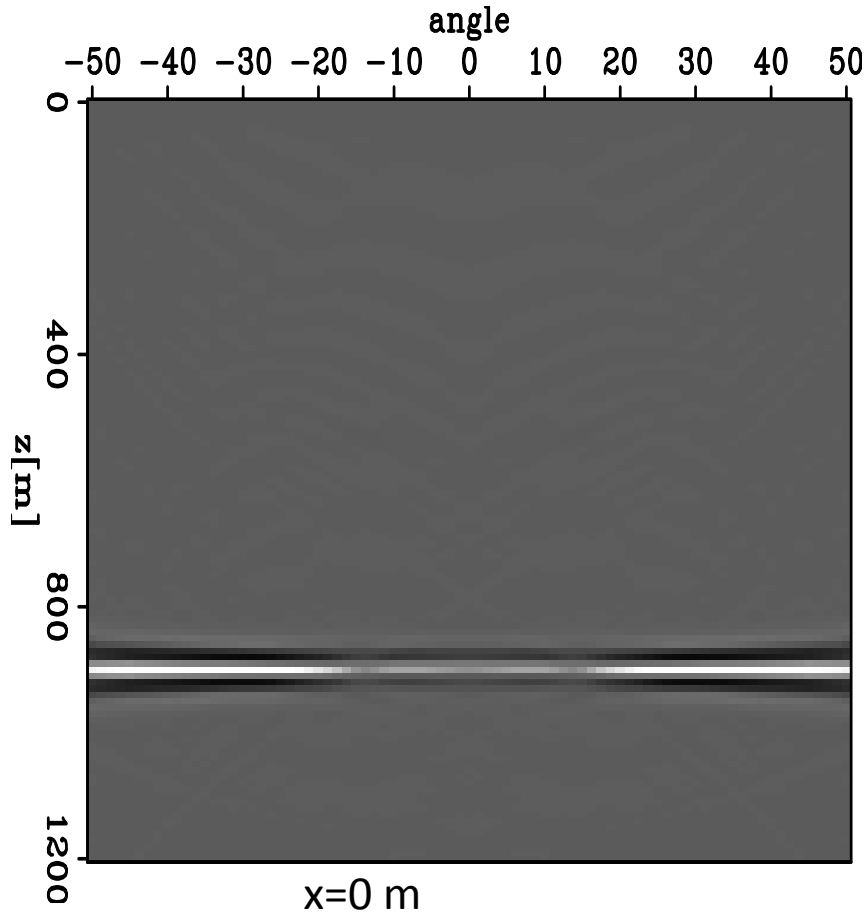
Inverted Q model using prestack method



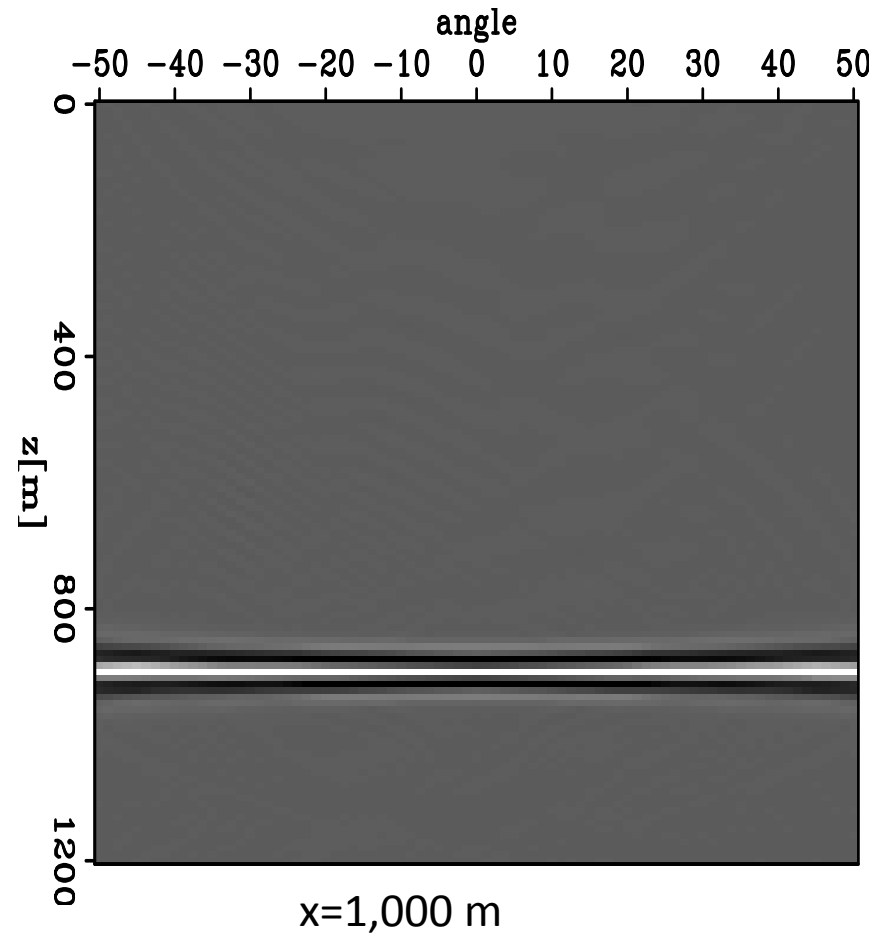
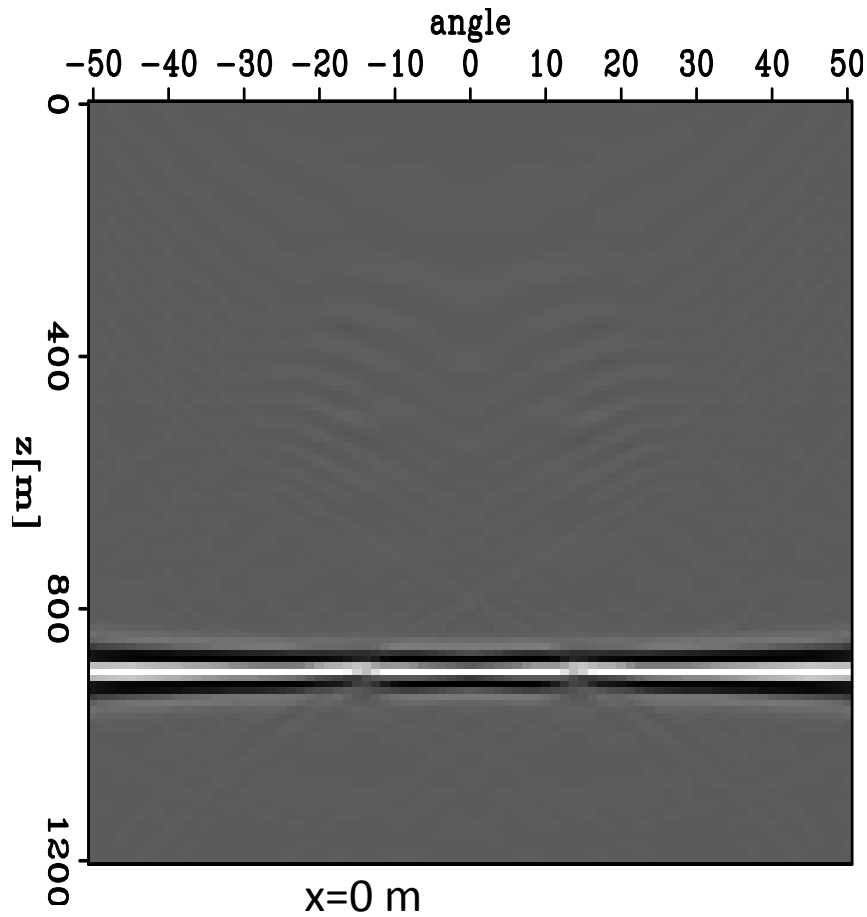
True Q model



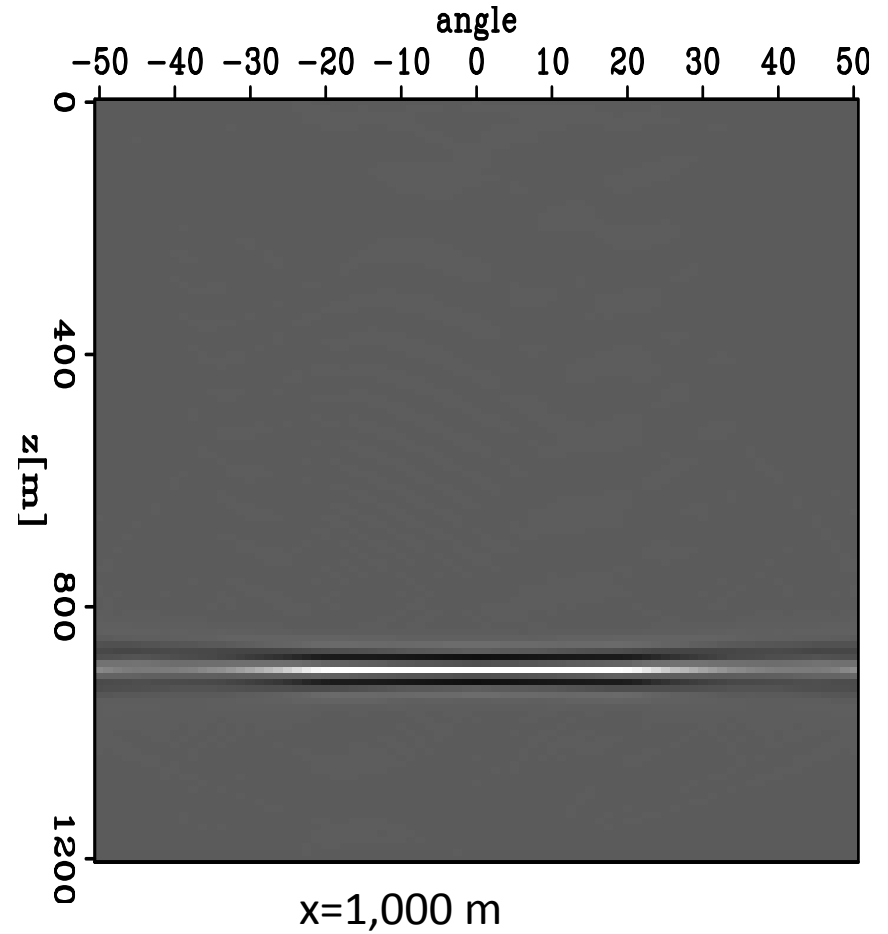
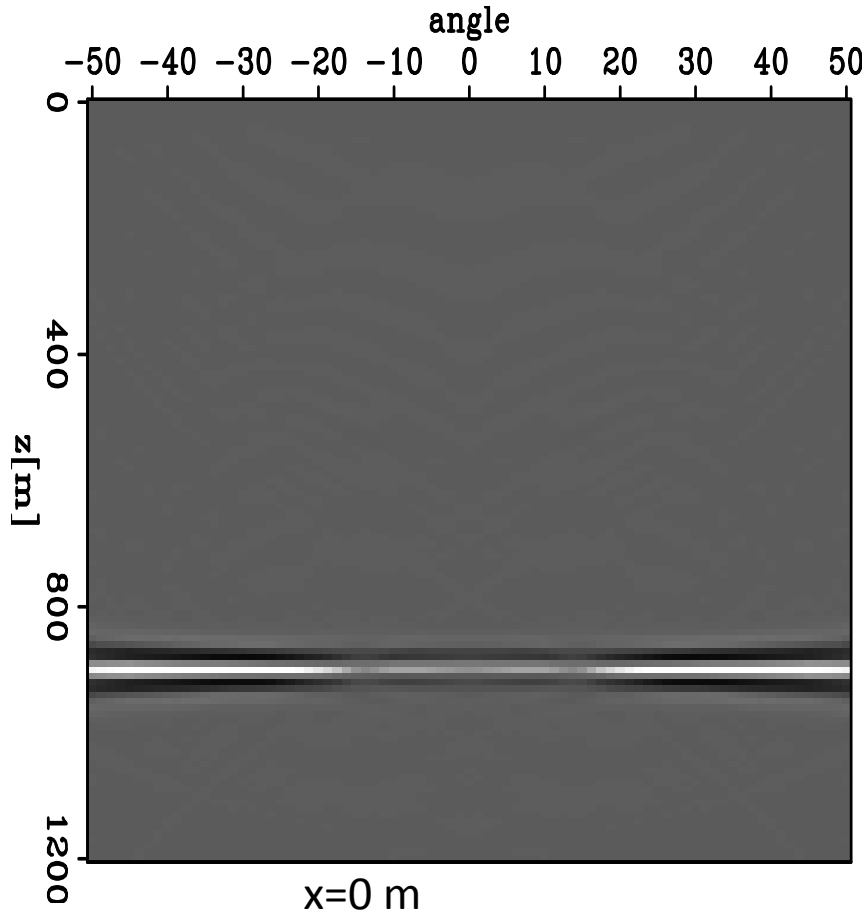
ADCIG before Q compensation



ADCIG after Q compensation



ADCIG before Q compensation



Field data application: streamer data

Shot spacing: 50m inline; 300m xline
Receiver spacing: 25m inline; 75m xline

Crossline

Inline
(Sailing direction)

Source Point – (S_x, S_y)

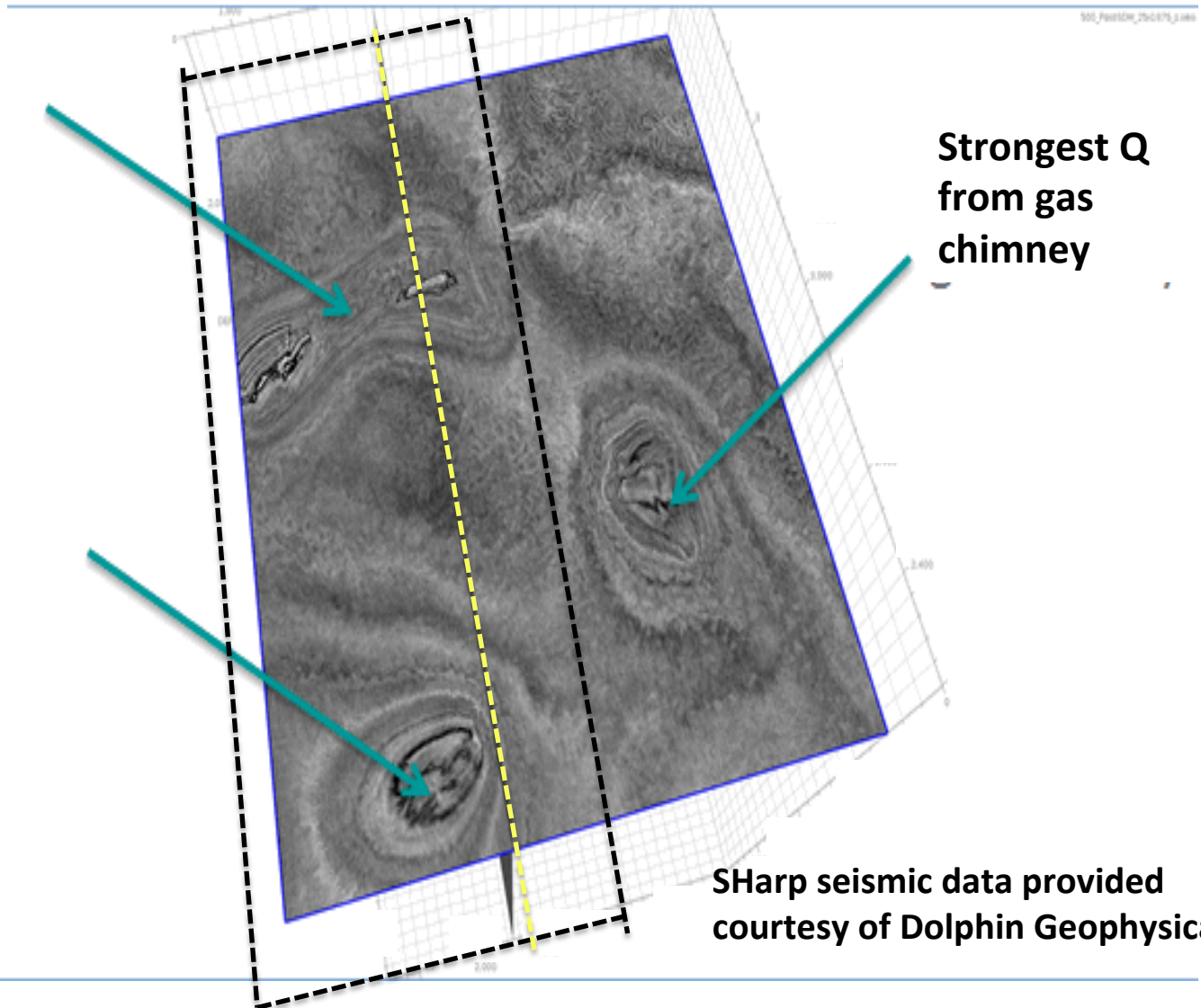
Polarcus vessel (<http://subseaworldnews.com/wp-content/uploads/2016/03/Polarcus-Snaps-Up-Dolphins-Streamer-Package.jpeg>)

