
Random boundary for low-frequency wave propagation

Xukai Shen, Robert Clapp

SEP143 Pg 85 - 92

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Outline

1. Motivation
2. Design of random boundary for low frequency
3. Examples

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1. Motivation

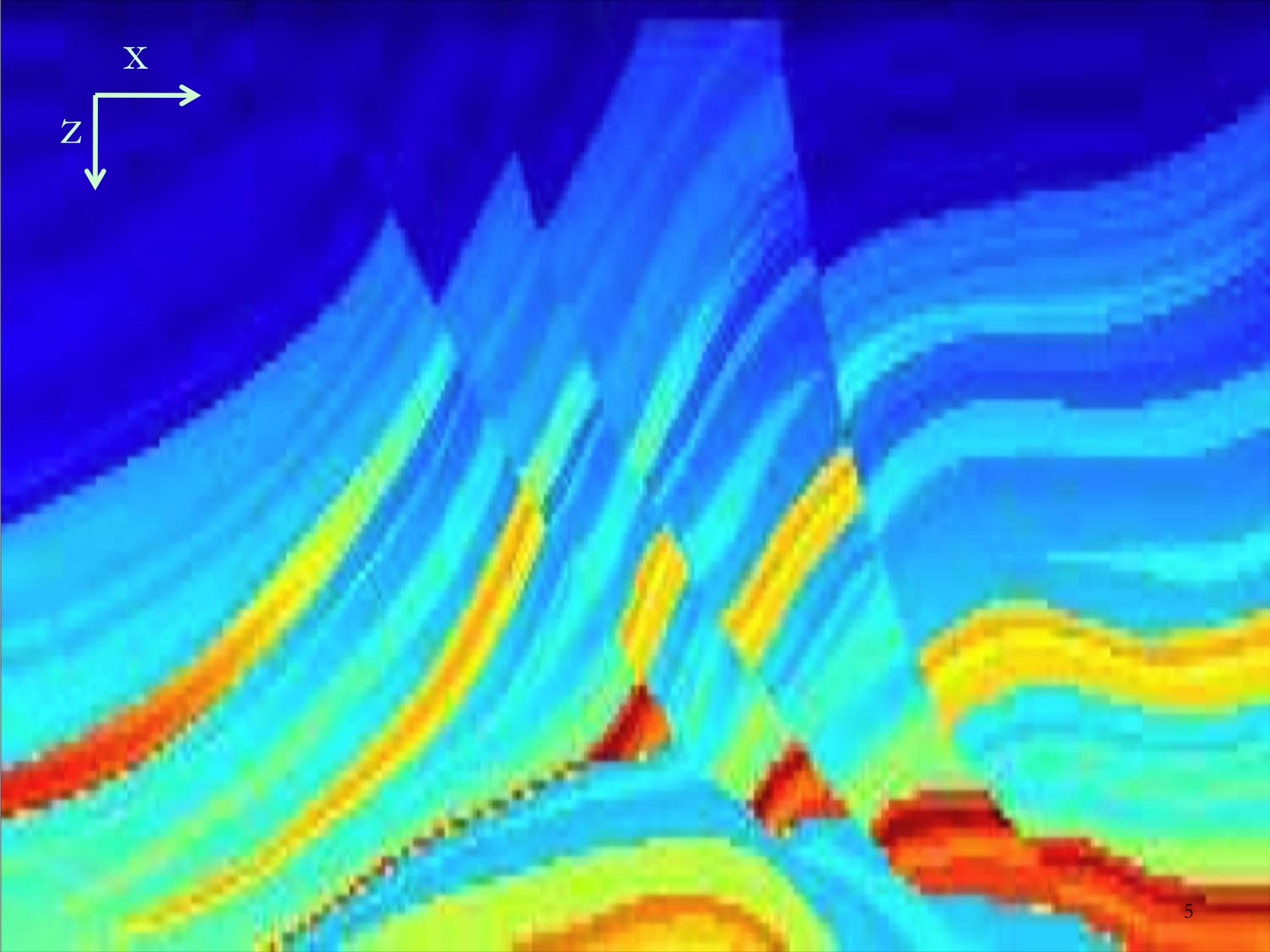
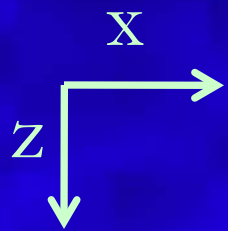
2. Design of random boundary for low frequency