Depth slice that highlights anomalies

Channel with
strong velocity
drop

Strong Q
from gas
chimney

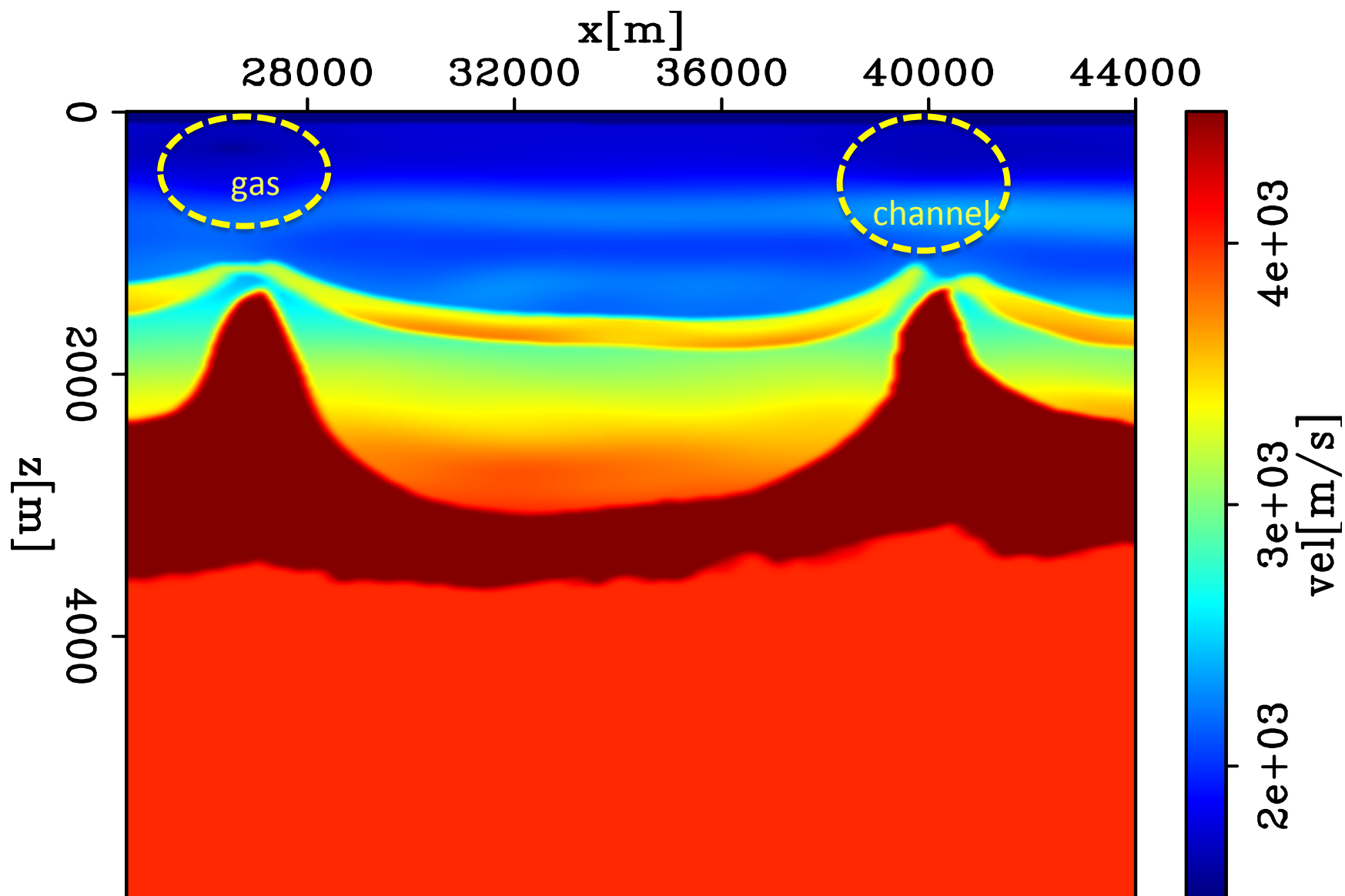
Strongest Q
from gas
chimney



SHarp seismic data provided
courtesy of Dolphin Geophysical

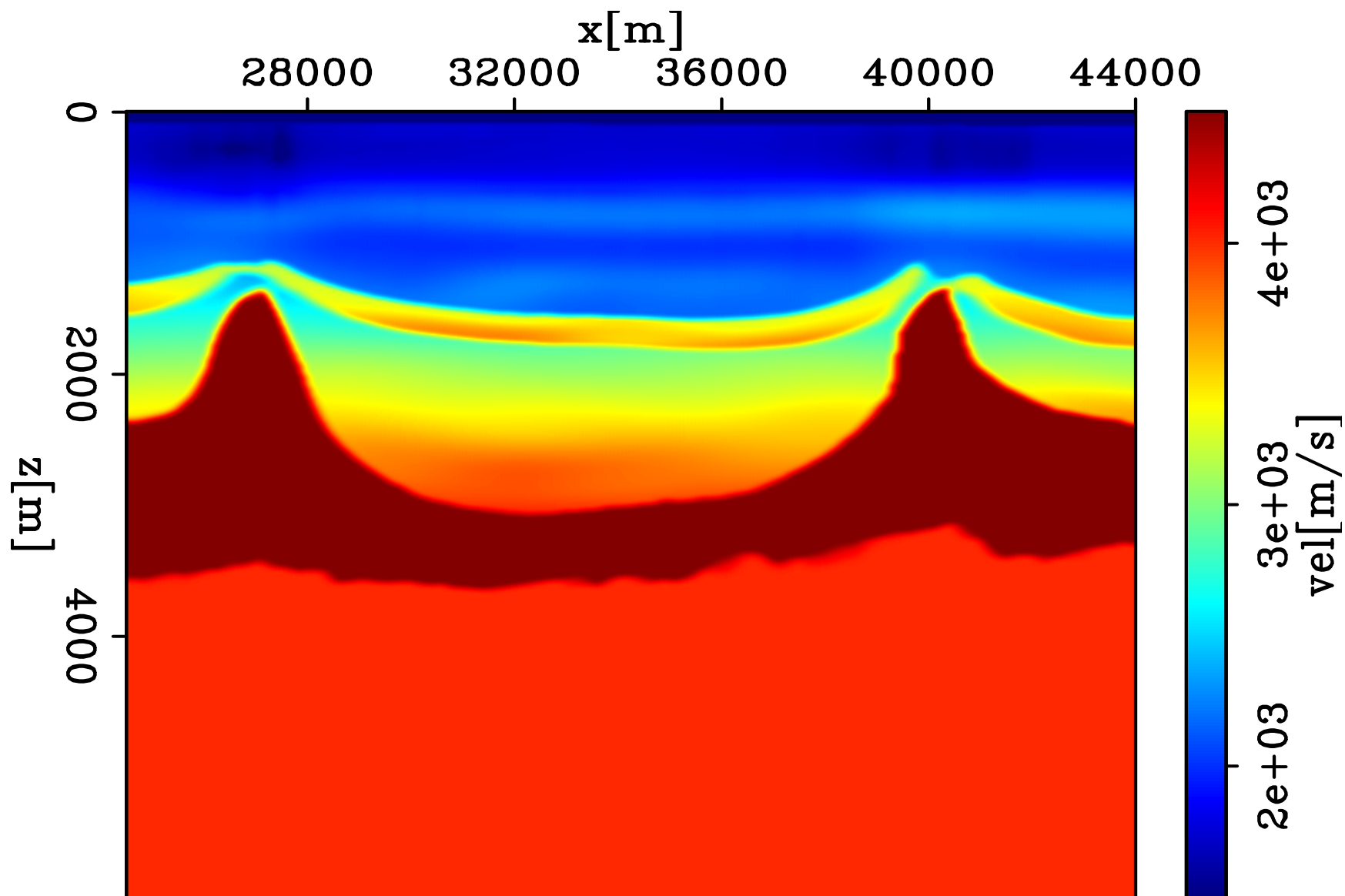
2D initial velocity

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



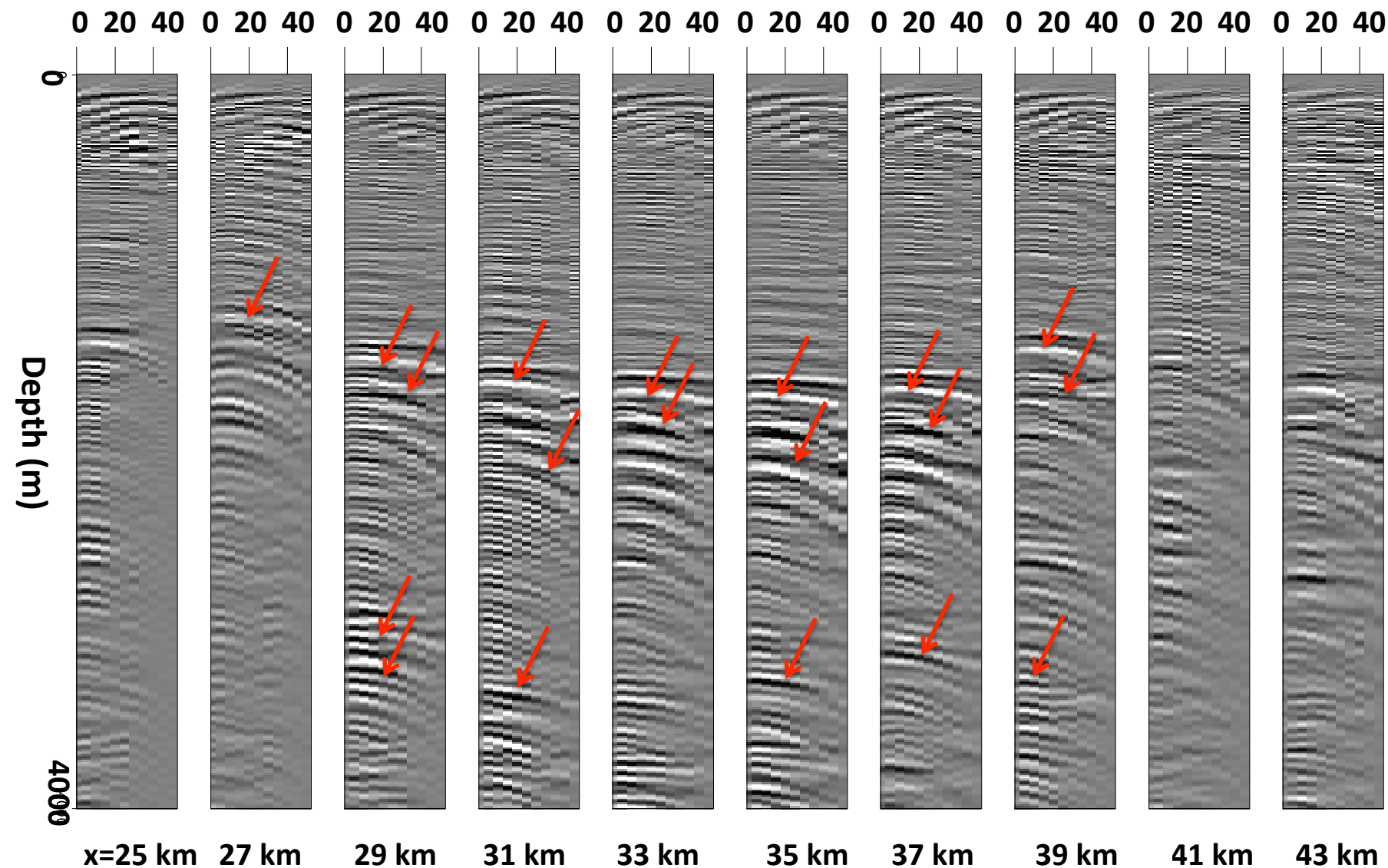
2D updated velocity

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



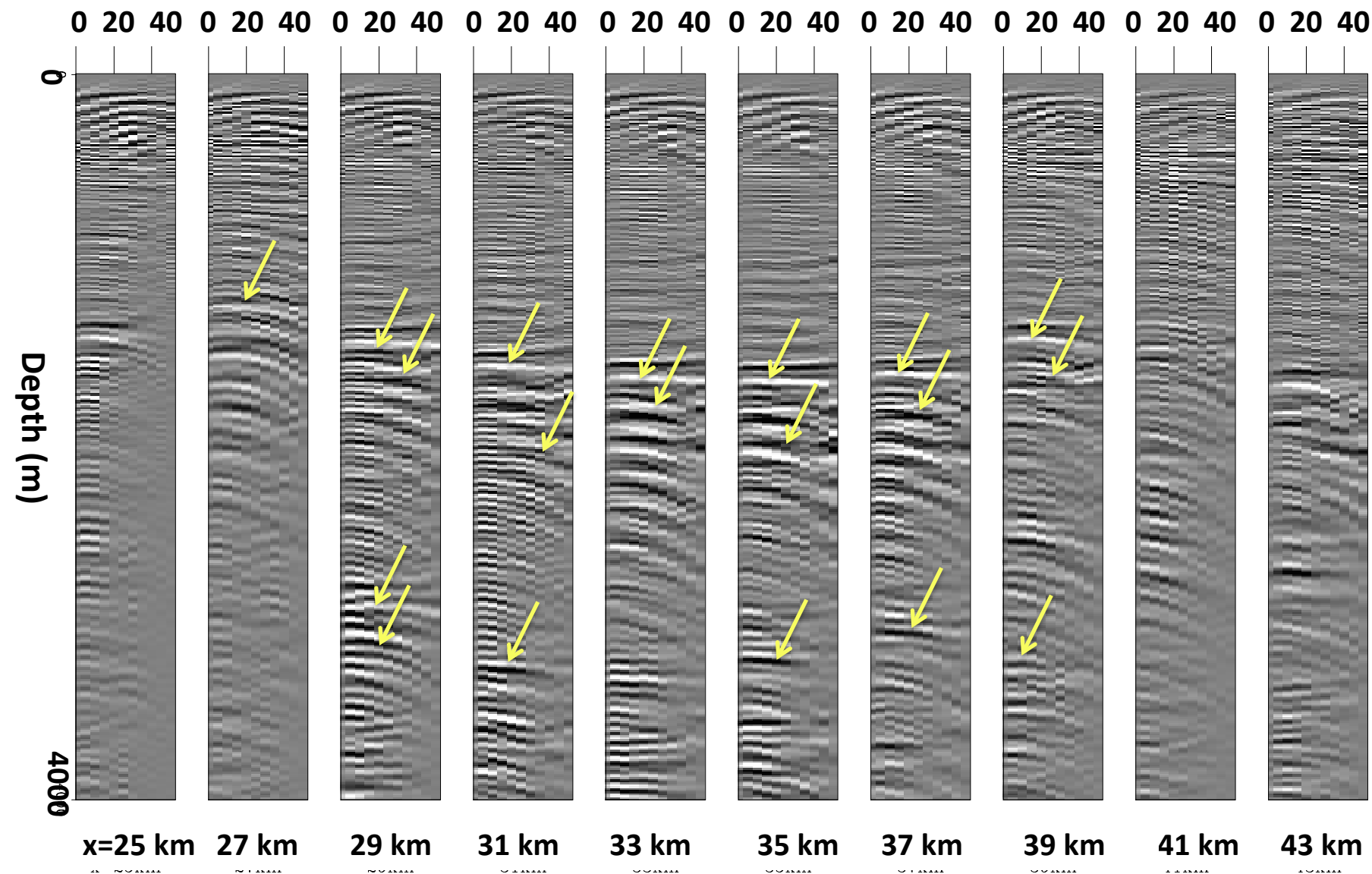
ADCIGs **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



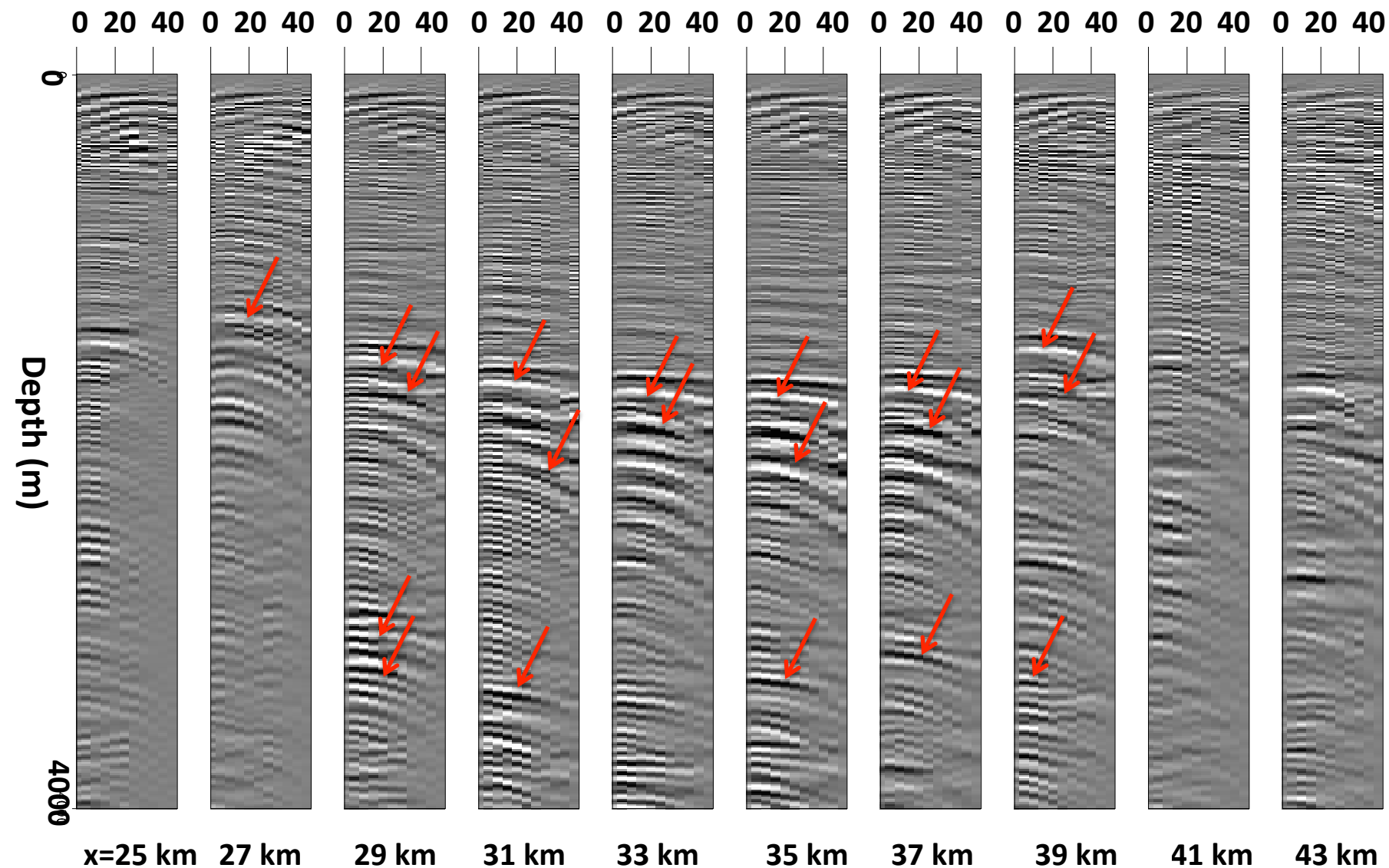
ADCIGs **after** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



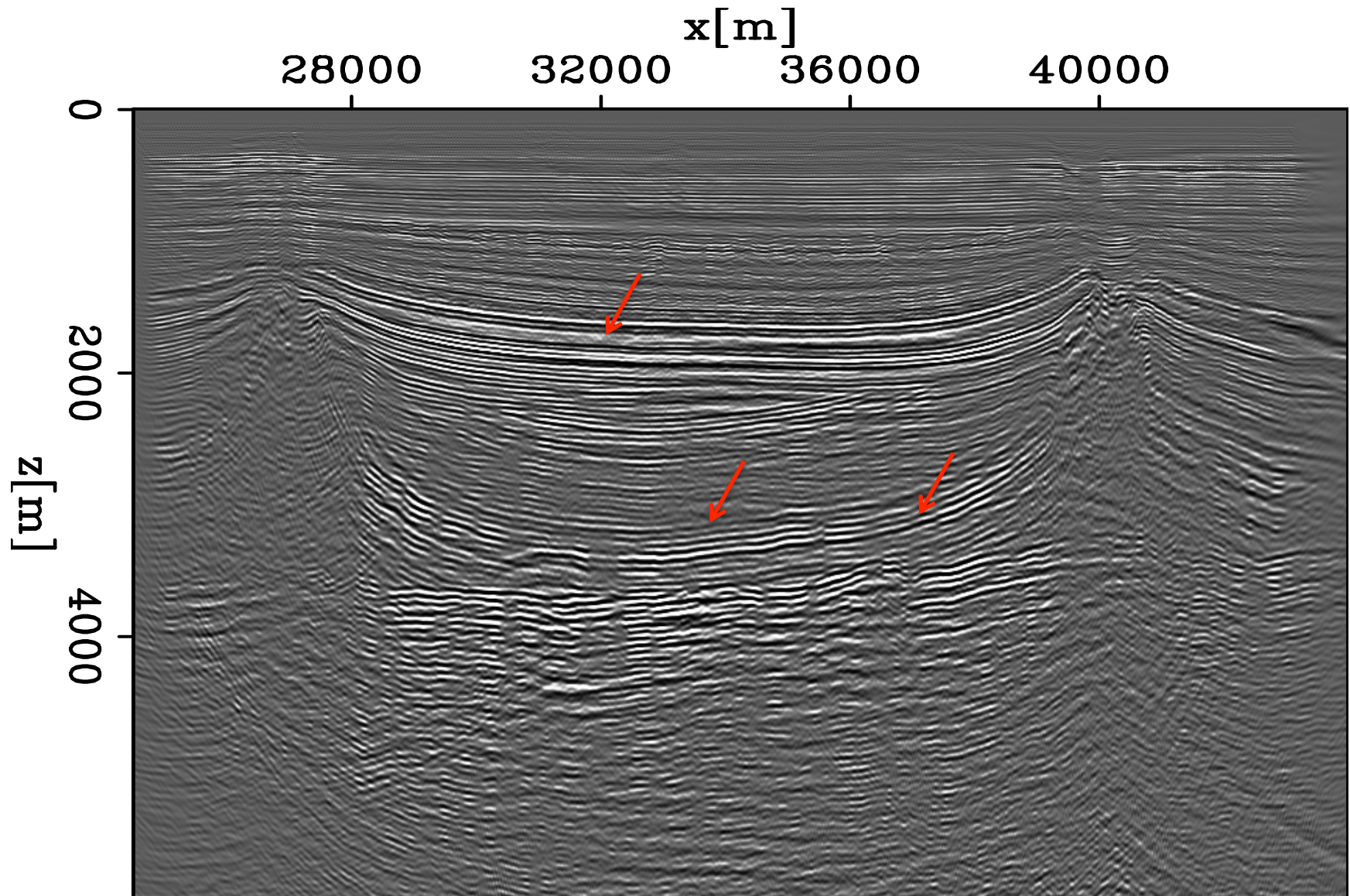
ADCIGs **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



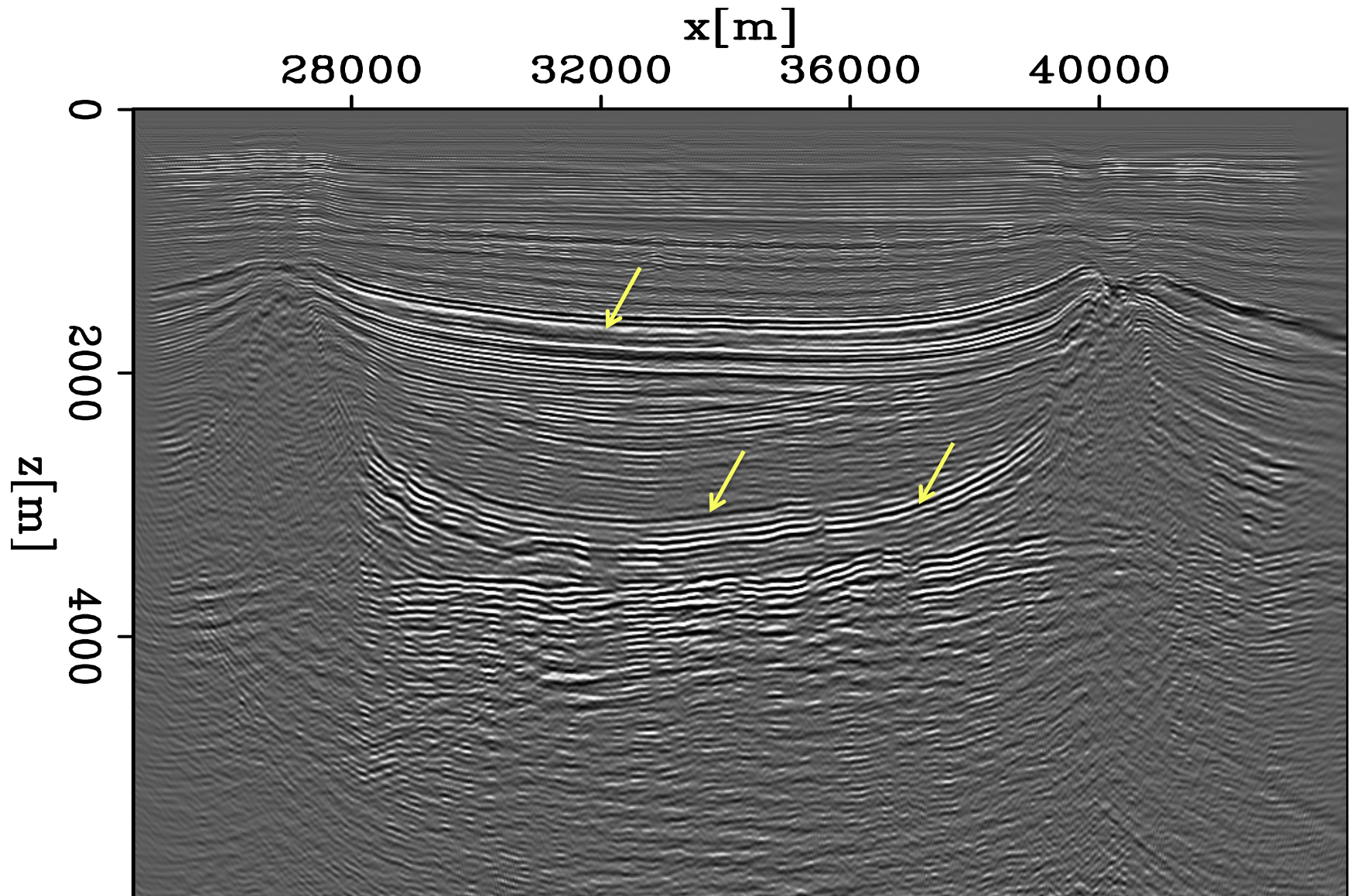
2D image **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



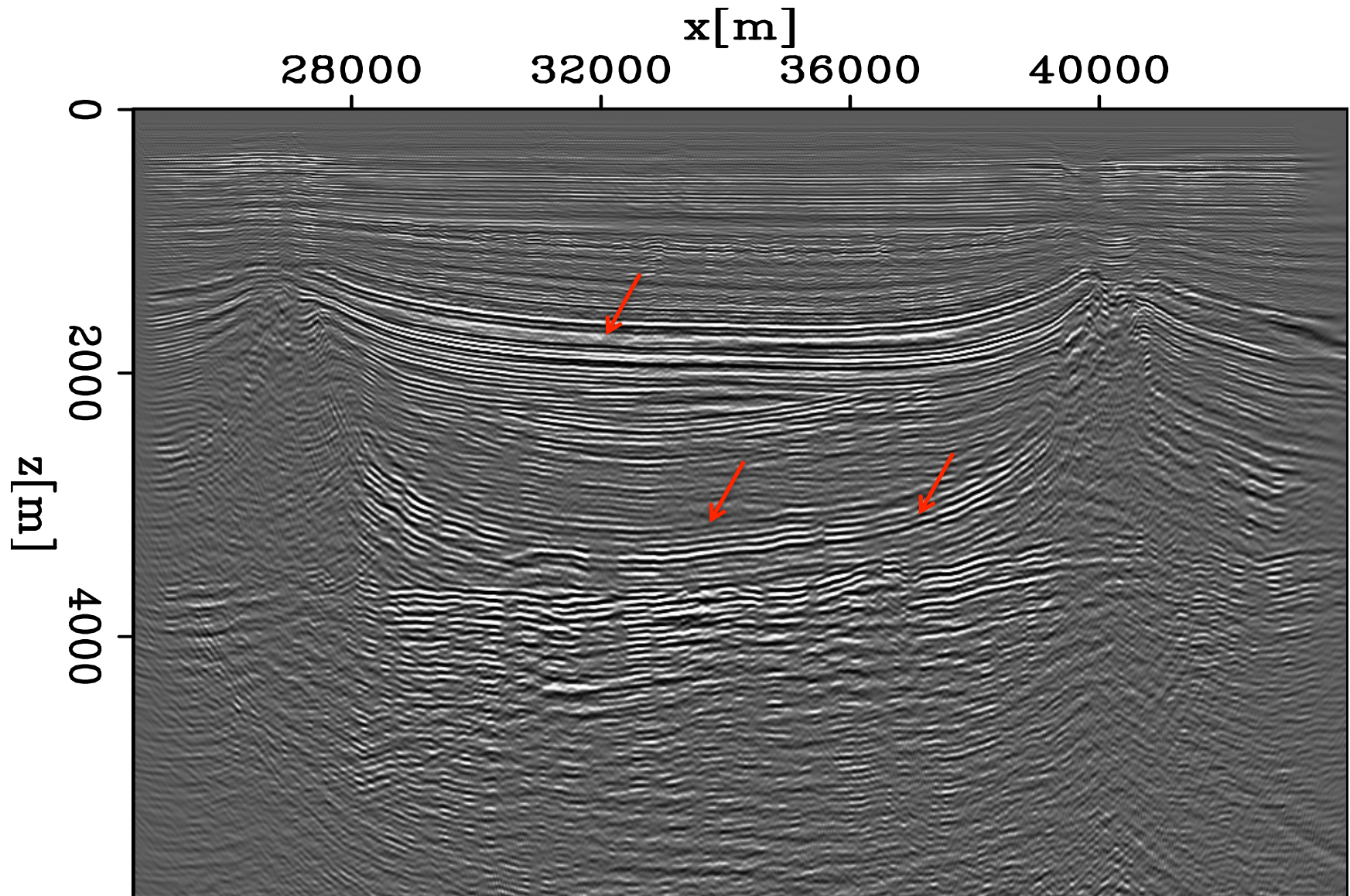
2D image **after** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