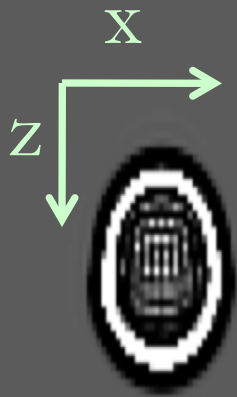
3. Examples

Reverse Time Migration Image calculation:

Source propagation , record source wavefield \mathbf{U}_s





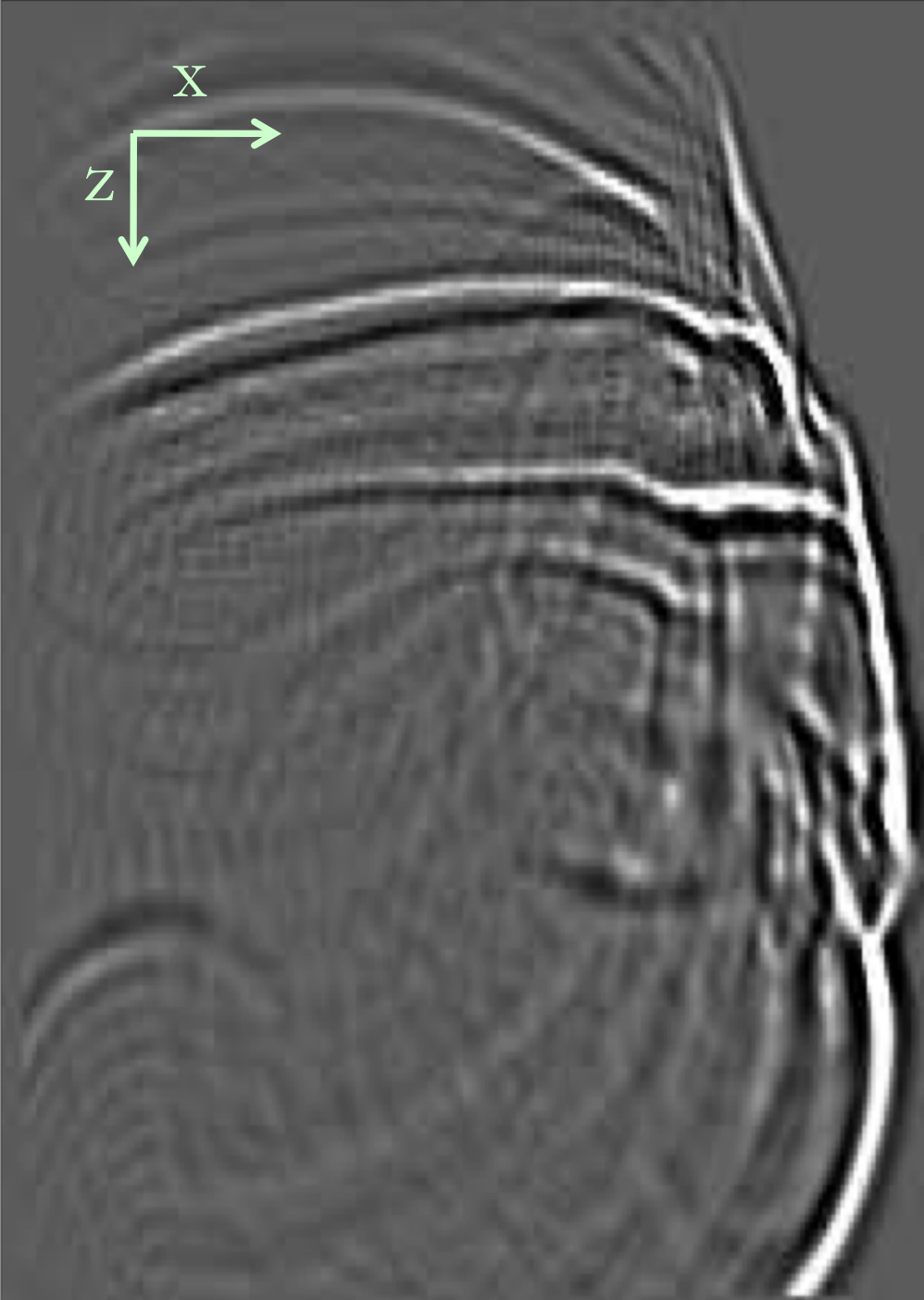
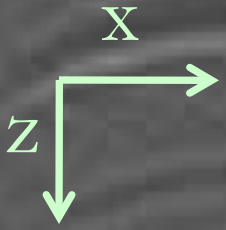