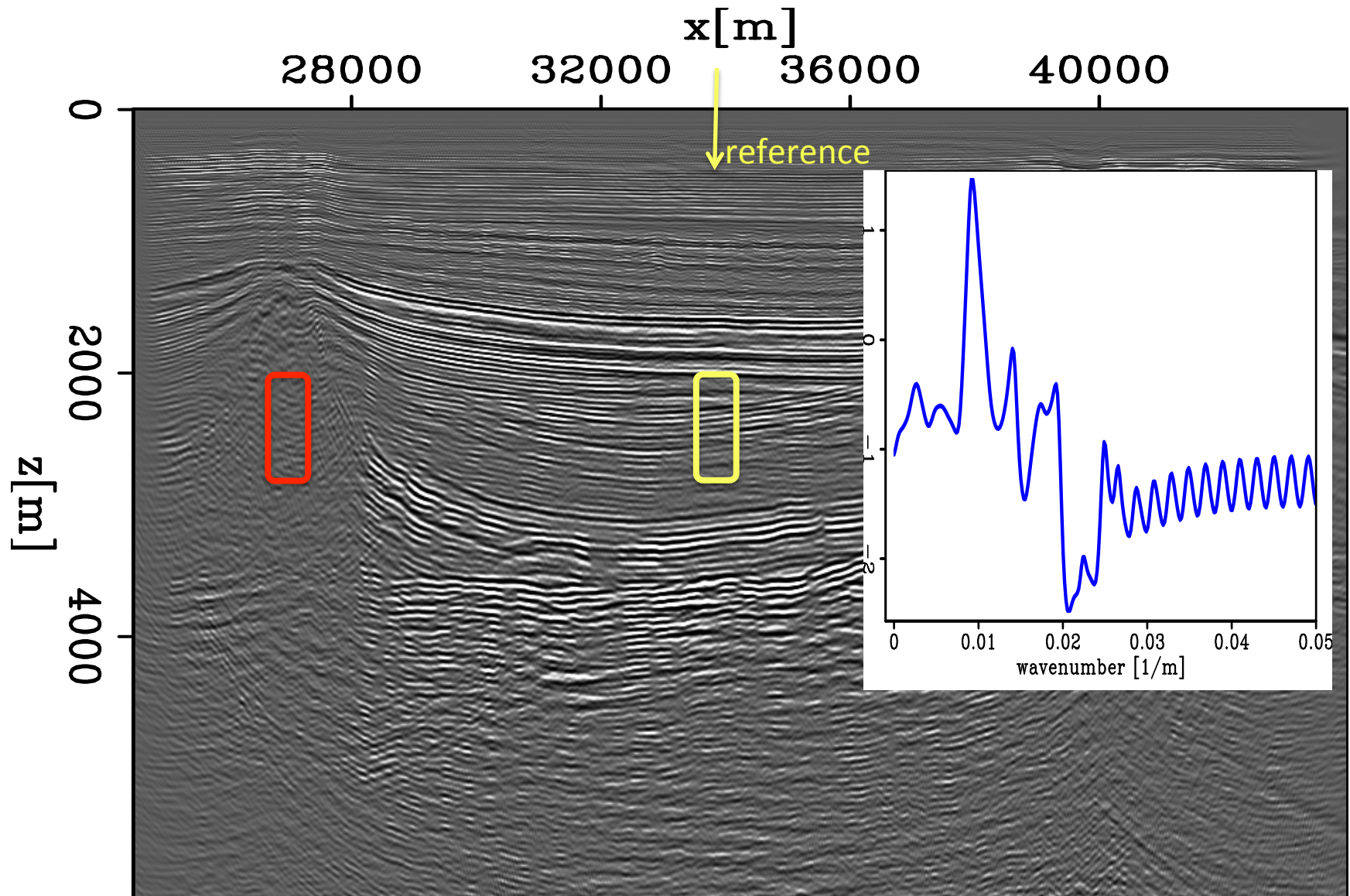
2D image **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



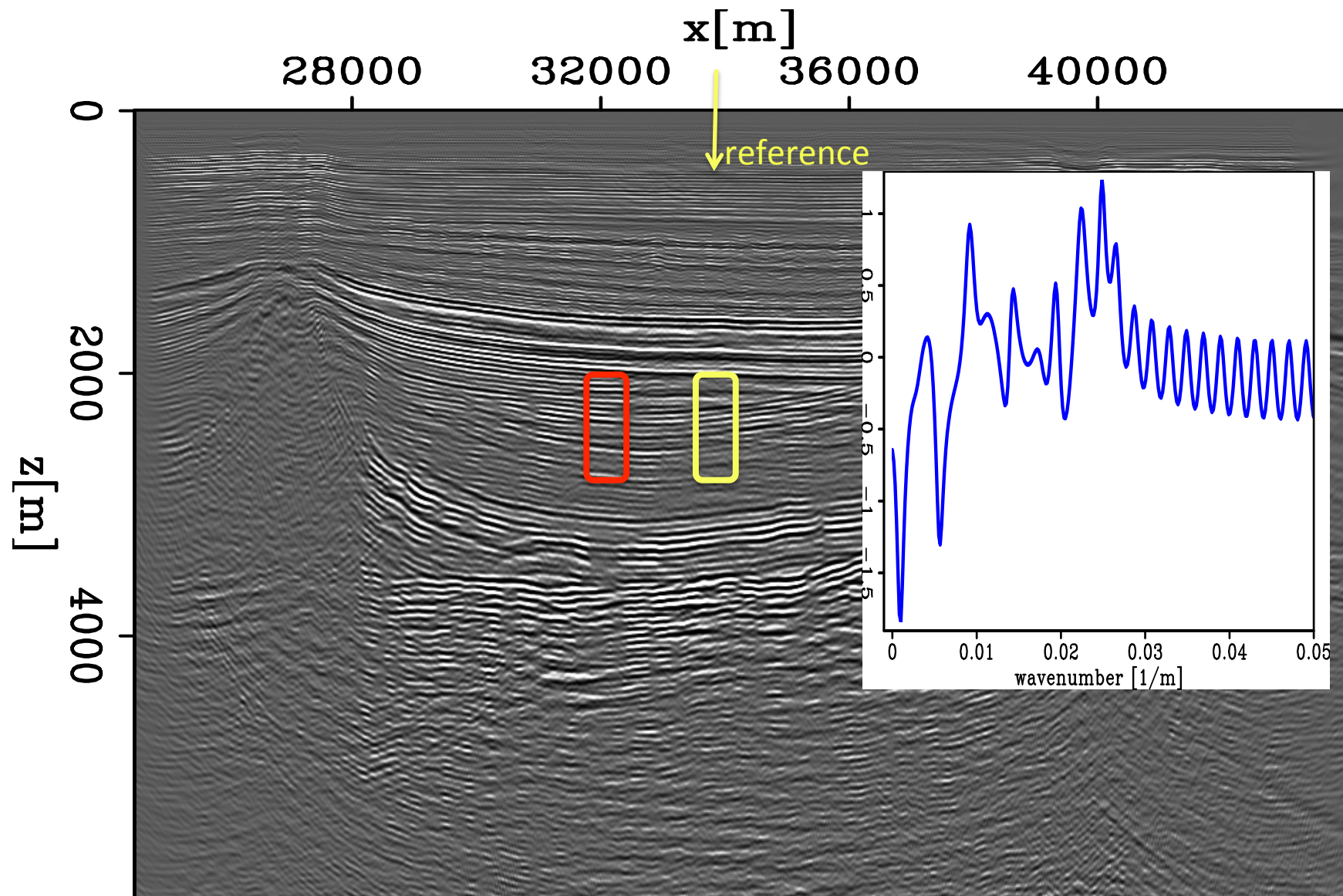
2D image **before** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



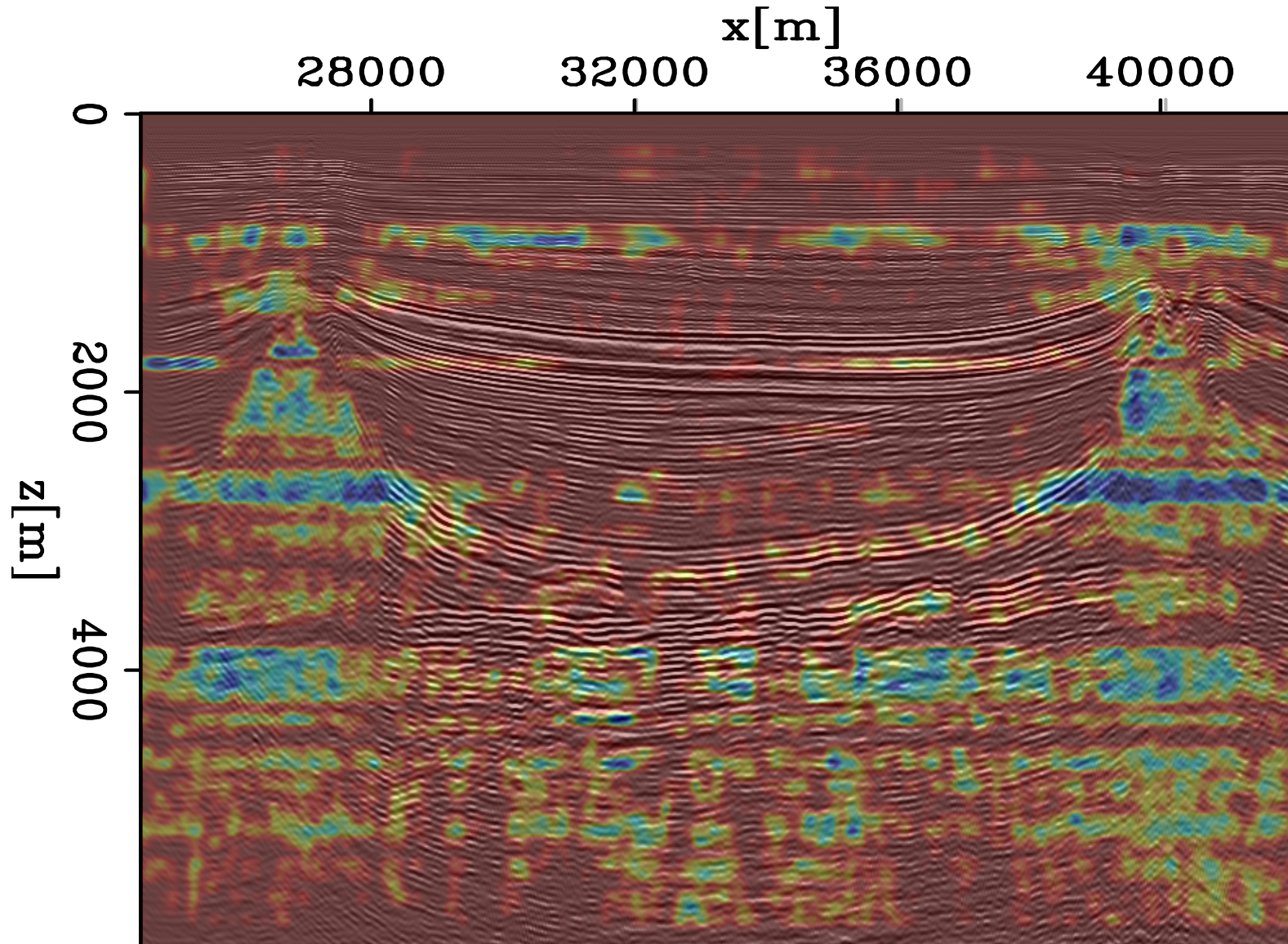
2D image **before** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