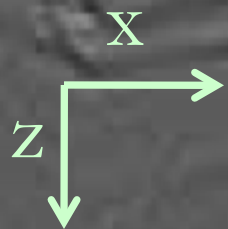
Source wavefield
 $t=0.35\text{s}$



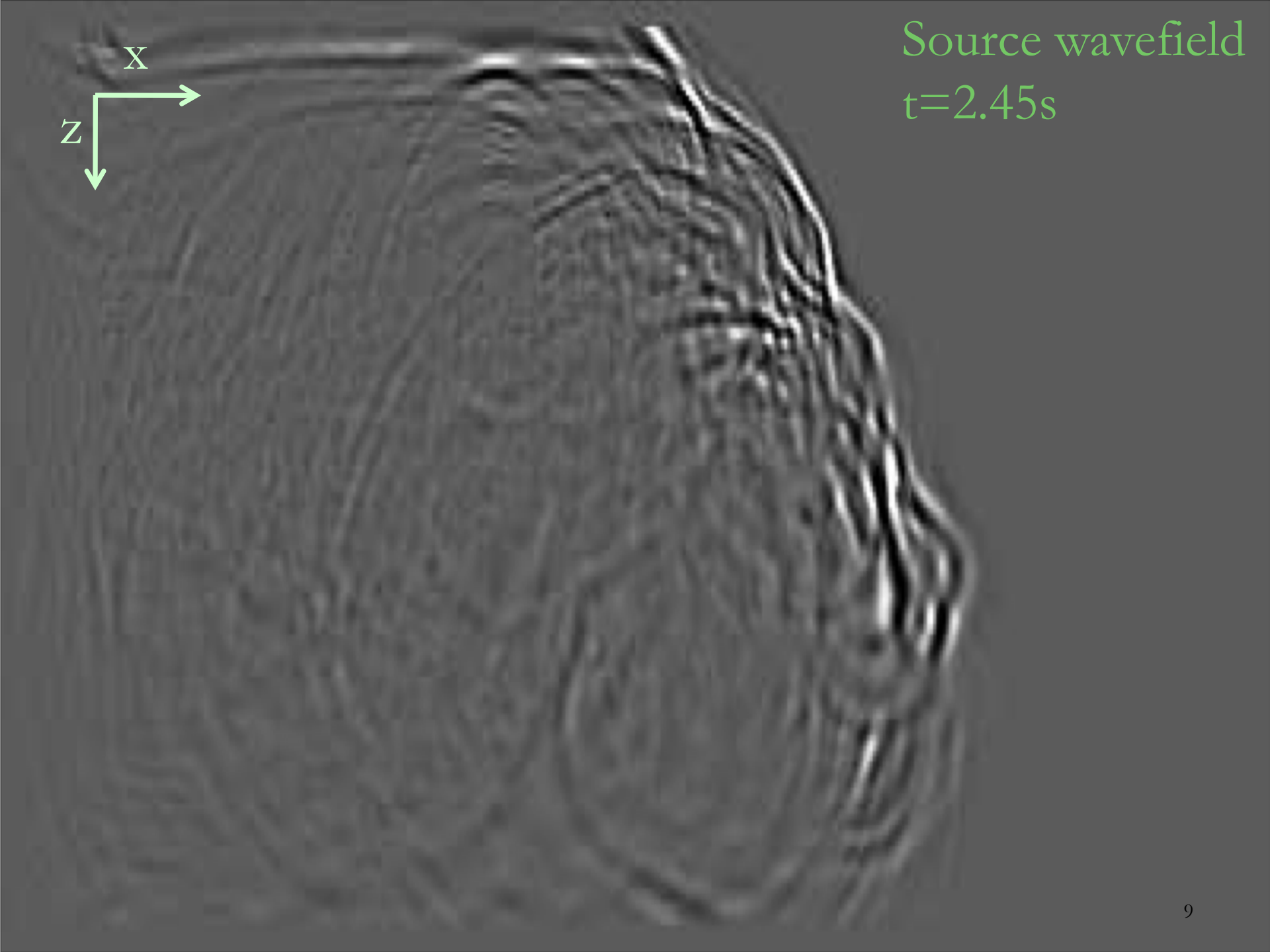
Source wavefield
 $t=1.05\text{s}$

Source wavefield
 $t=1.75\text{s}$



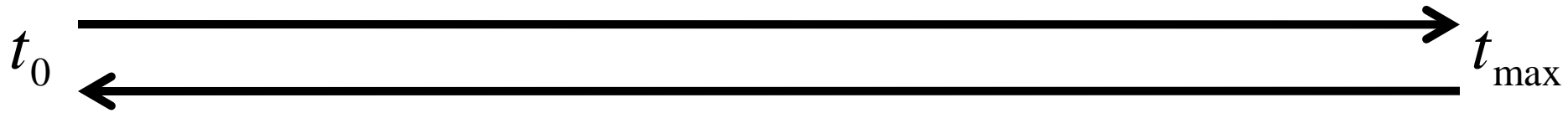