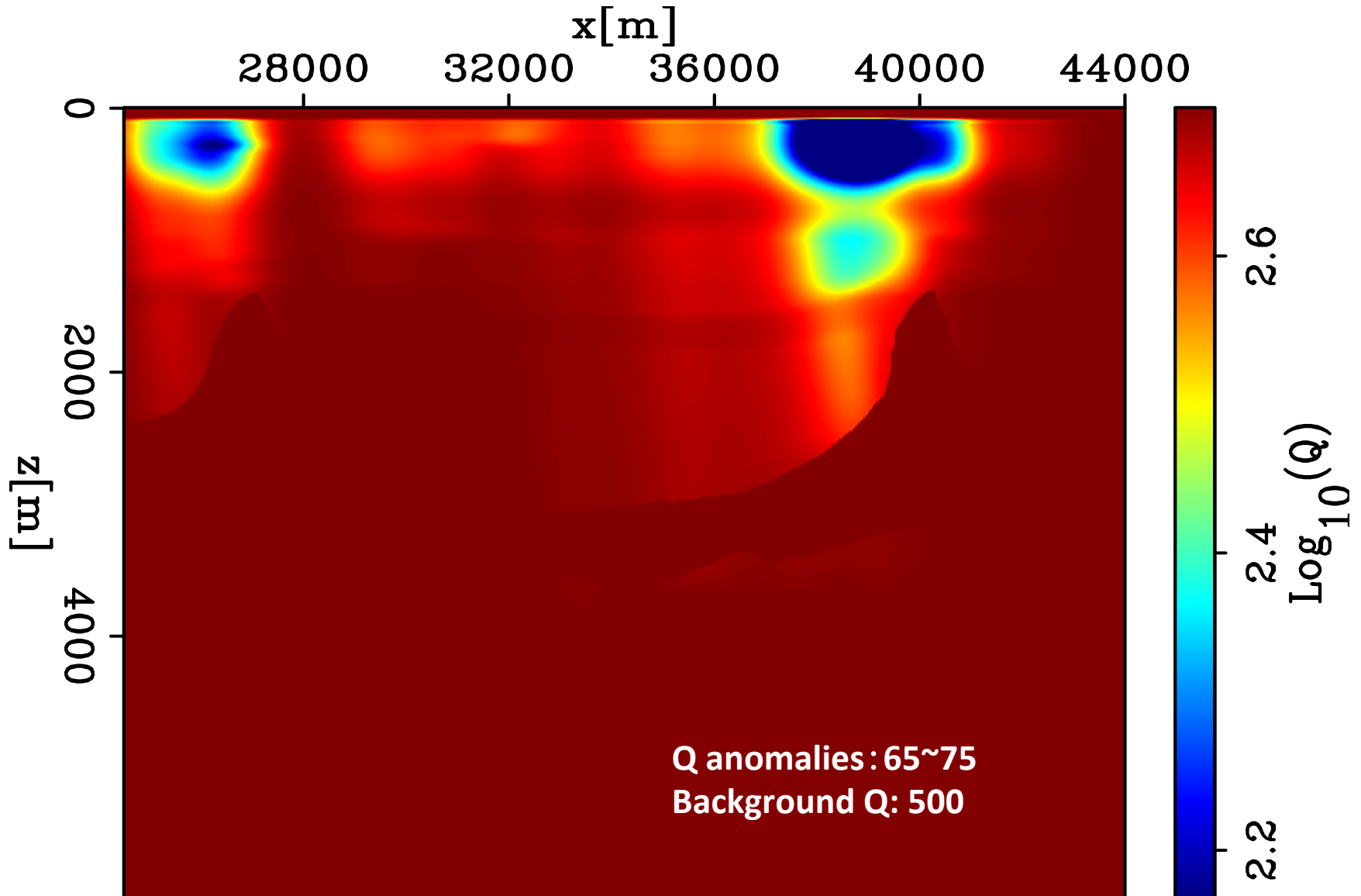
Slope of the stacked image

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



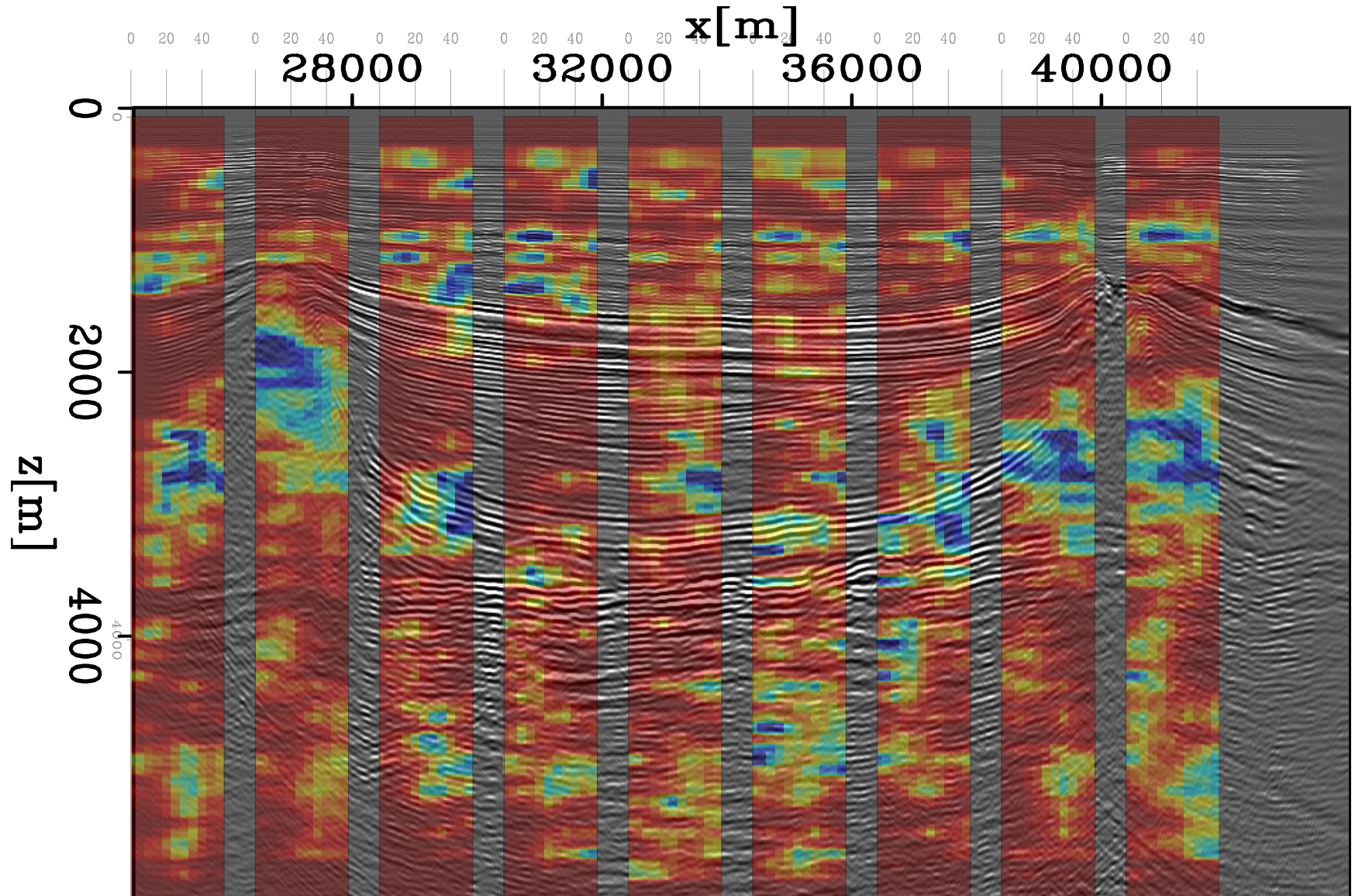
Inverted Q using **stacked** WEMQA

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



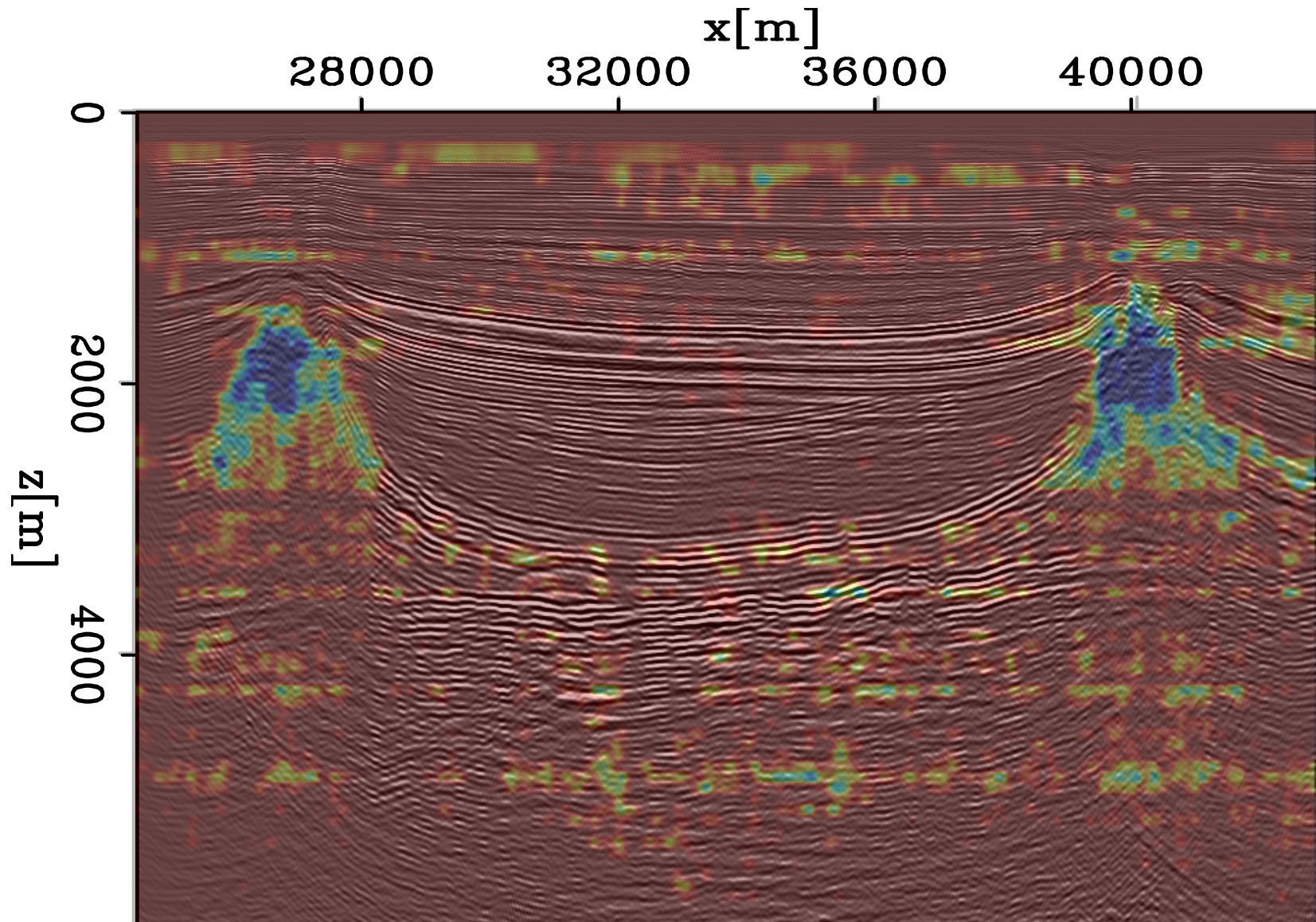
Slope of ADCIGs

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



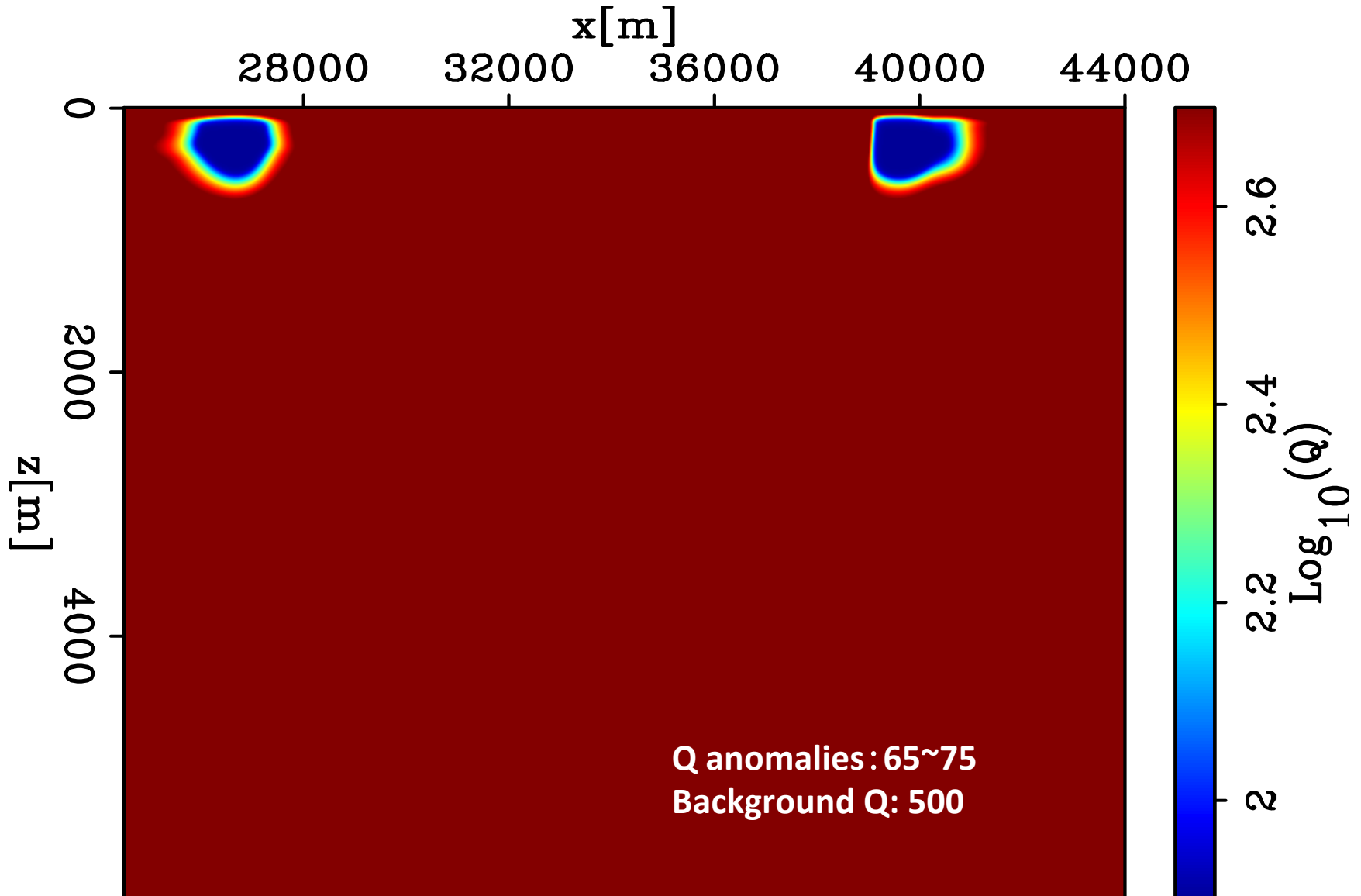
Slope of near angle image

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



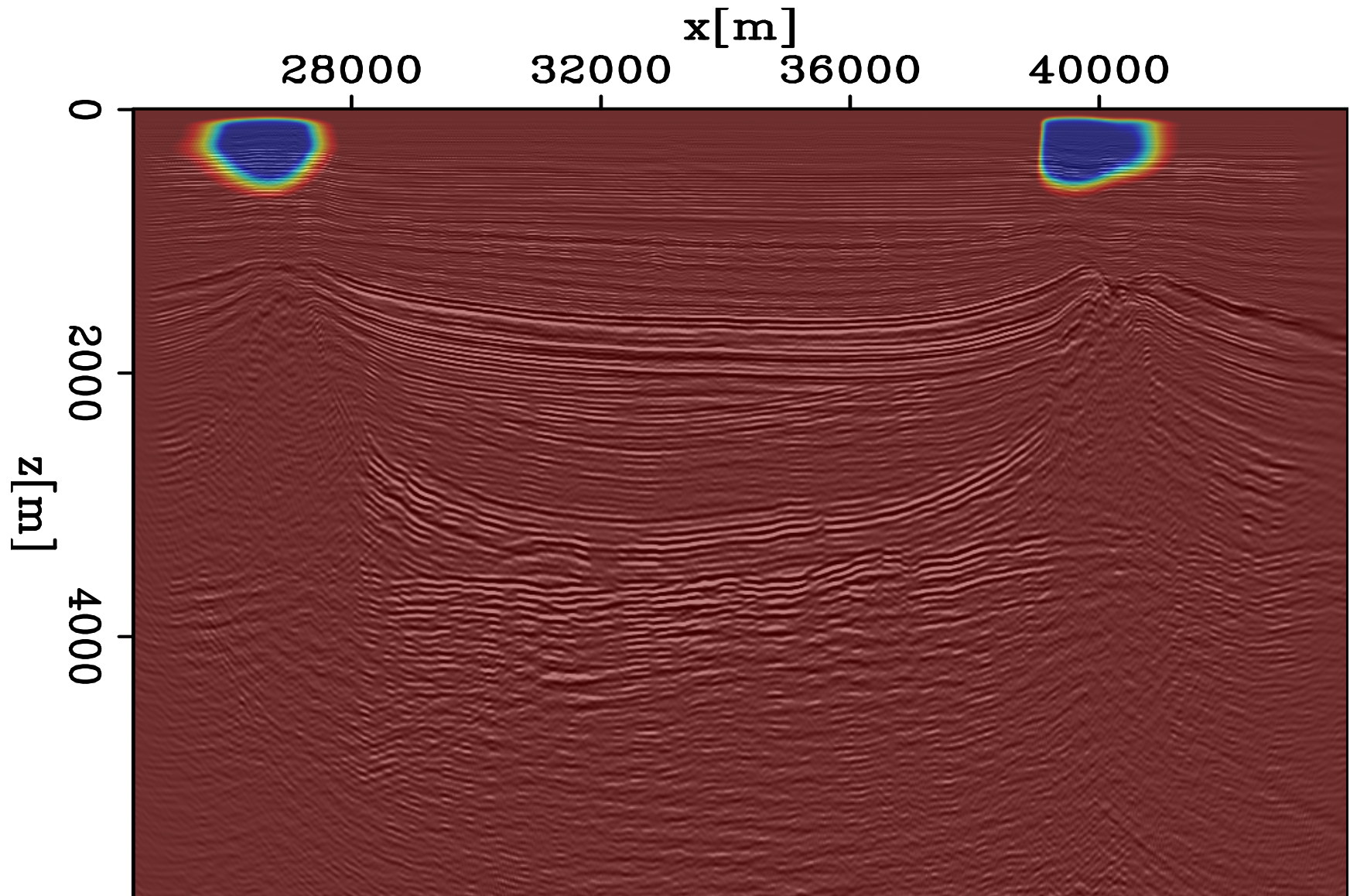
Inverted Q using **prestack** WEMQA

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



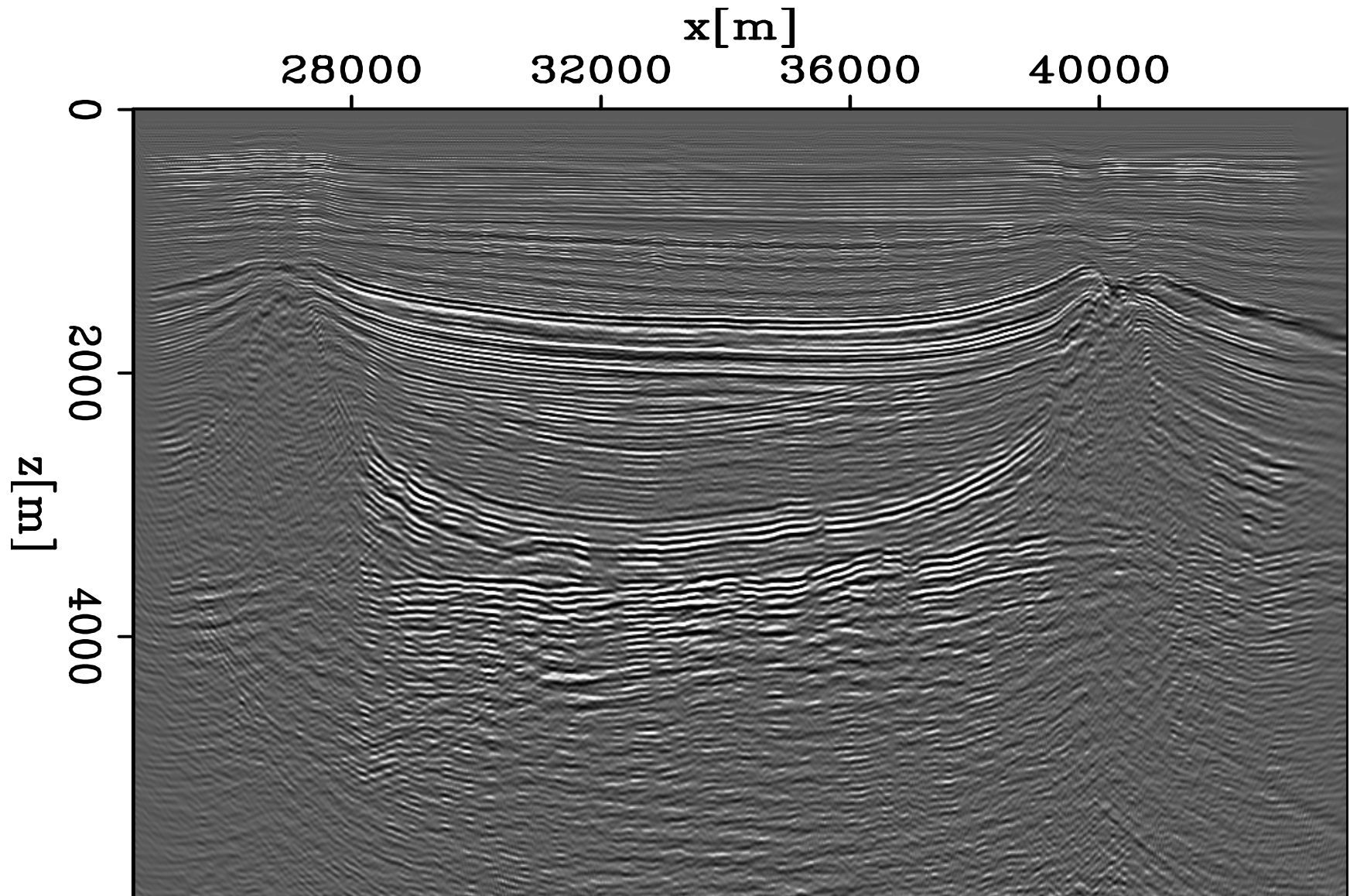
Inverted Q using **prestack** WEMQA

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



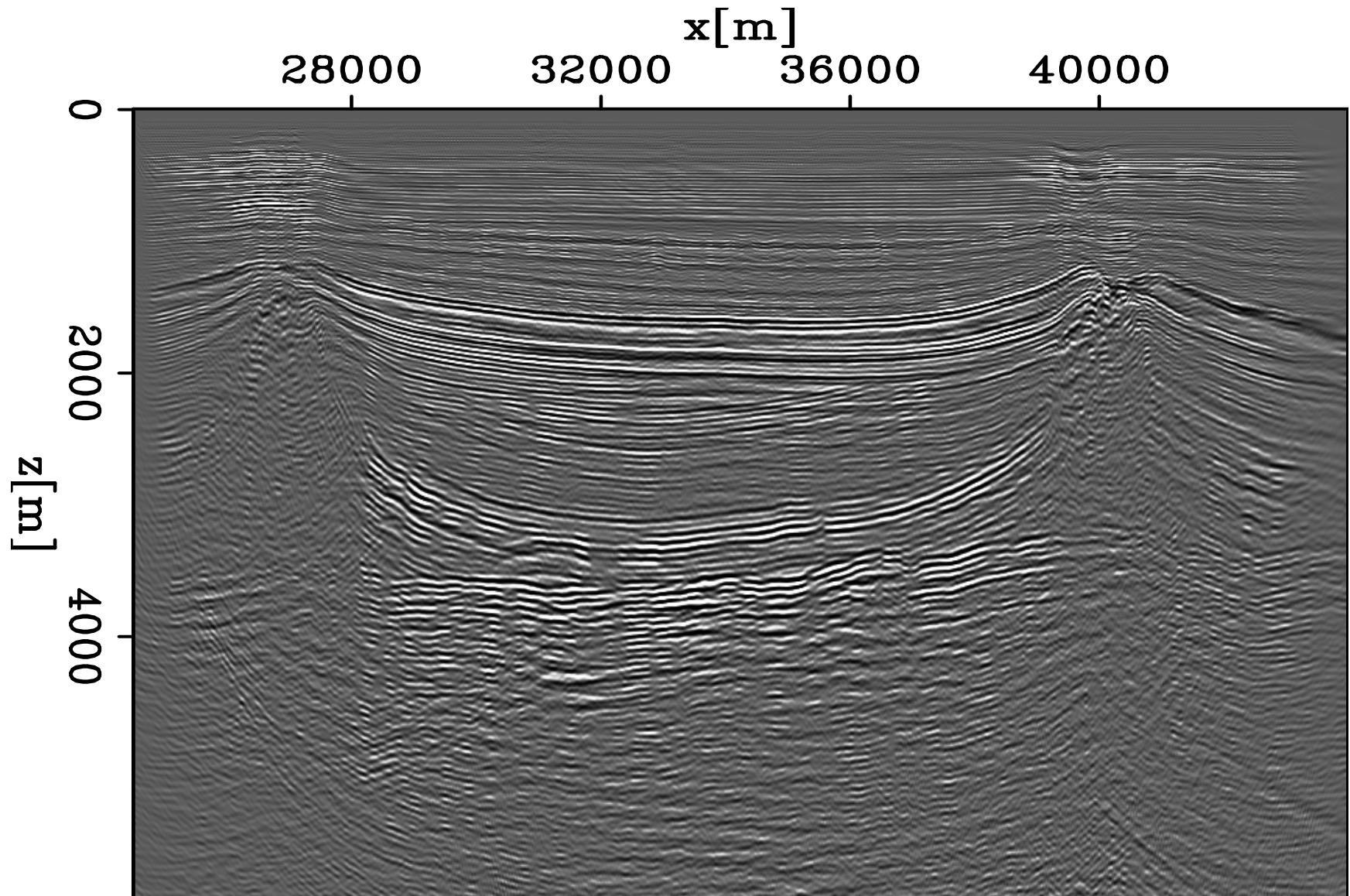
2D image **before** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



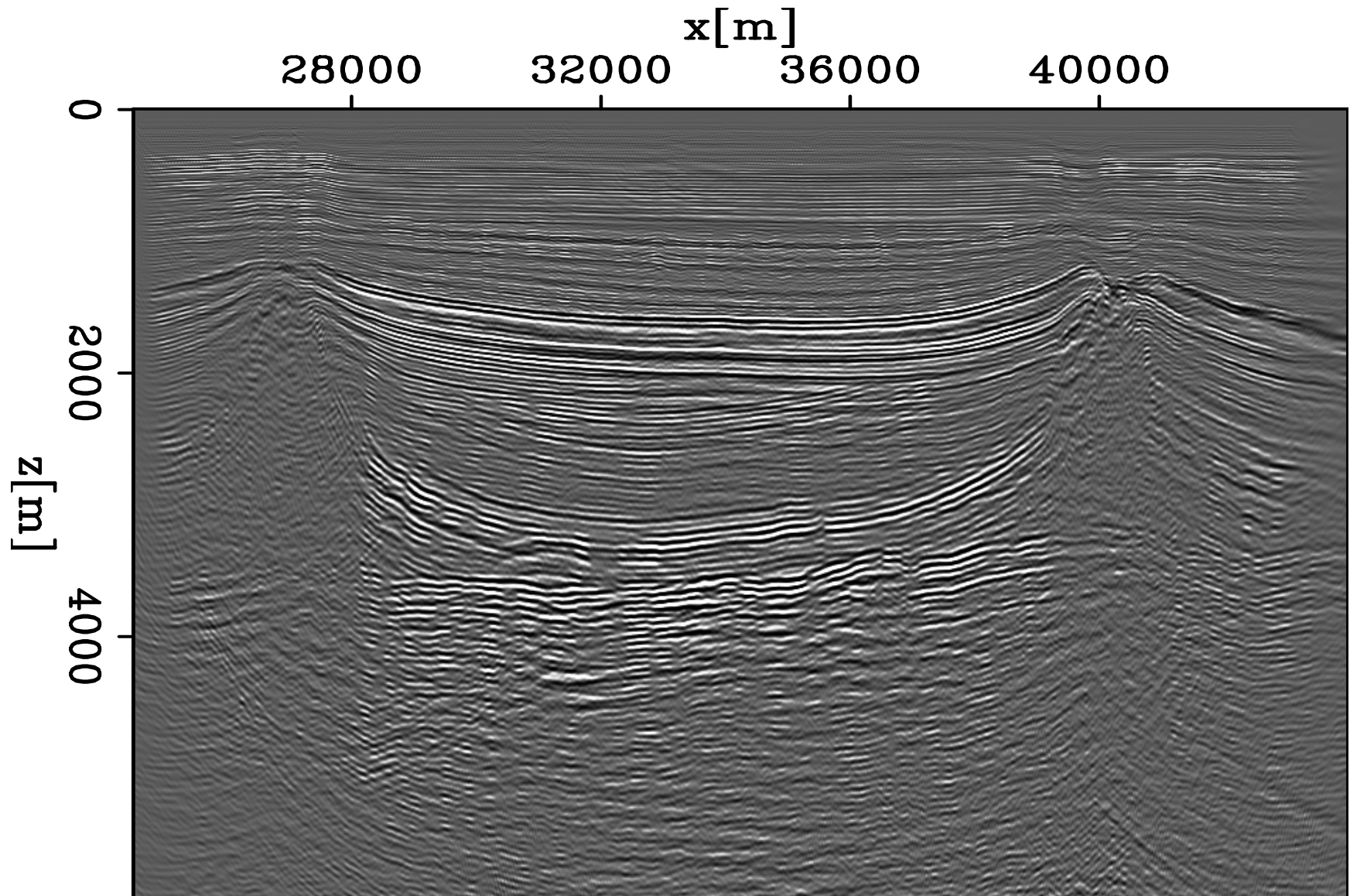
2D image **after** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



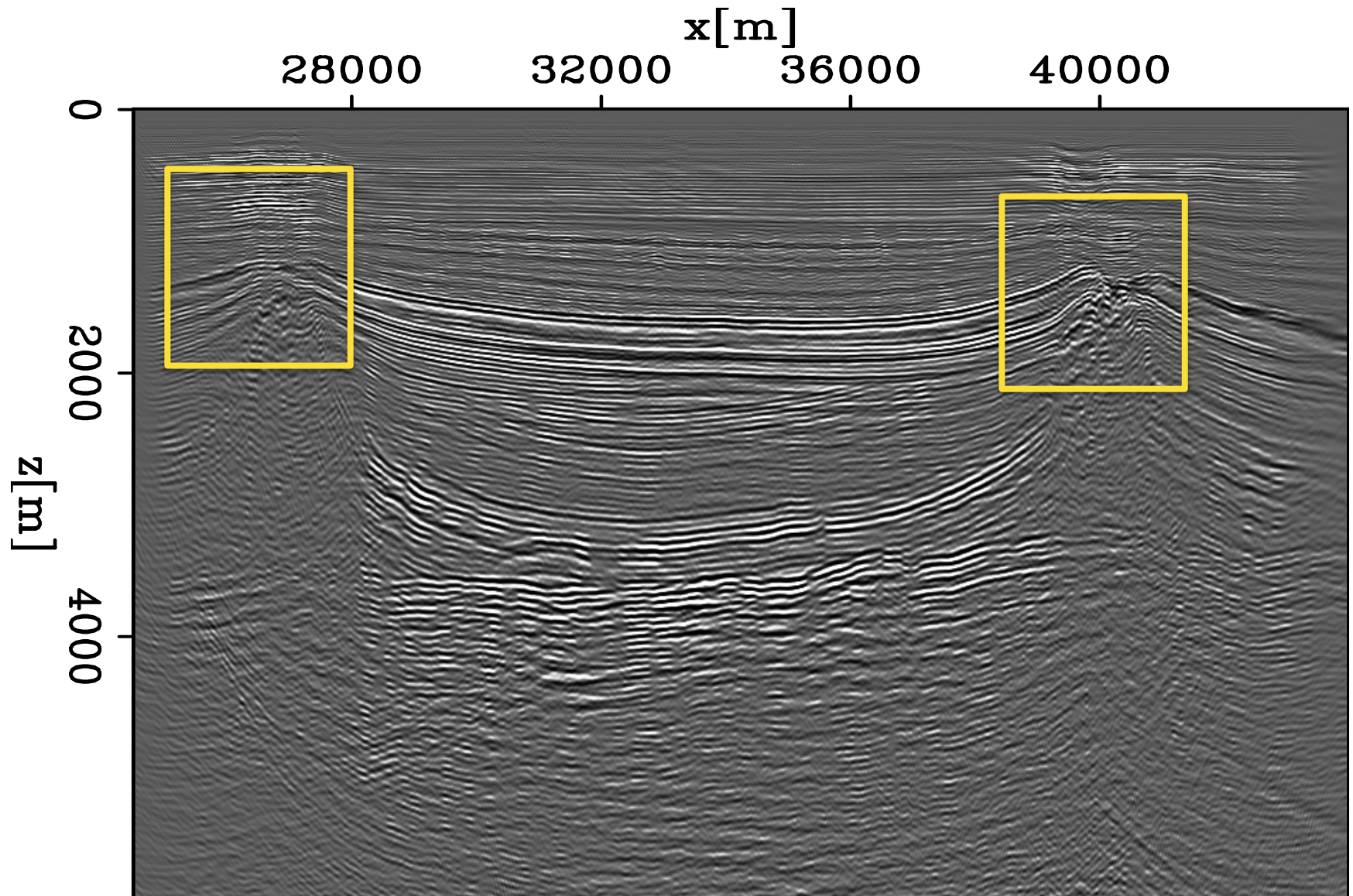
2D image before Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



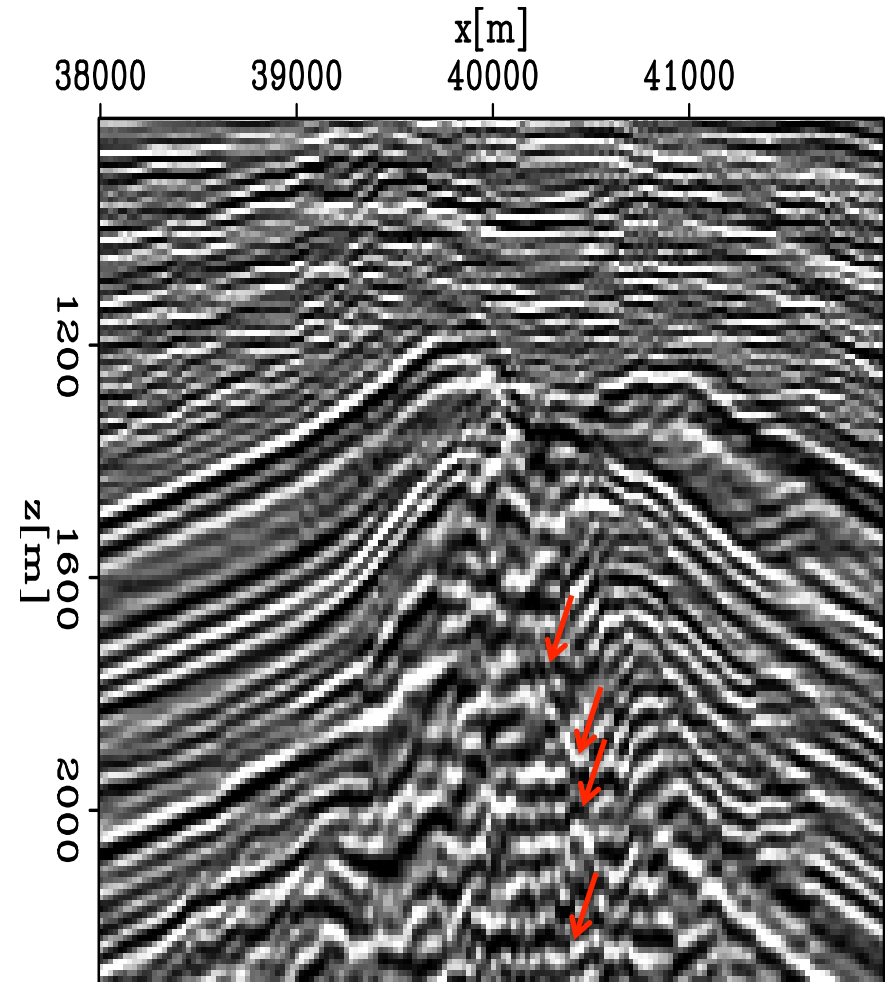
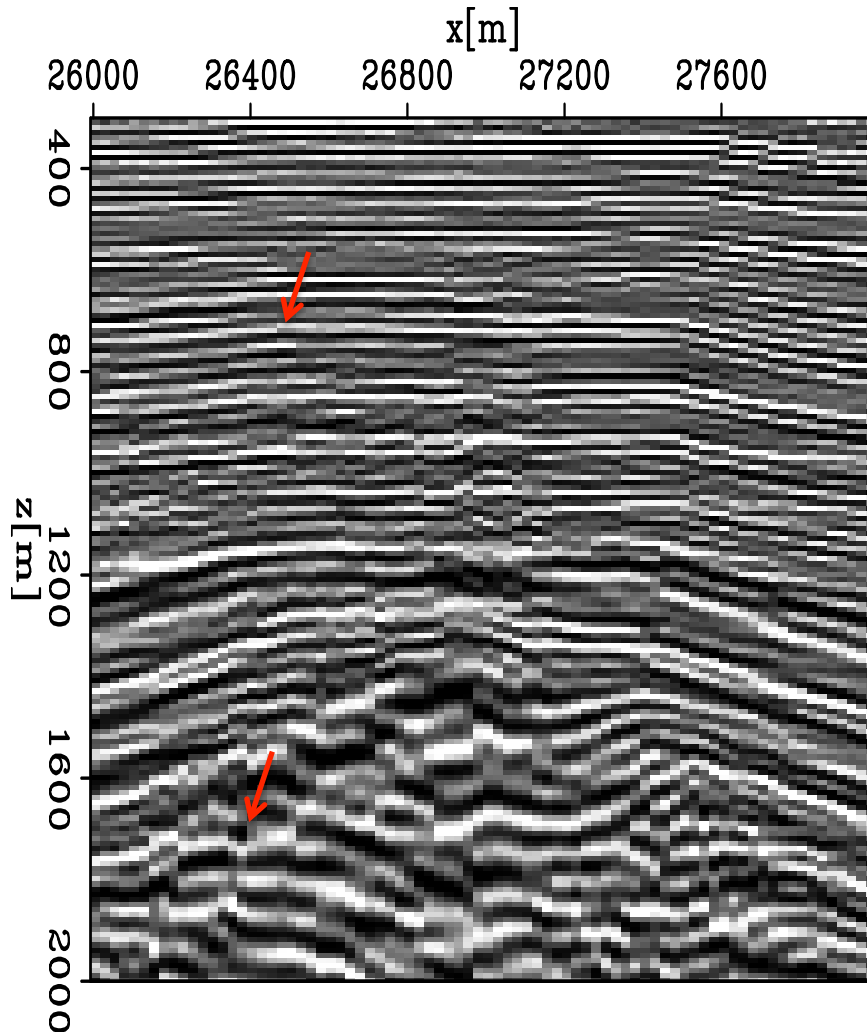
2D image **after** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



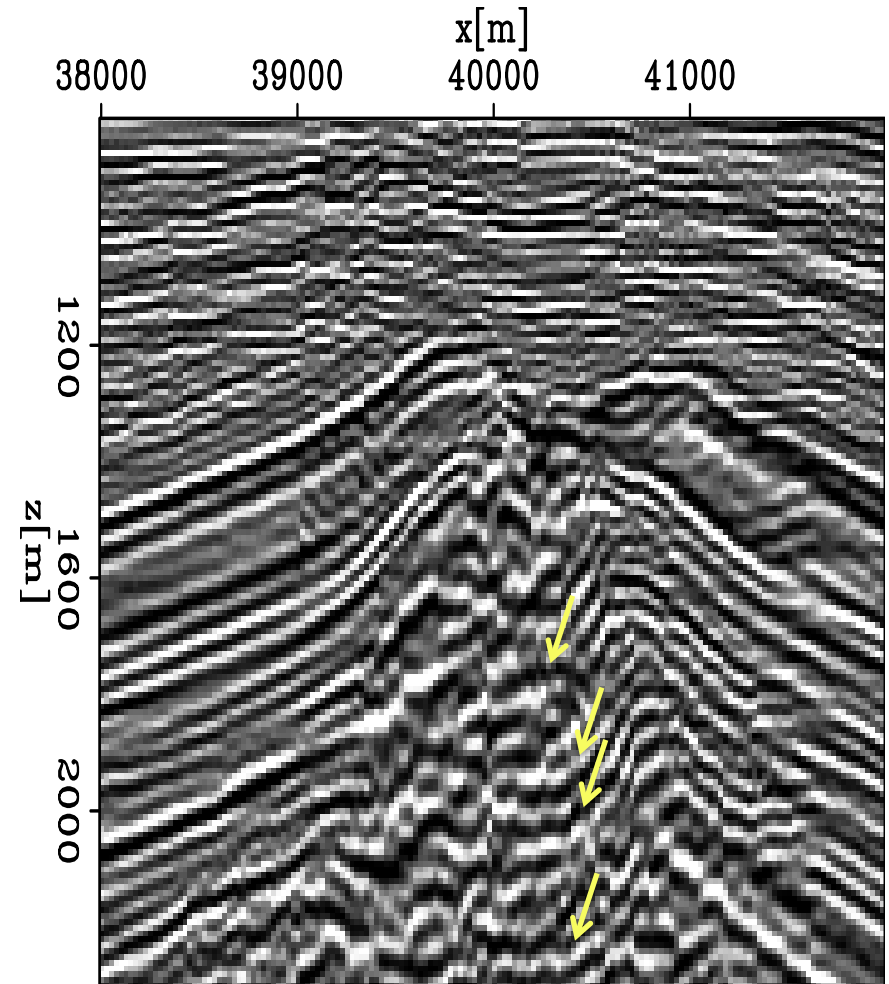
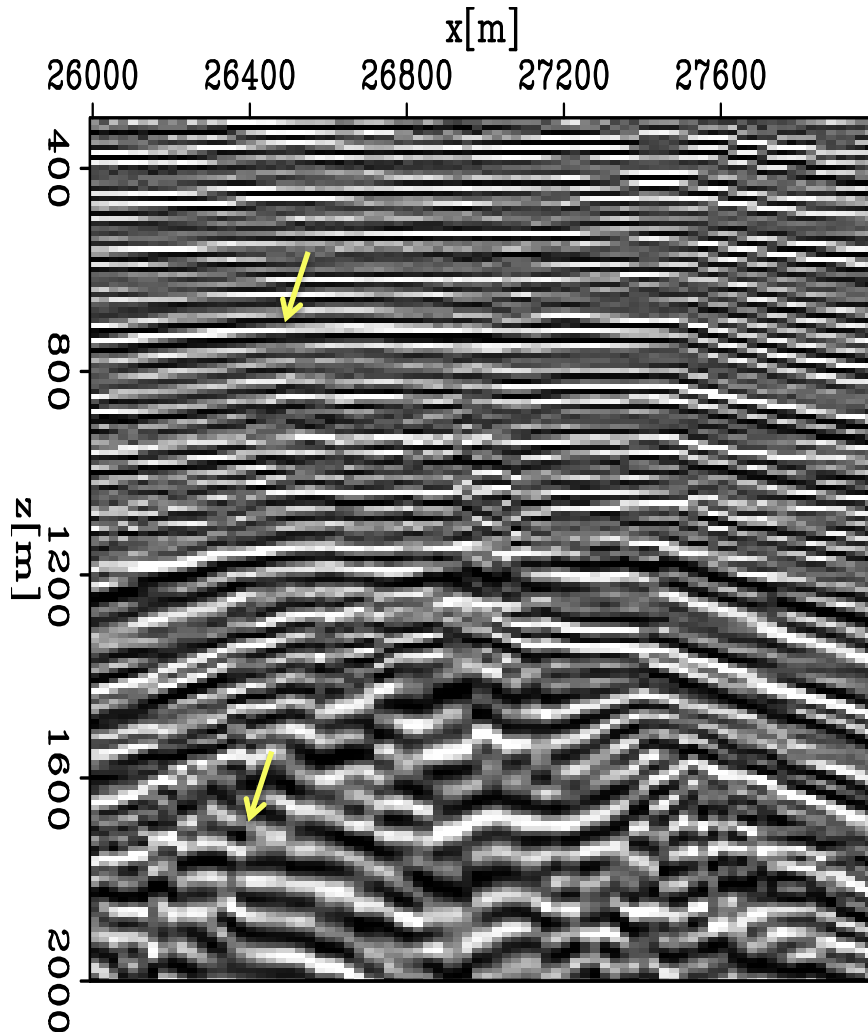
2D image **before** Q compensation: Automatic gain control (AGC) is applied

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



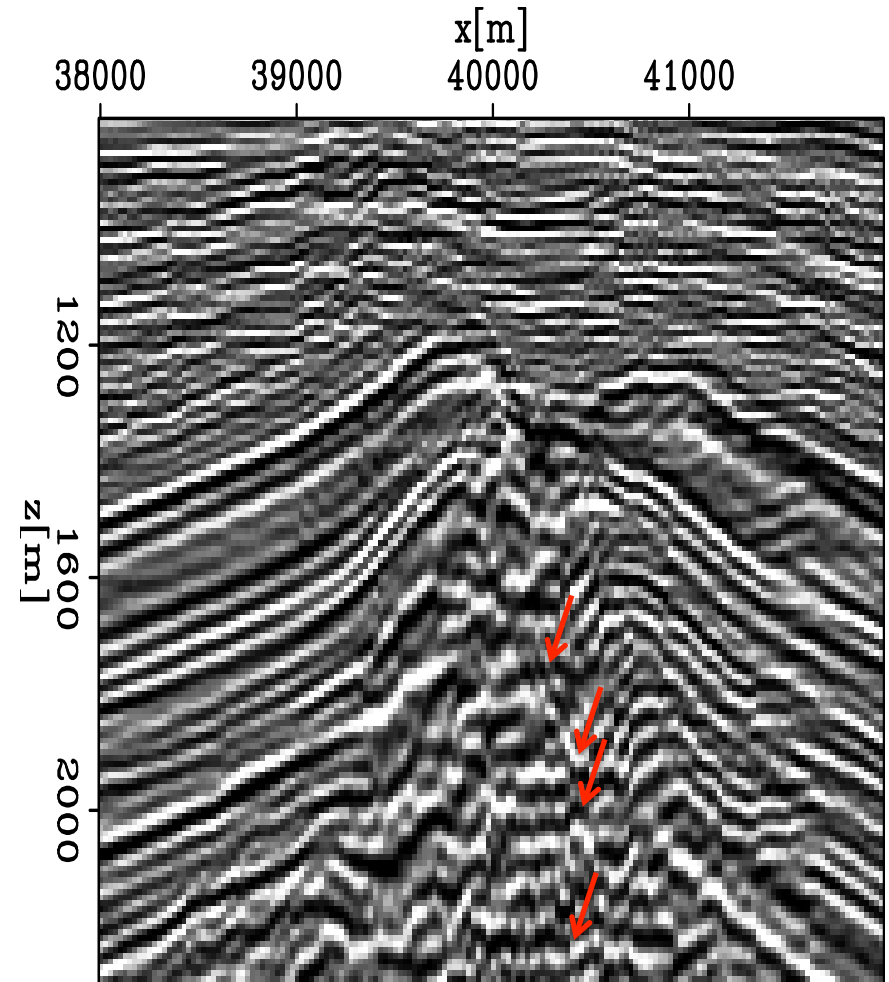
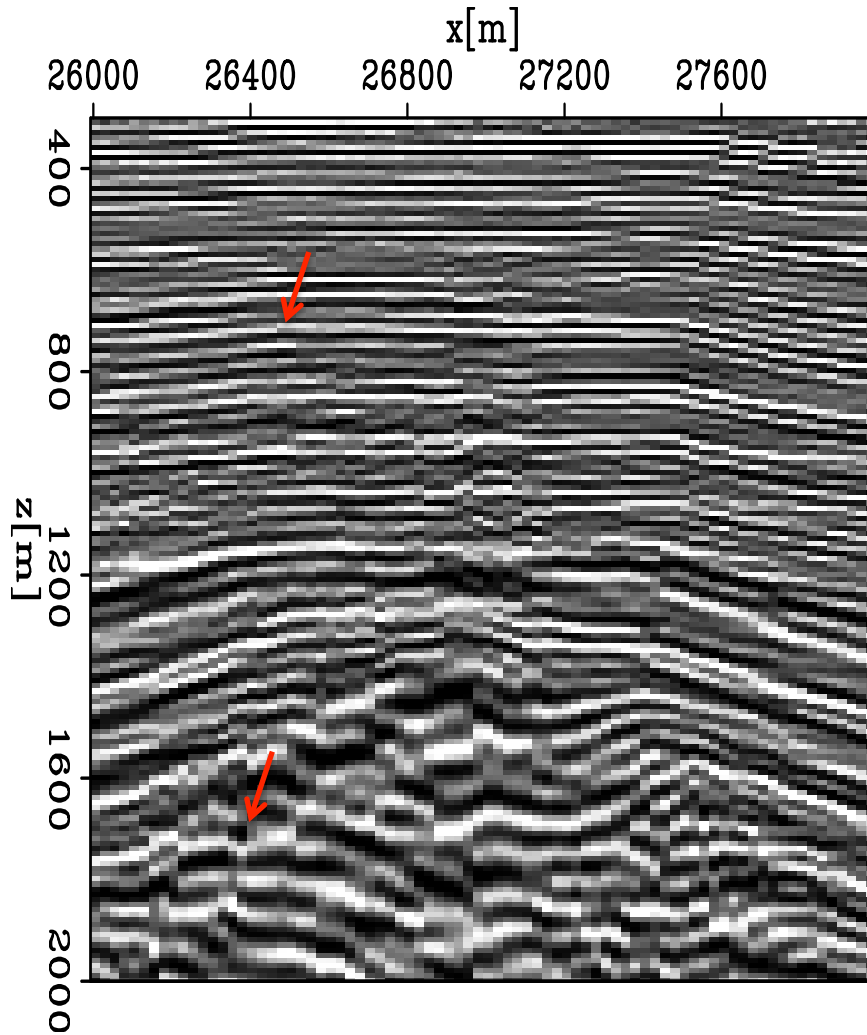
2D image **after** Q compensation: Automatic gain control (AGC) is applied

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



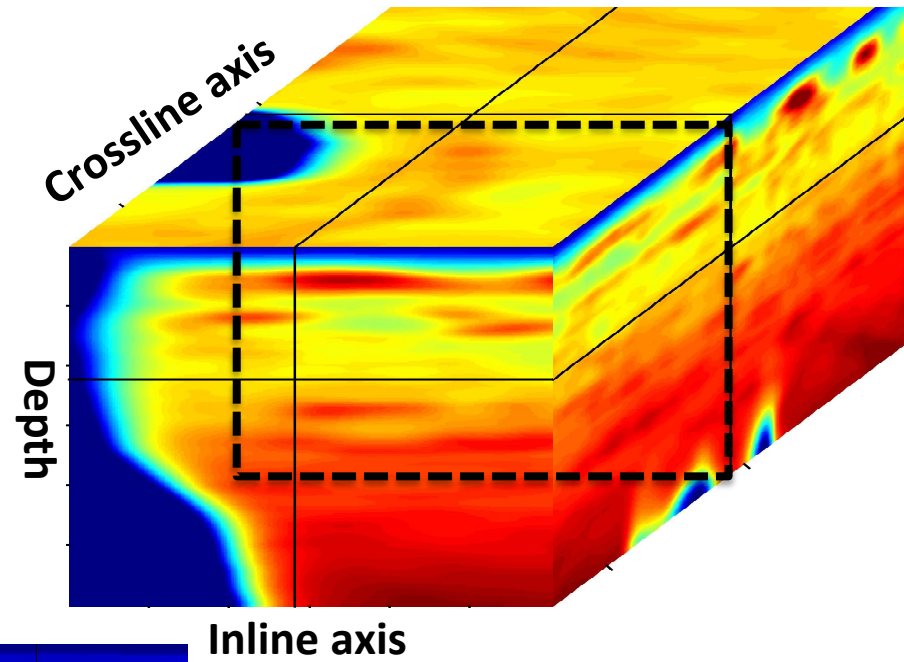
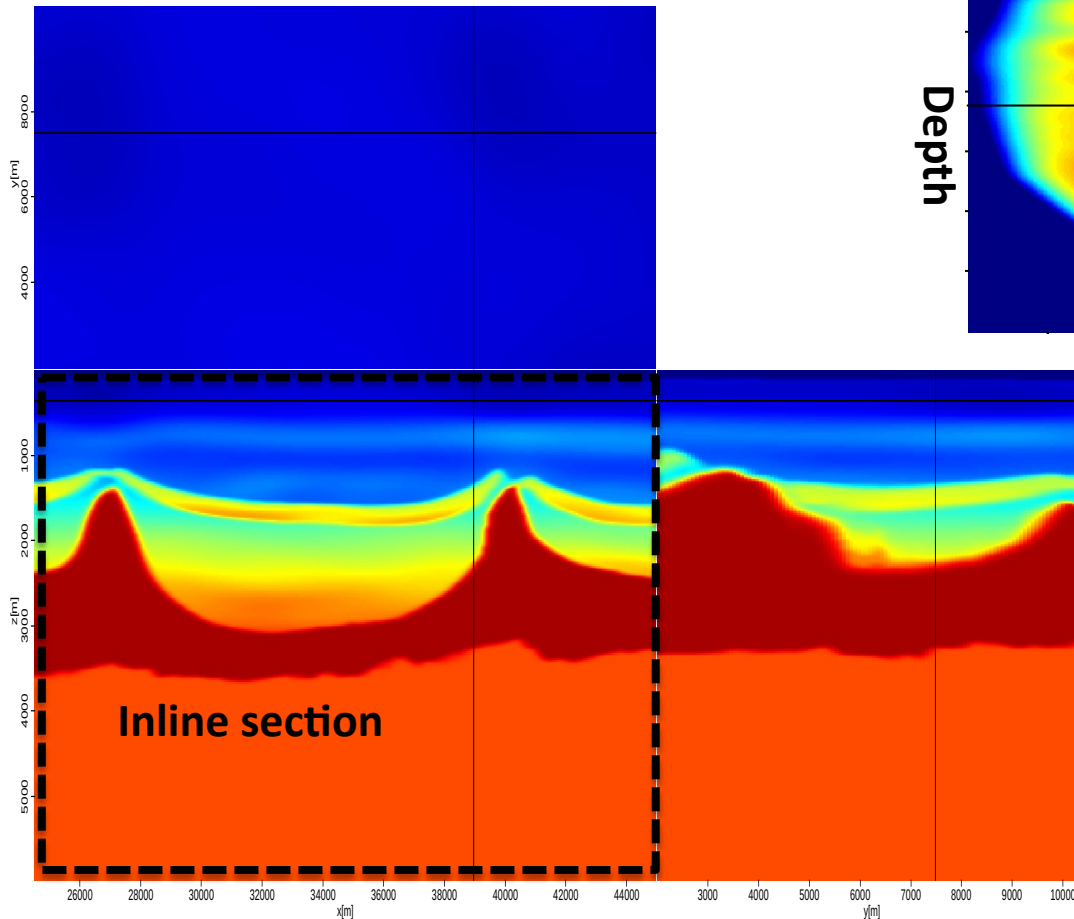
2D image before Q compensation: Automatic gain control (AGC) is applied

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



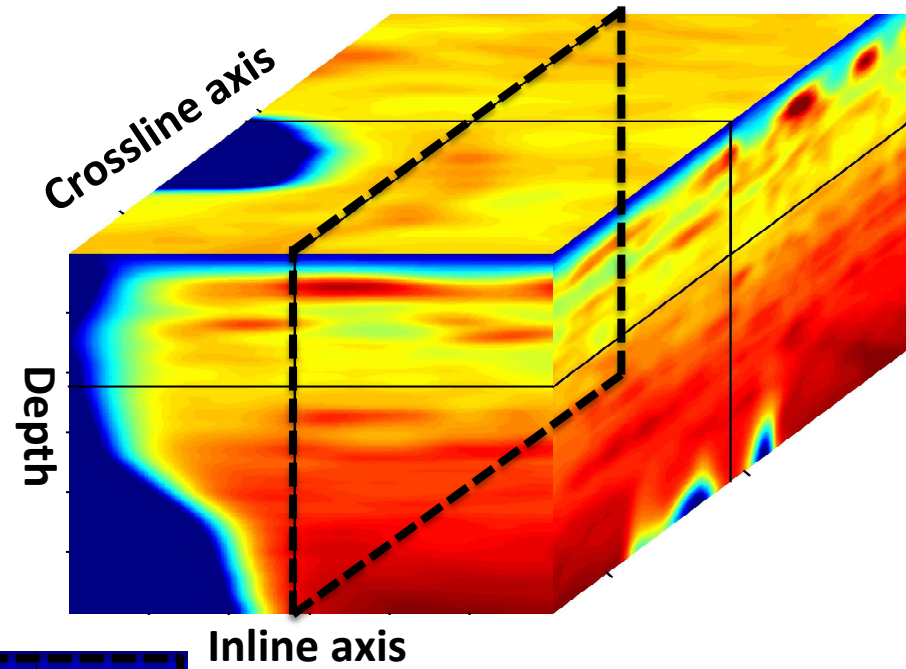
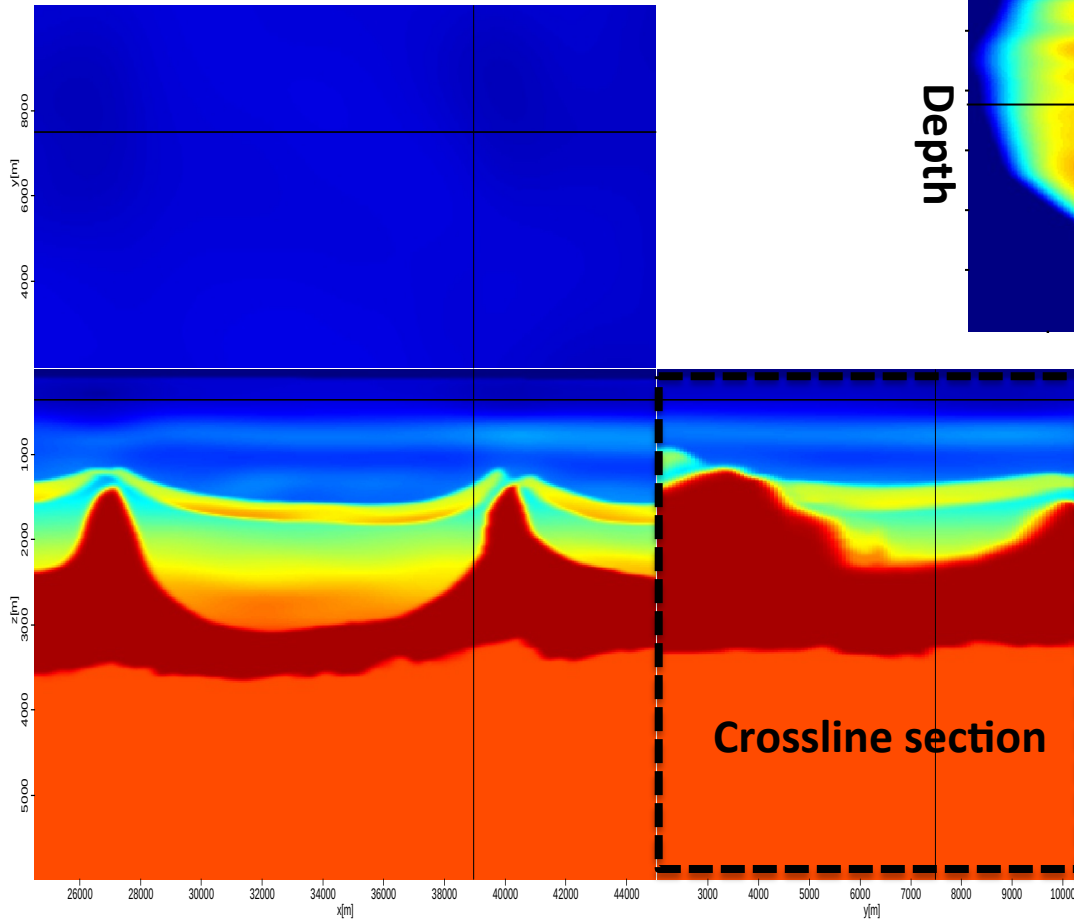
SEP 3D viewer: inline section