Source wavefield
 $t=2.45\text{s}$

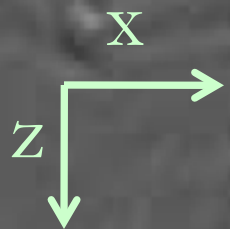


Reverse Time Migration Image calculation:

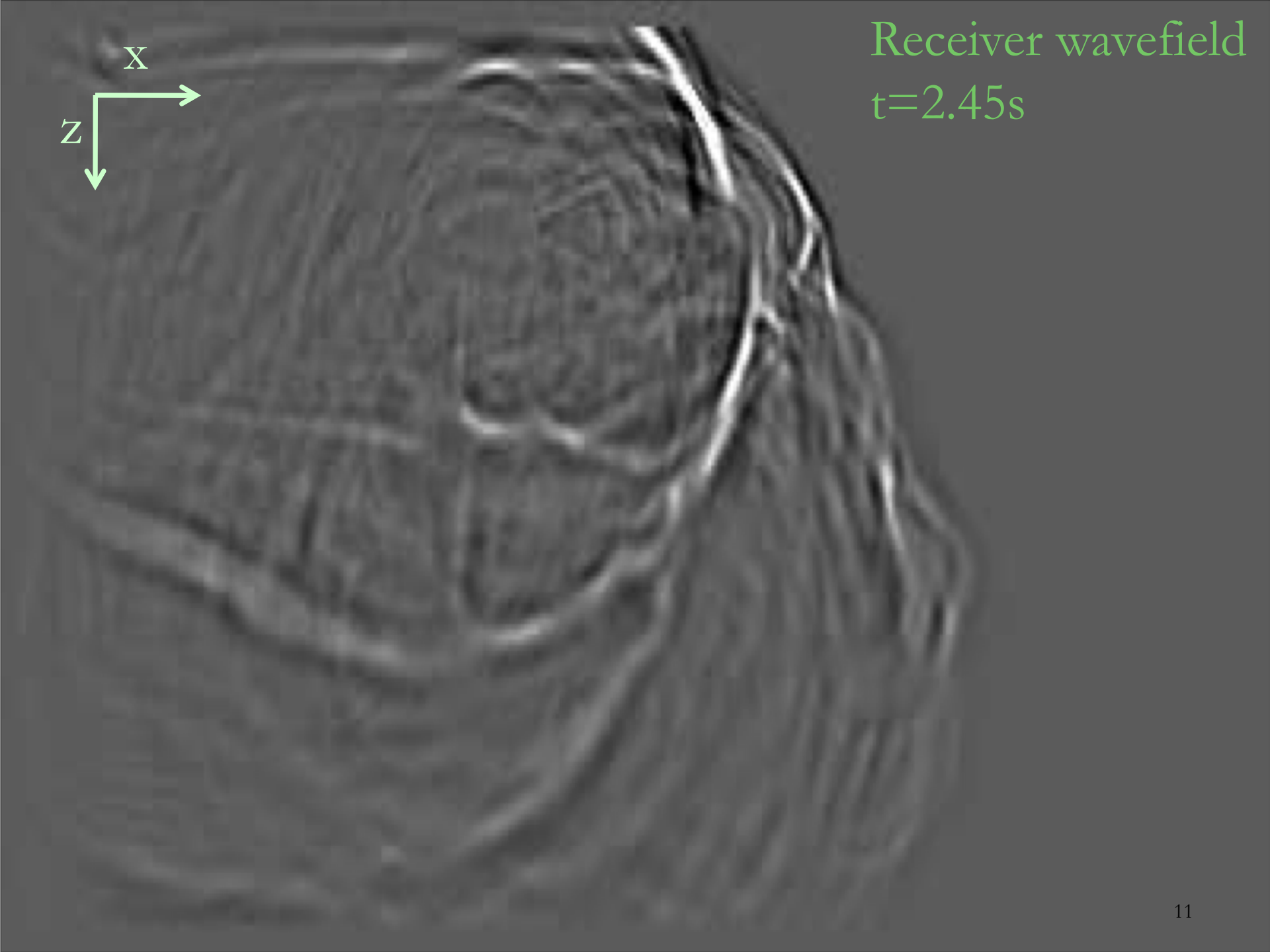
Source propagation , record source wavefield \mathbf{U}_s