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



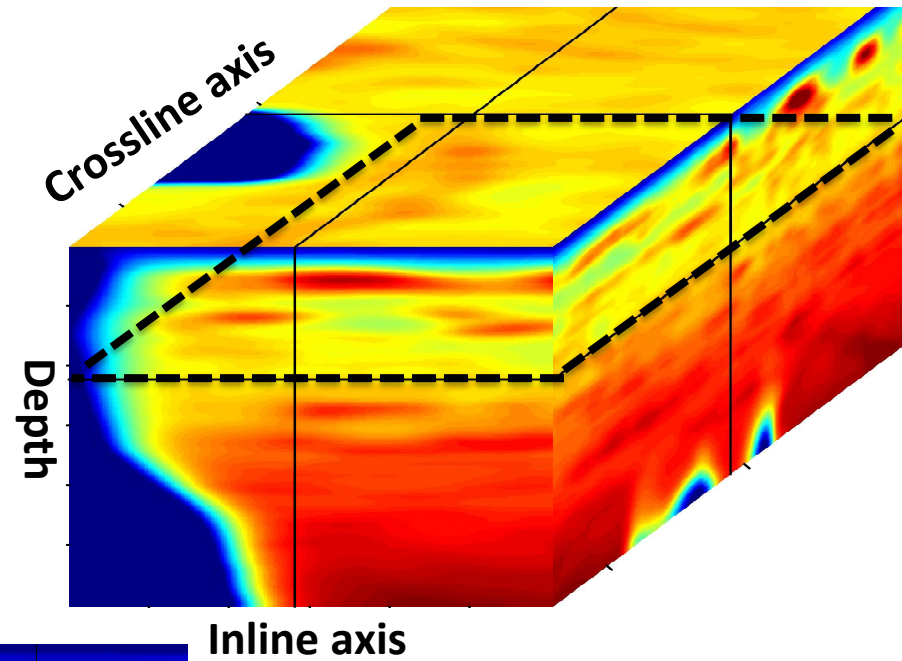
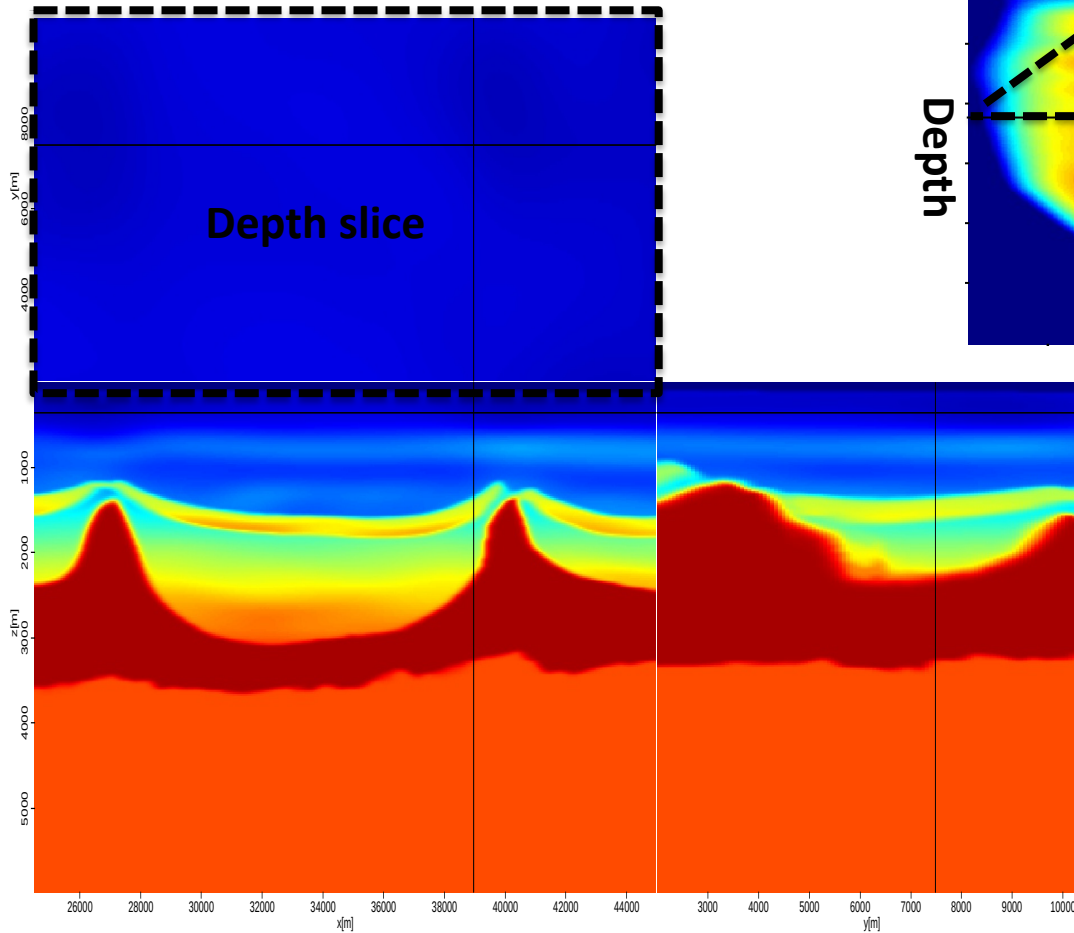
SEP 3D viewer: inline section

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



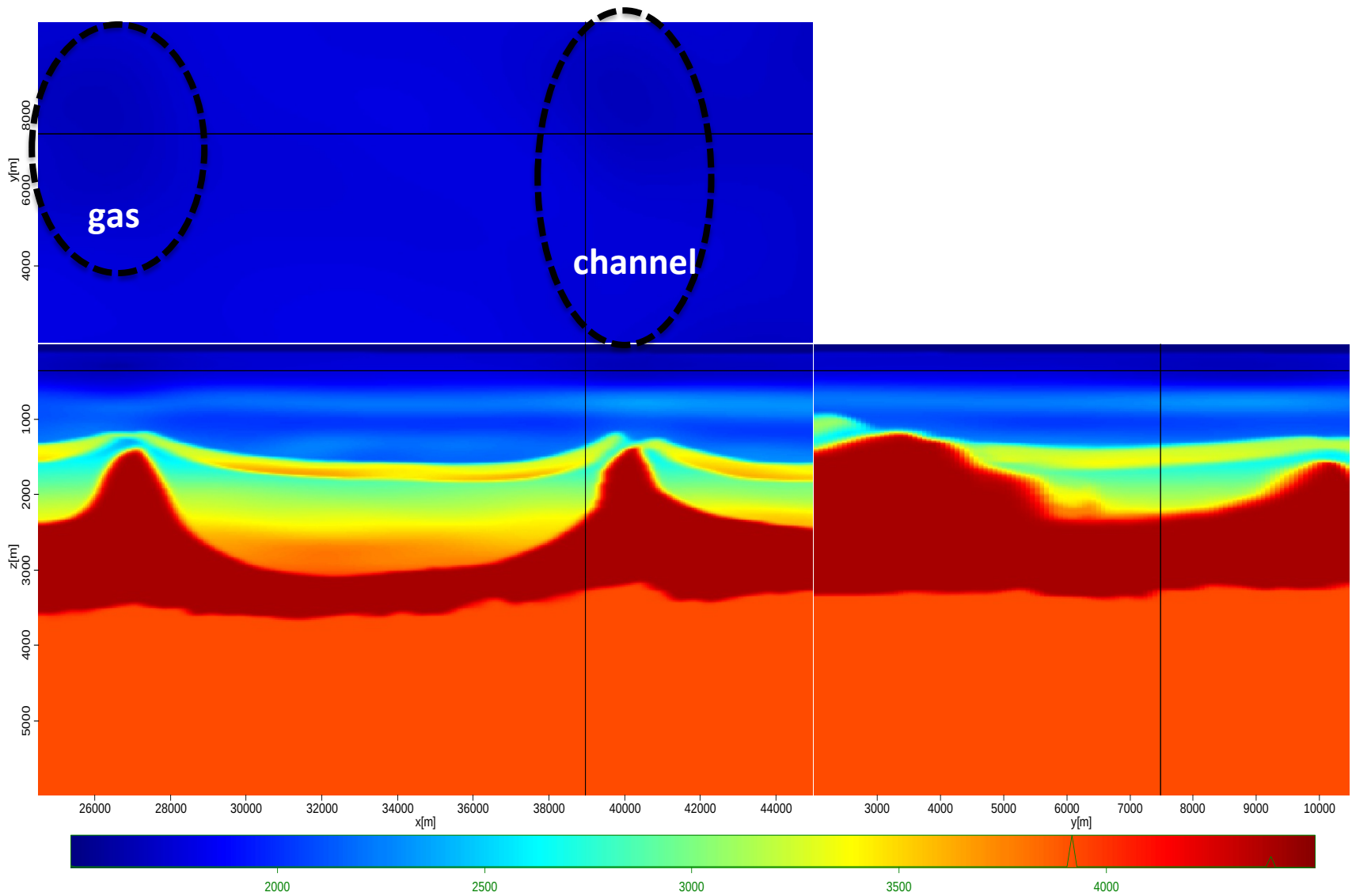
SEP 3D viewer: depth slice

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



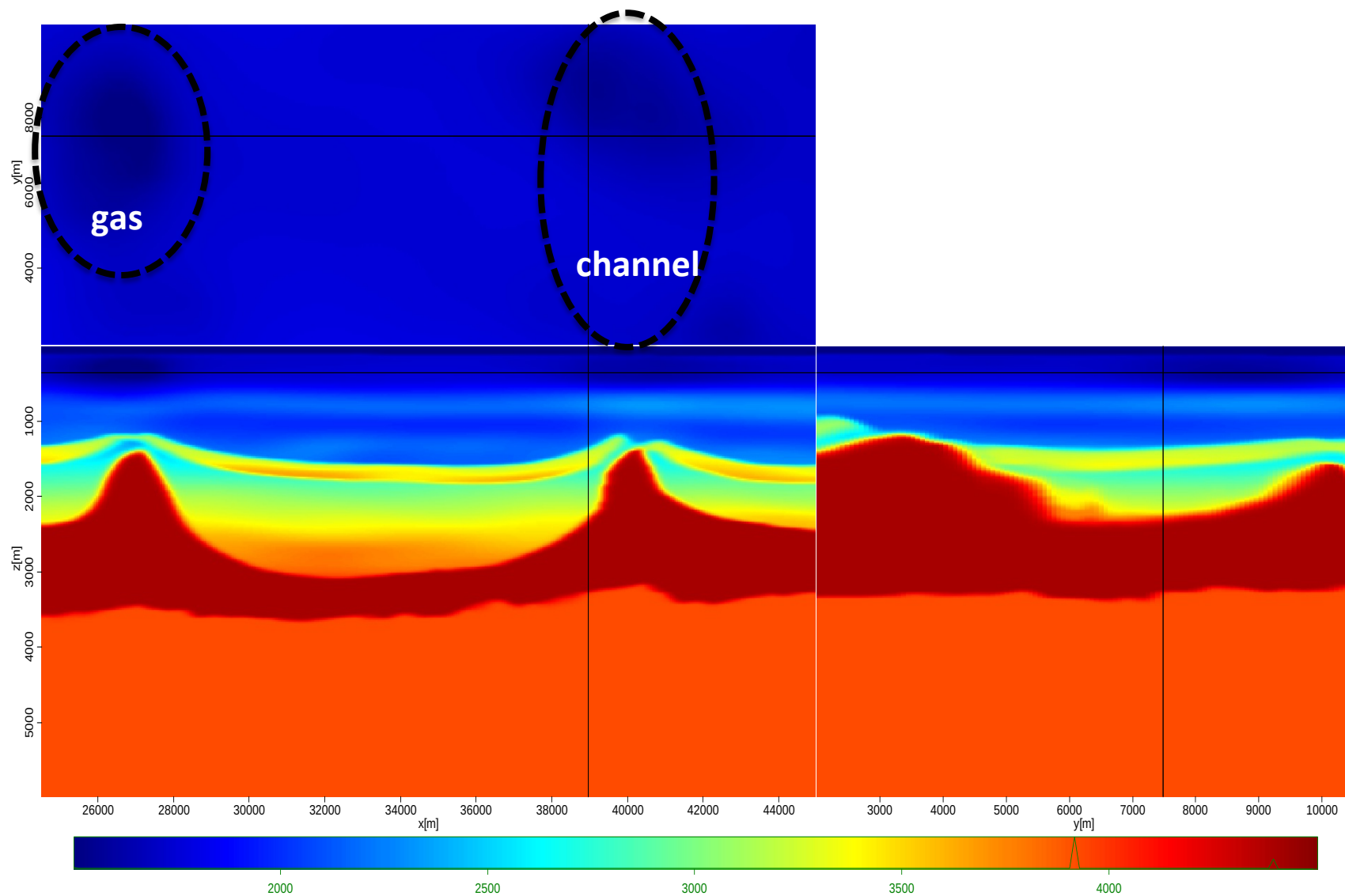
3D initial velocity

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



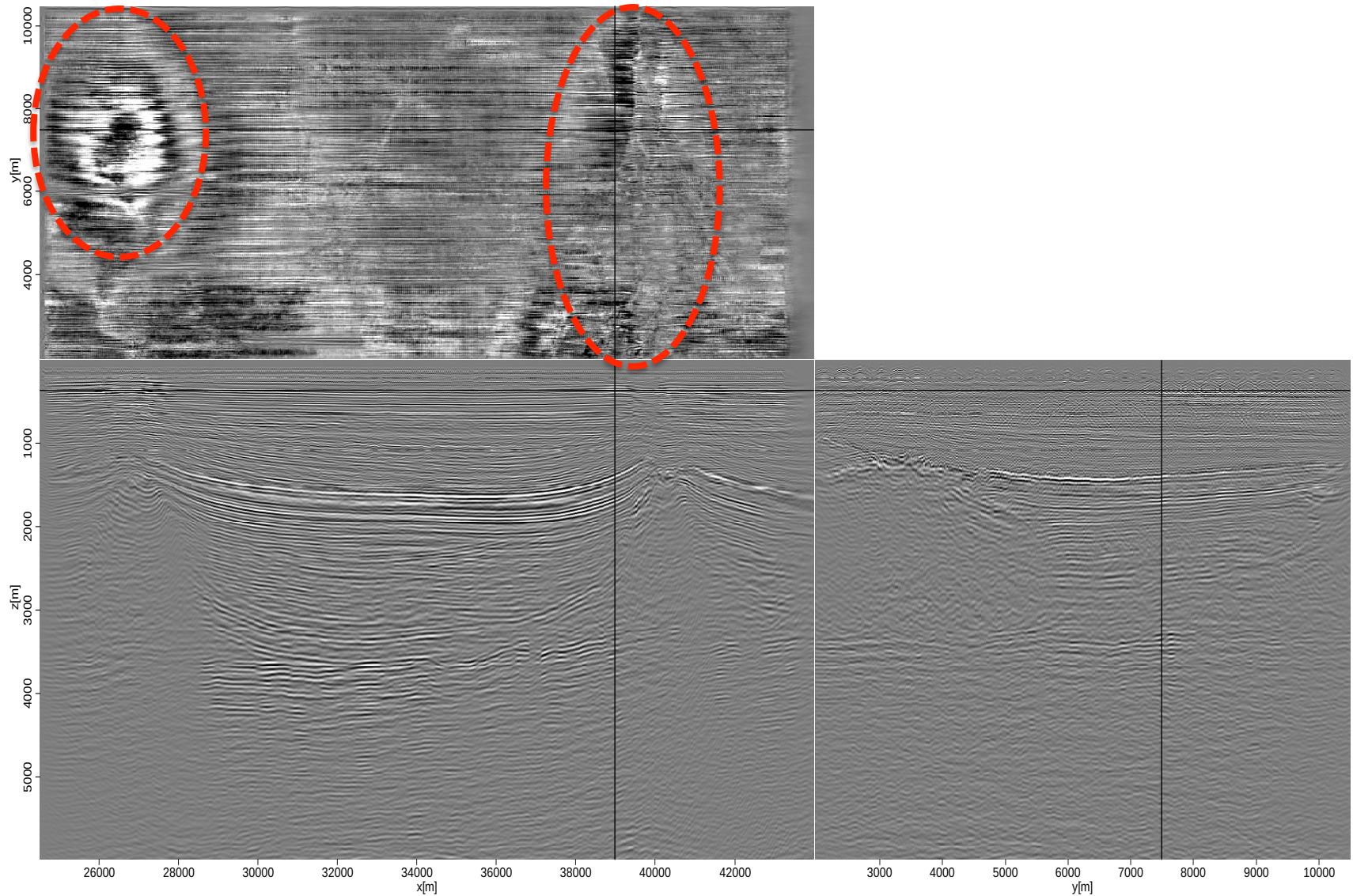
3D updated velocity

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



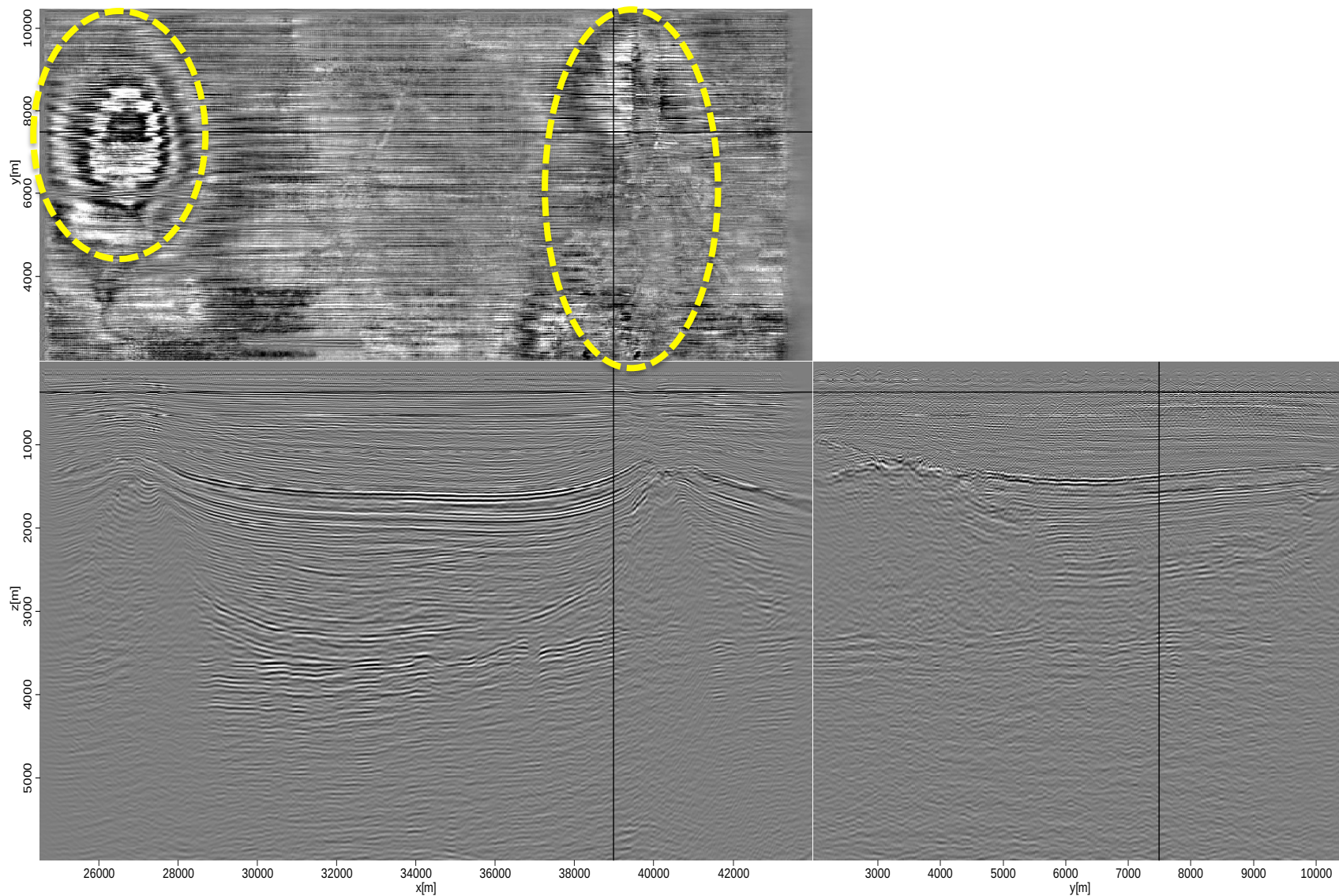
3D image **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



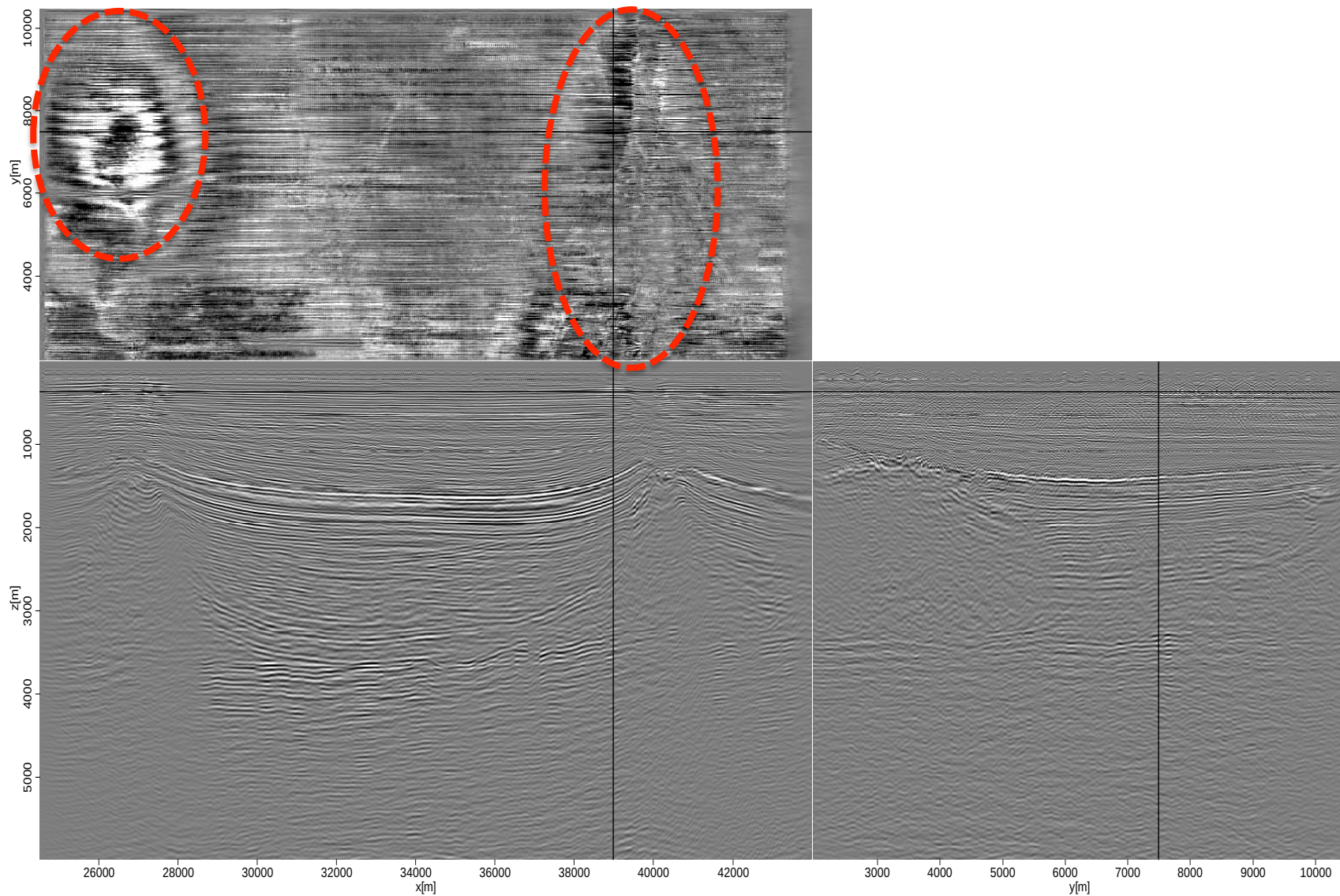
3D image **after** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



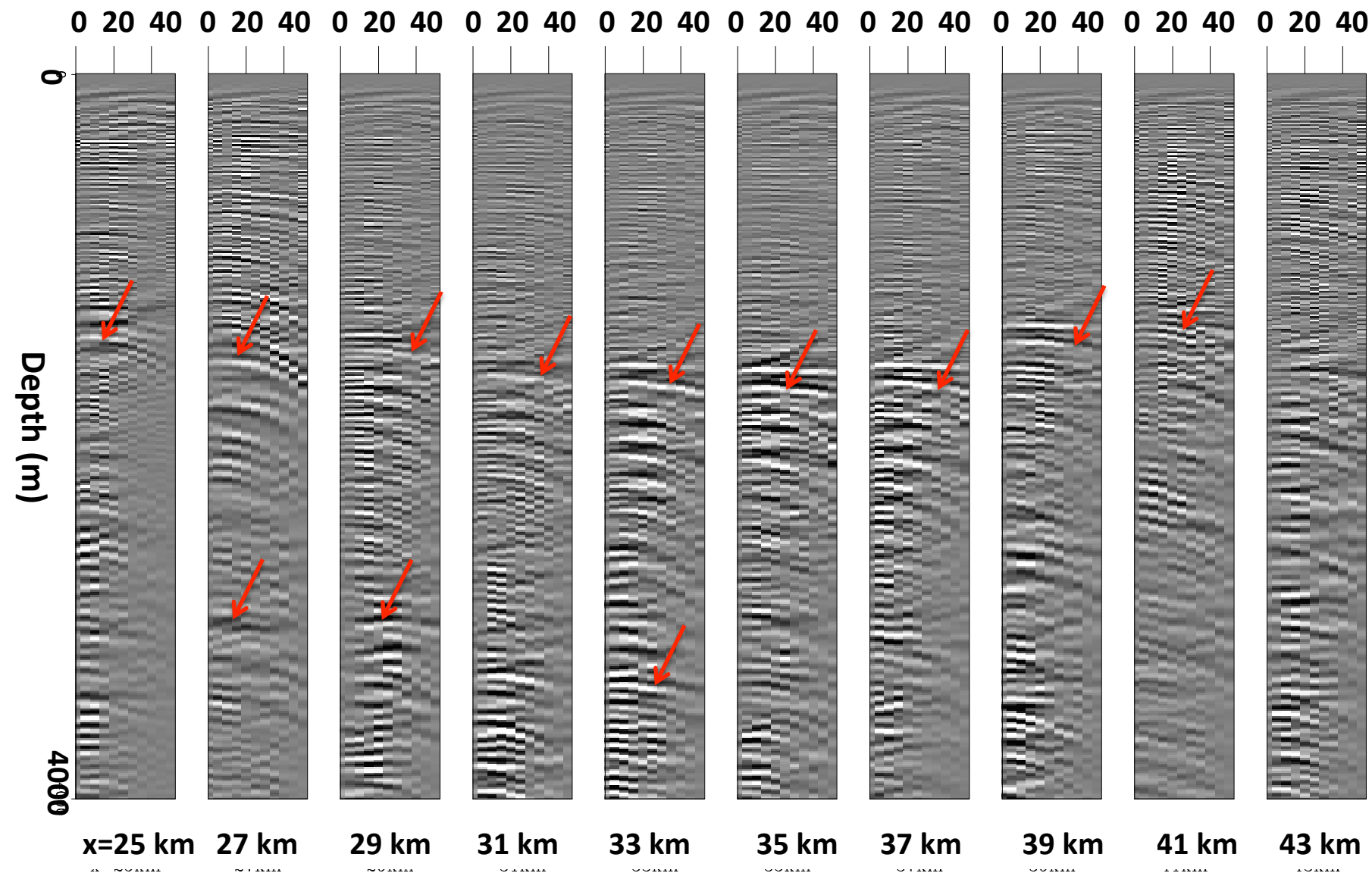
3D image **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



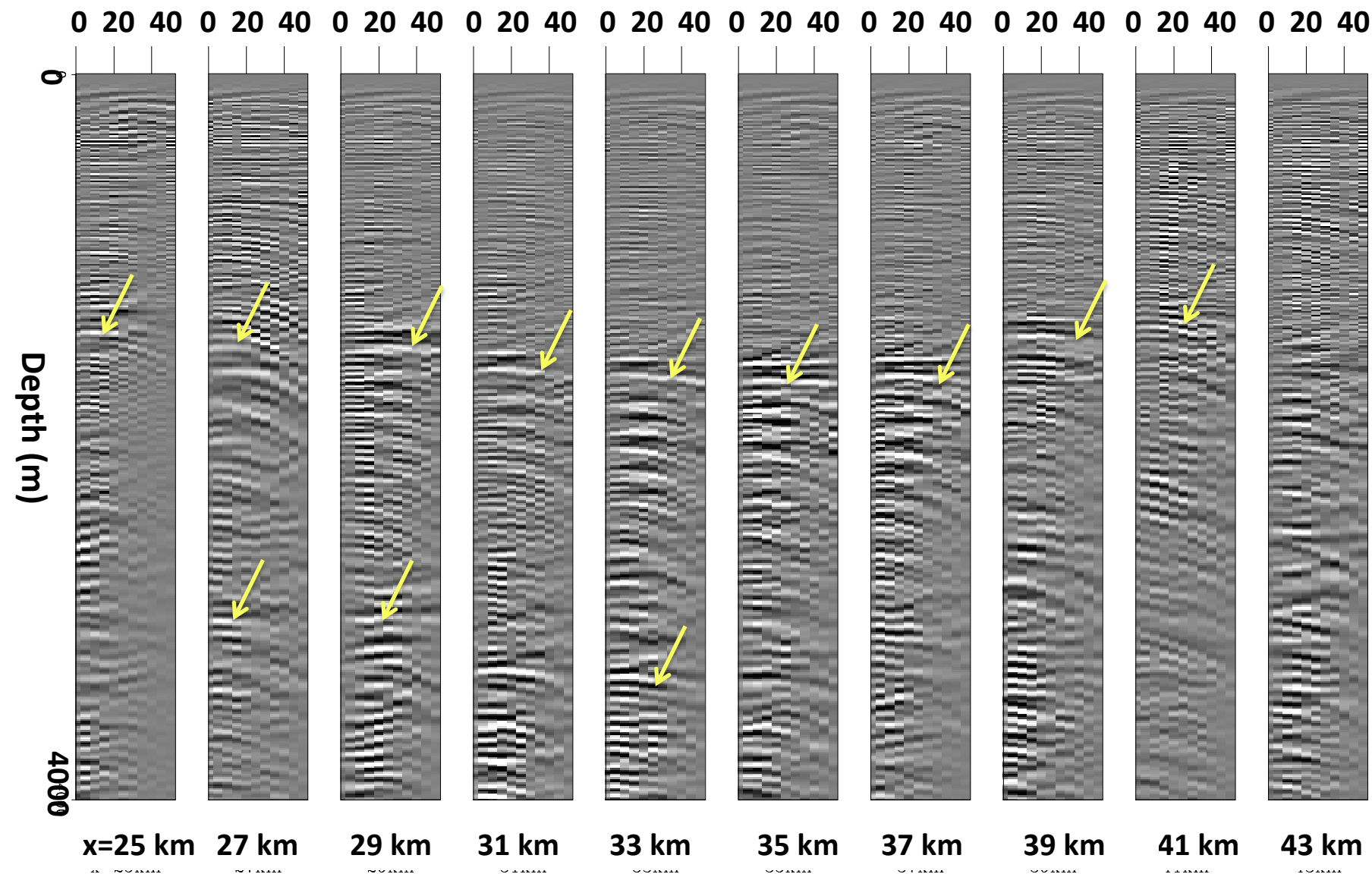
ADCIGs **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



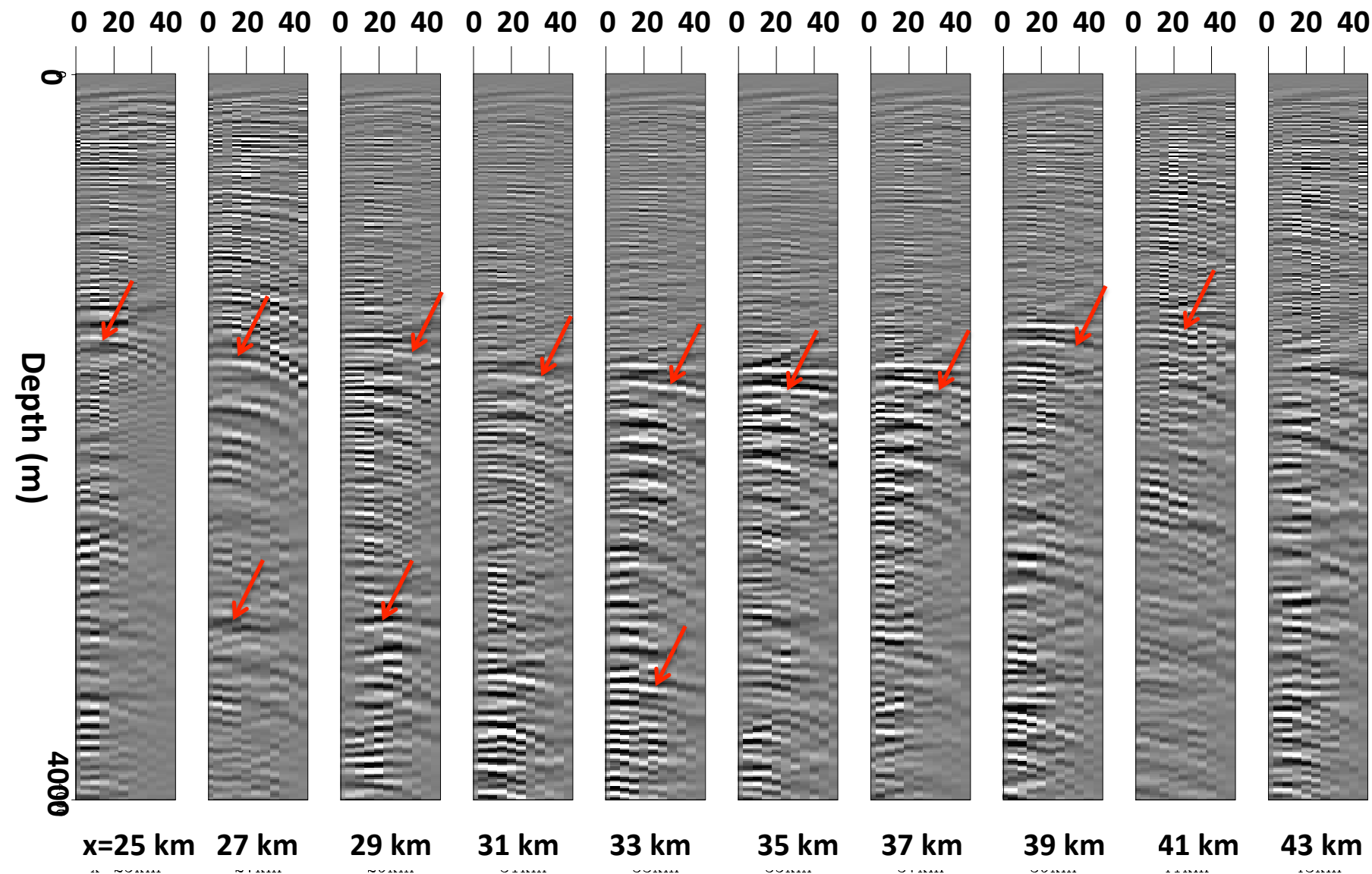
ADCIGs **after** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



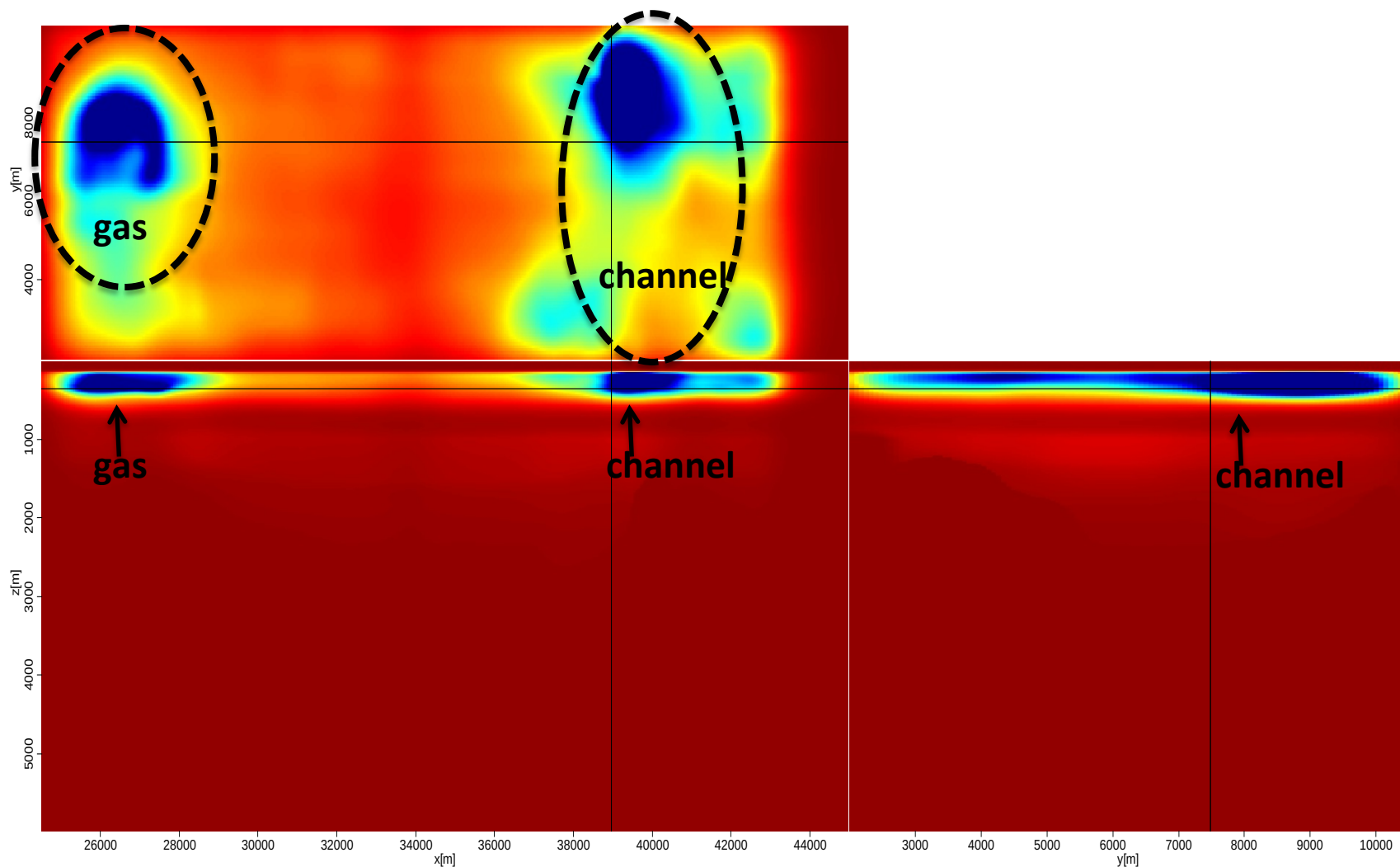
ADCIGs **before** velocity updating

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



Inverted Q model using prestack WEMQA

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA

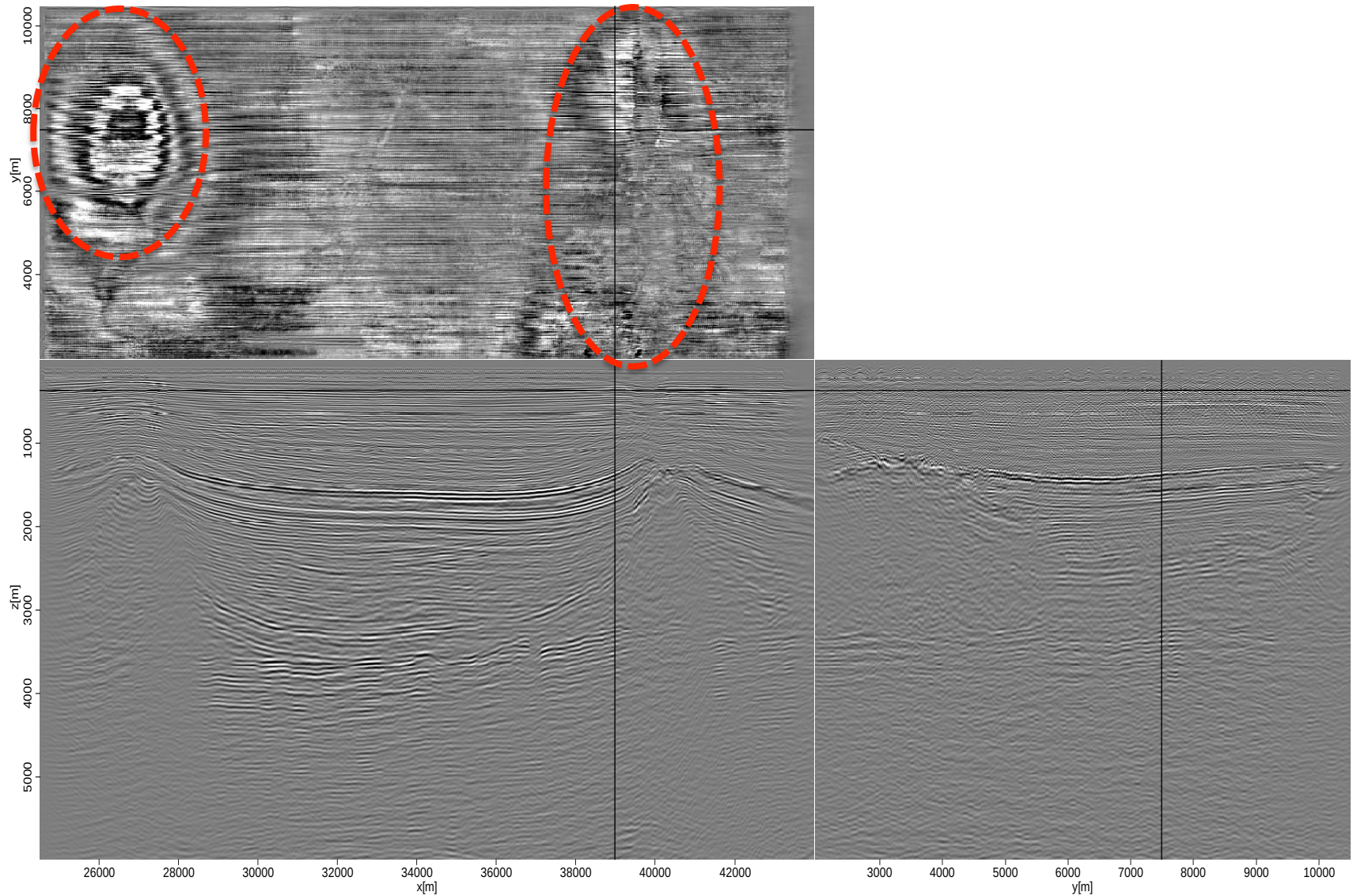


1.89 (Q=75)

2.7 (Q=500)

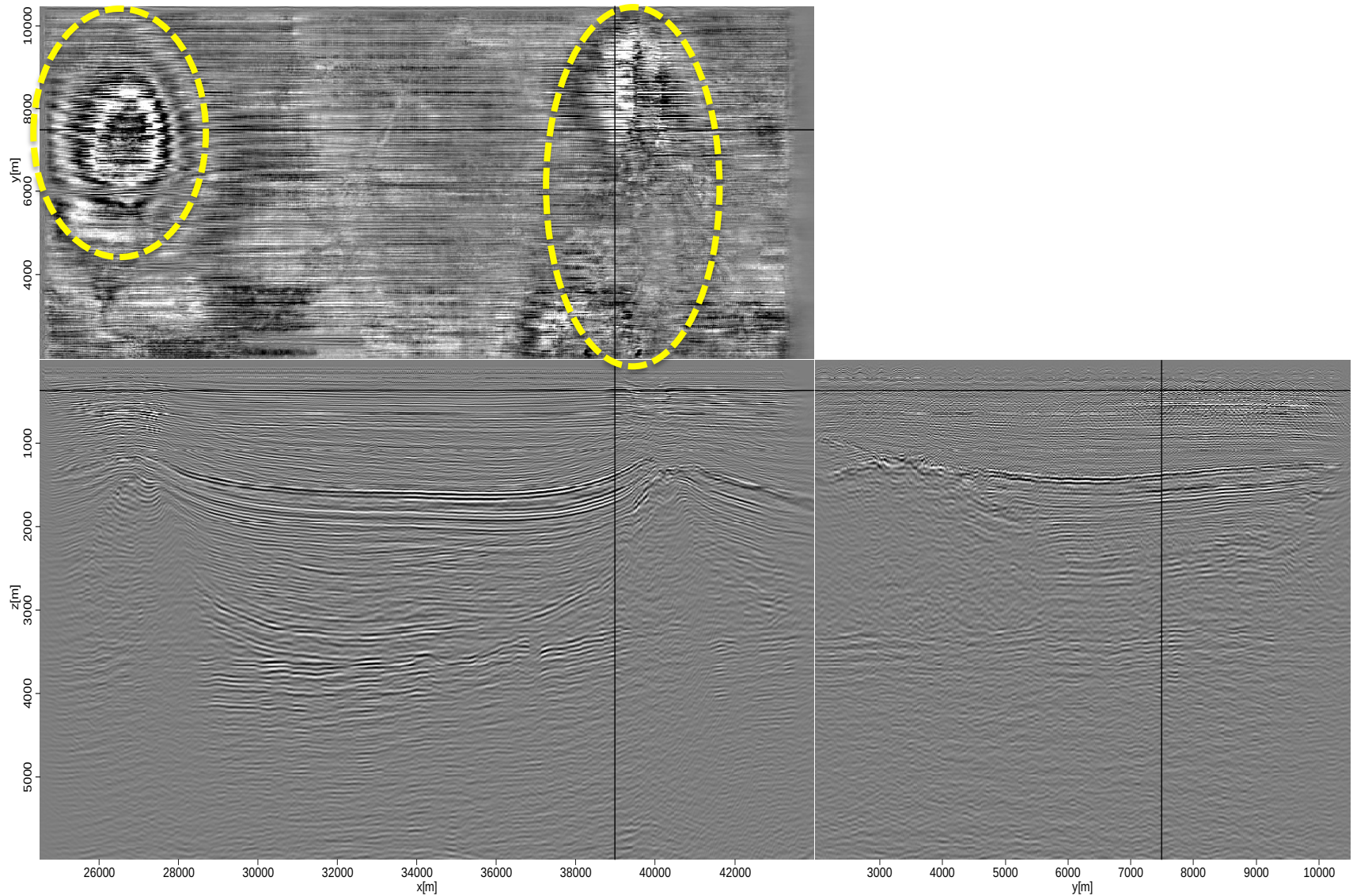
3D image **before** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



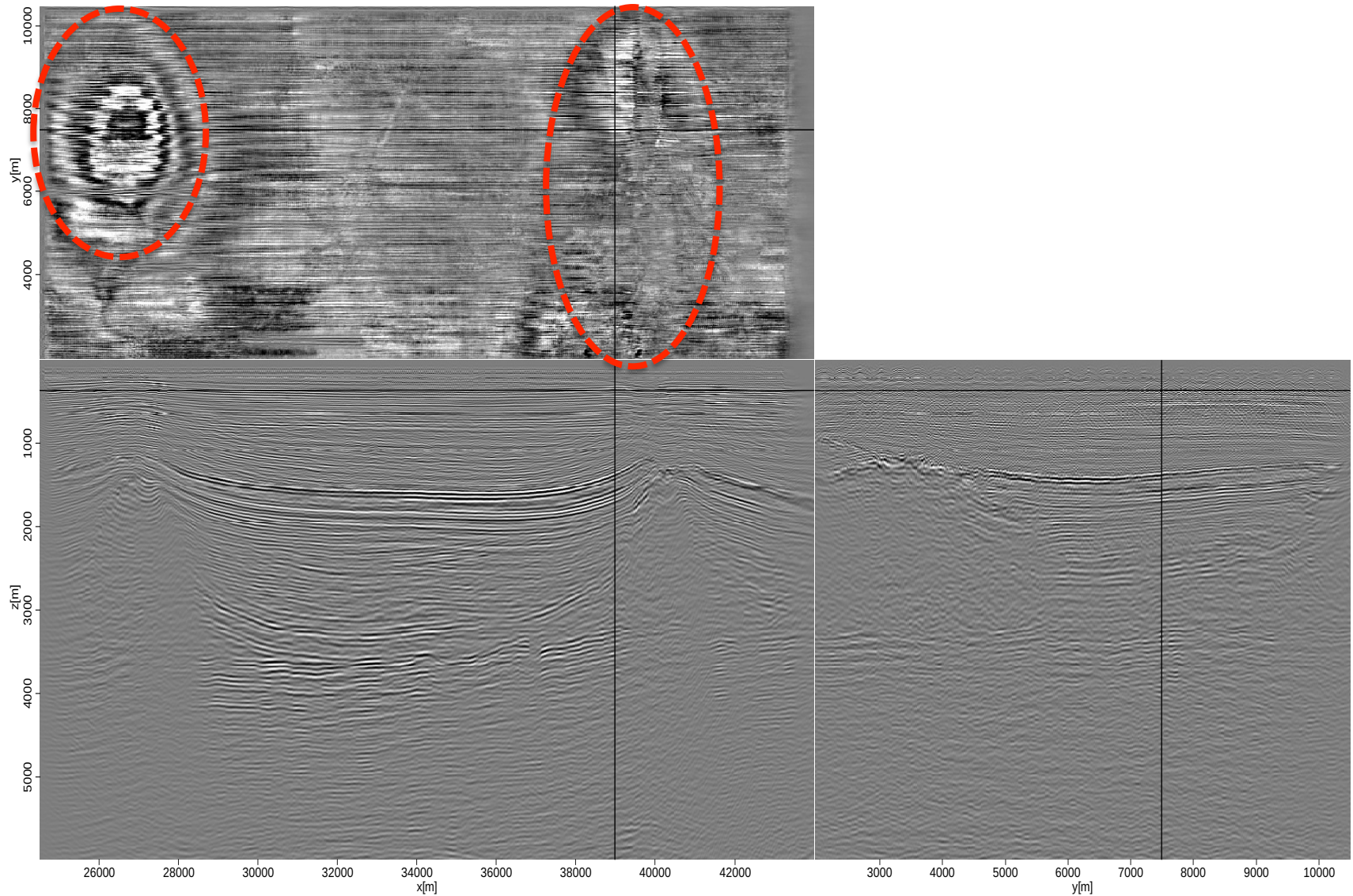
3D image **after** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



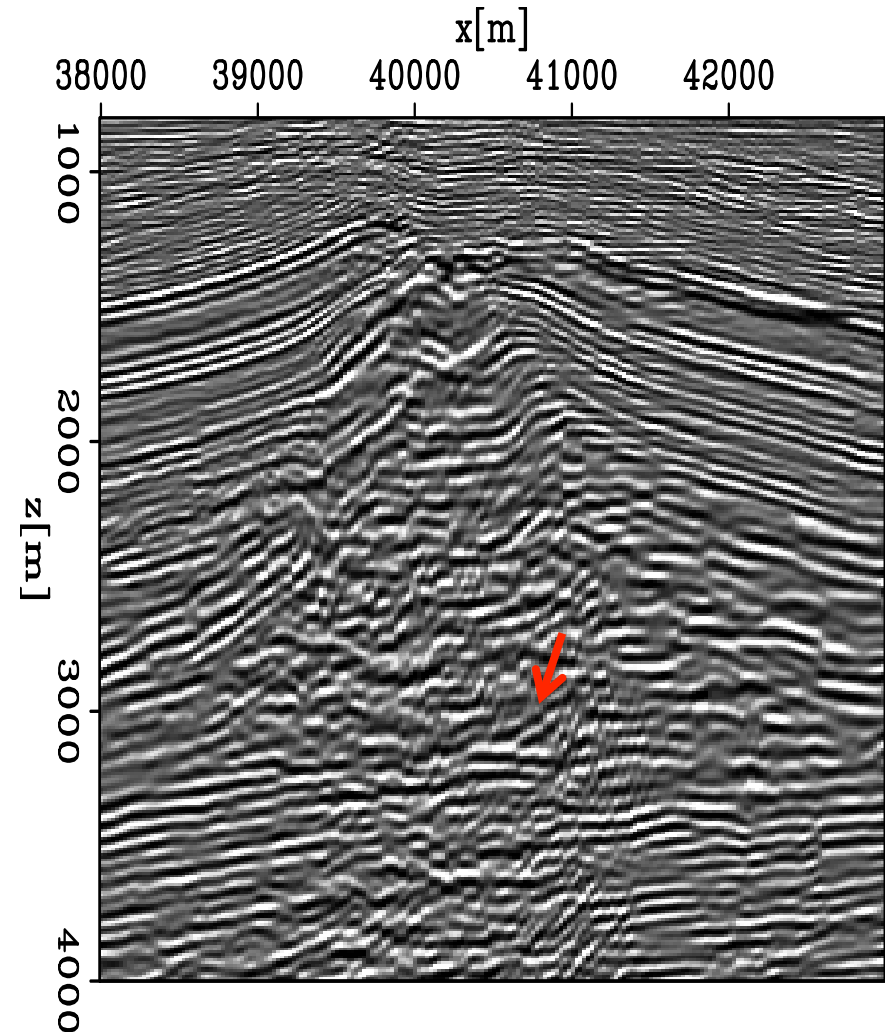
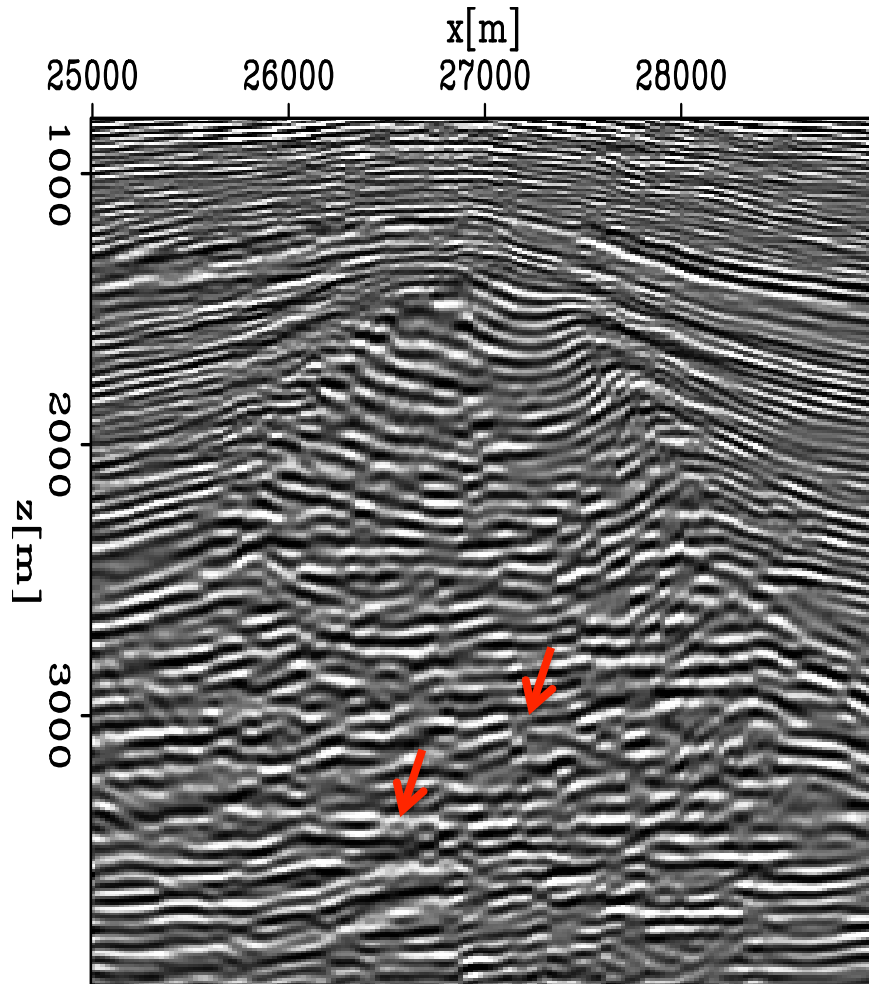
3D image **before** Q compensation

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



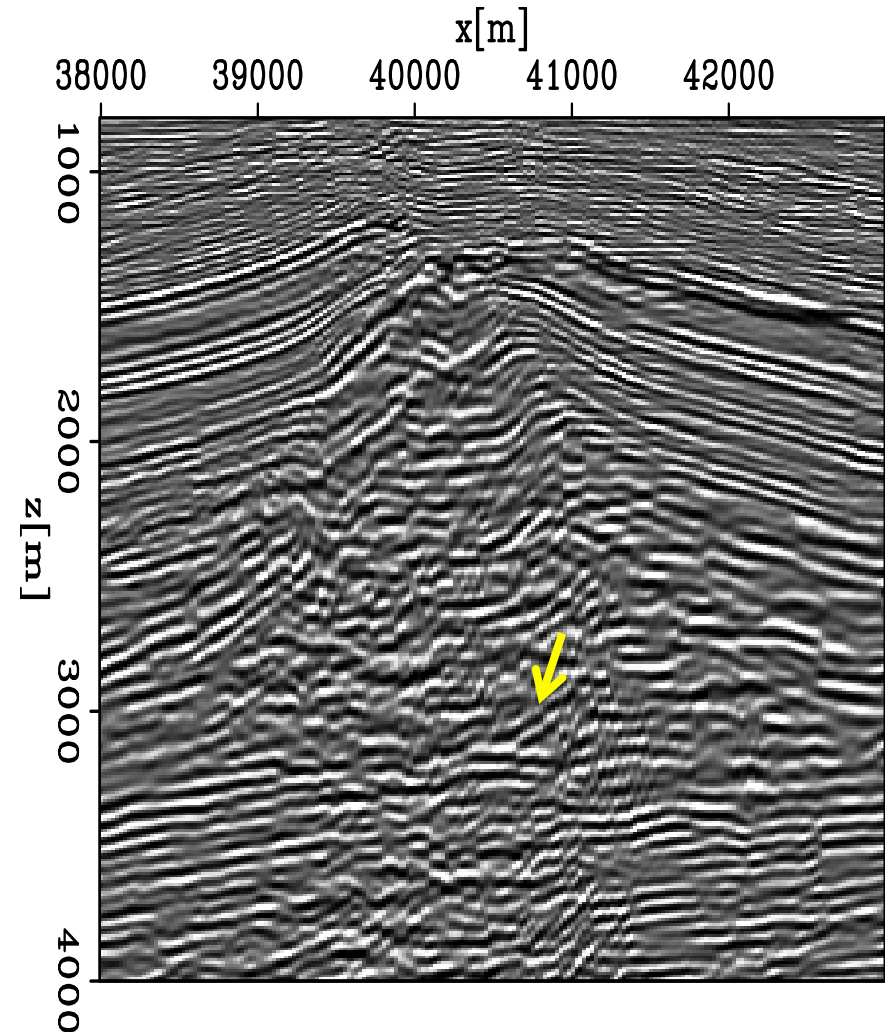
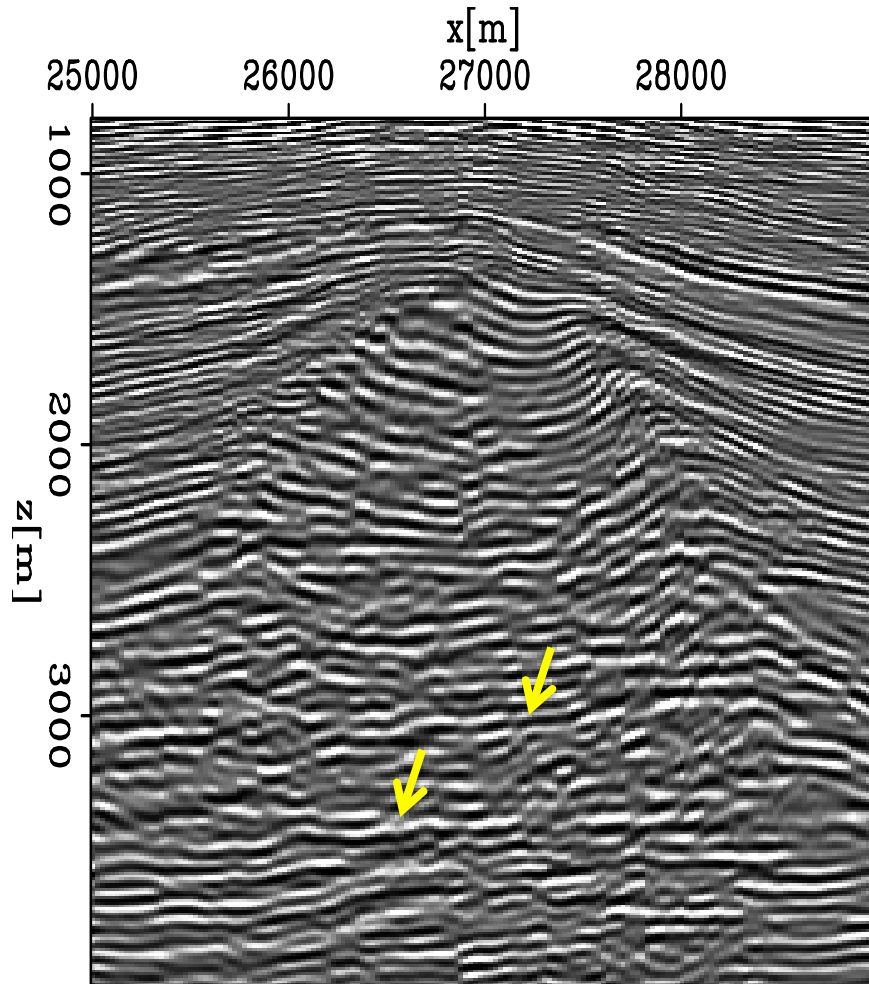
Zoomed-in image **before** Q compensation: Automatic gain control (AGC) is applied

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



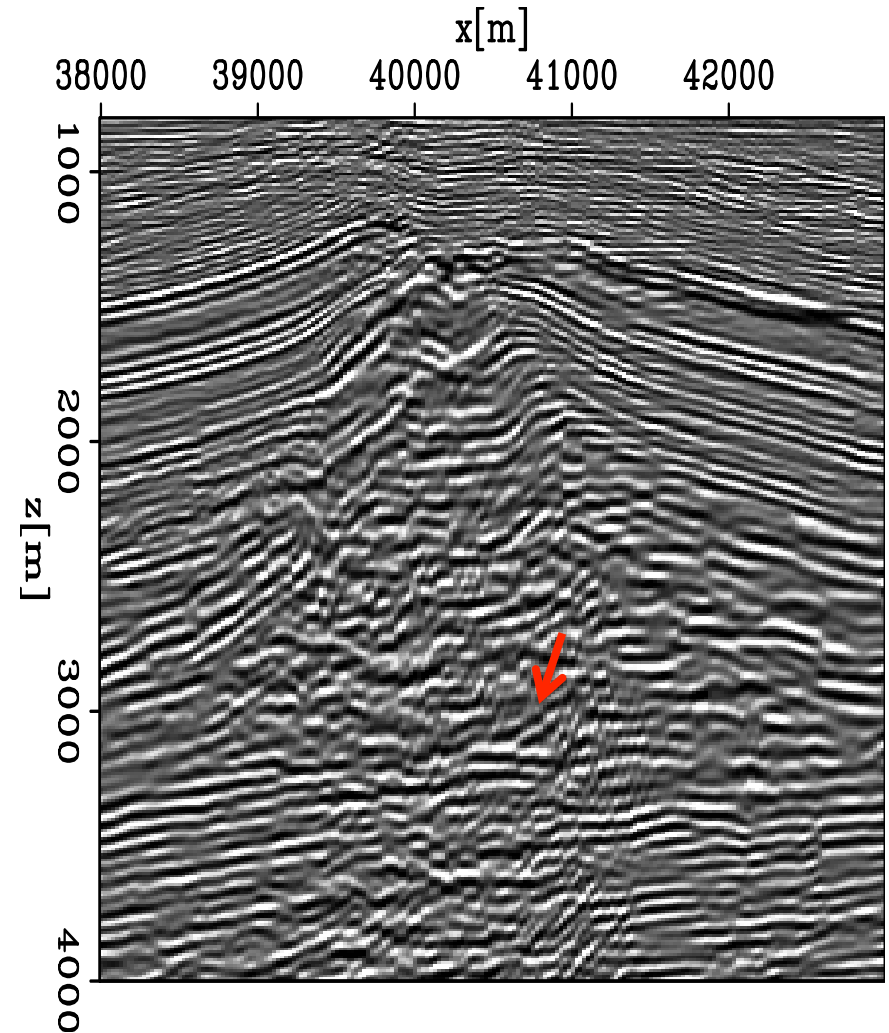
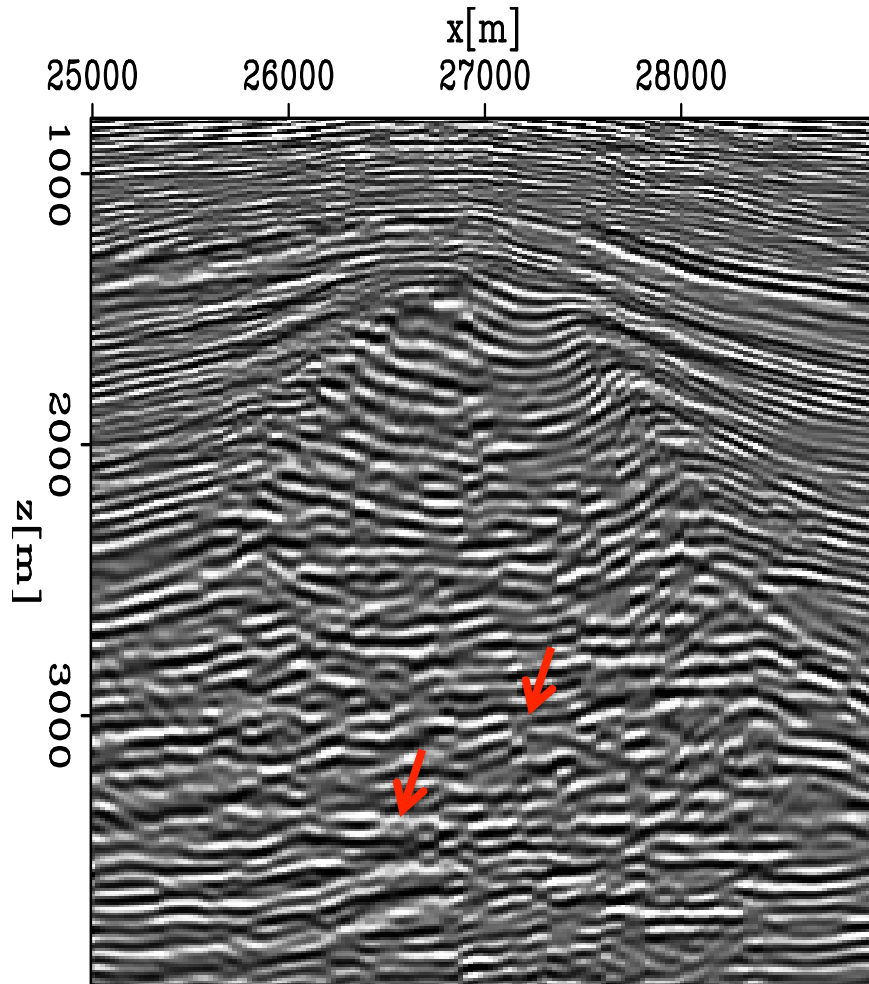
Zoomed-in image **after** Q compensation: Automatic gain control (AGC) is applied

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



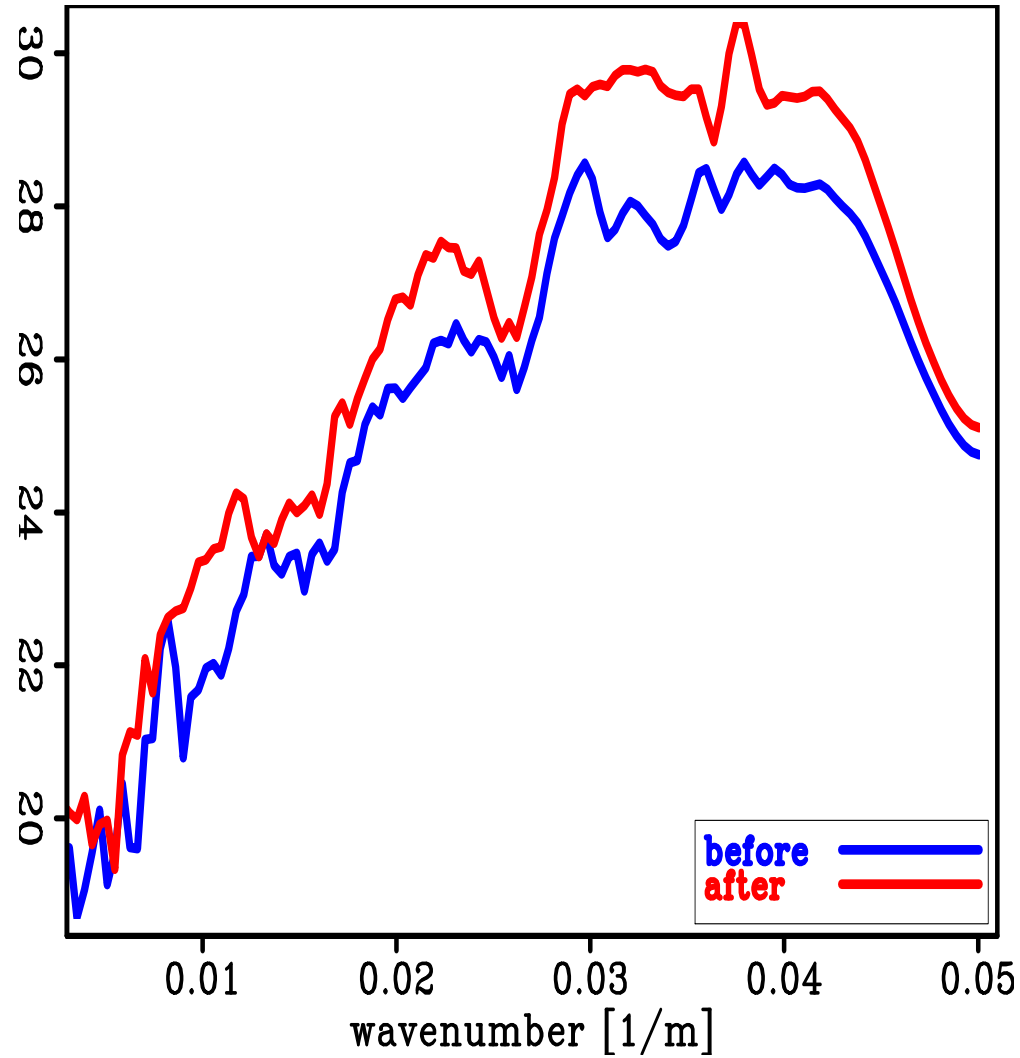
Zoomed-in image **before** Q compensation: Automatic gain control (AGC) is applied

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



3D image spectra

2D velocity estimation
2D one-way stacked WEMQA
2D one-way prestack WEMQA
3D one-way WEMVA and WEMQA



Conclusions I(壹)

- ◆ I have developed an inversion based method, WEMQA, to produce reliable Q models with two major features
 - Is performed in the image- space
 - Uses wave-equation-based Q tomography

Conclusions II(貳)

- ◆ Field application shows
 - The updated velocity shows regions around the gas and channel features, and makes the events in ADCIGs flatter.
 - The estimated Q anomalies for shallow gas and channel are consistent with Dolphin's interpretation.
 - The prestack WEMQA builds a higher resolution Q model than stacked WEMQA.

Conclusions III(叁)

- ◆ Field application shows
 - The migration compensation makes the seismic events below the anomalies clearly visible, with improved frequency content and phase coherency.
 - These improvements in image quality provide greater confidence for hydrocarbon exploration.

Acknowledgements

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ThankQ and Q?