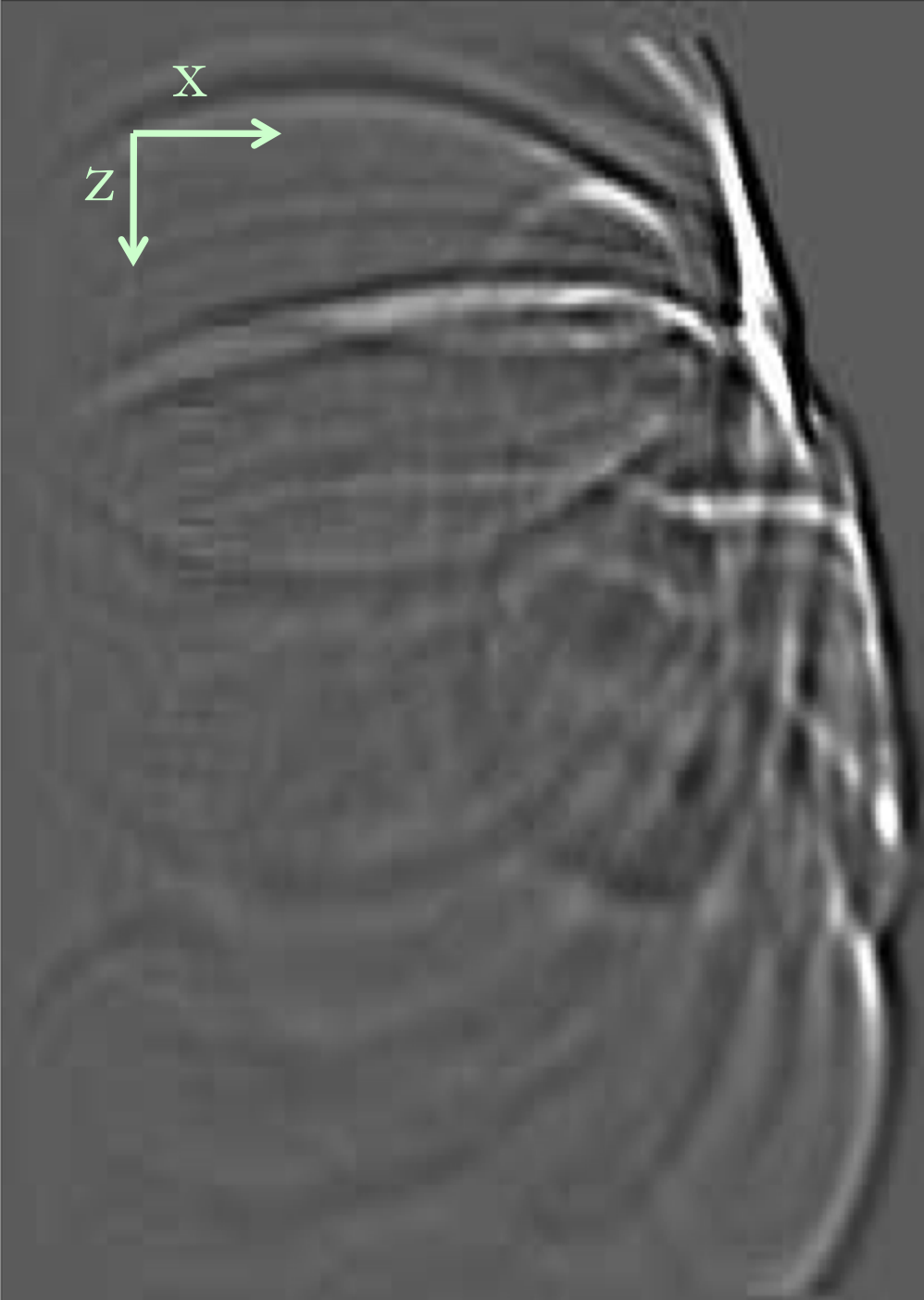


Data propagation, record receiver wavefield \mathbf{U}_r , correlate with \mathbf{U}_s



Receiver wavefield
 $t=2.45\text{s}$





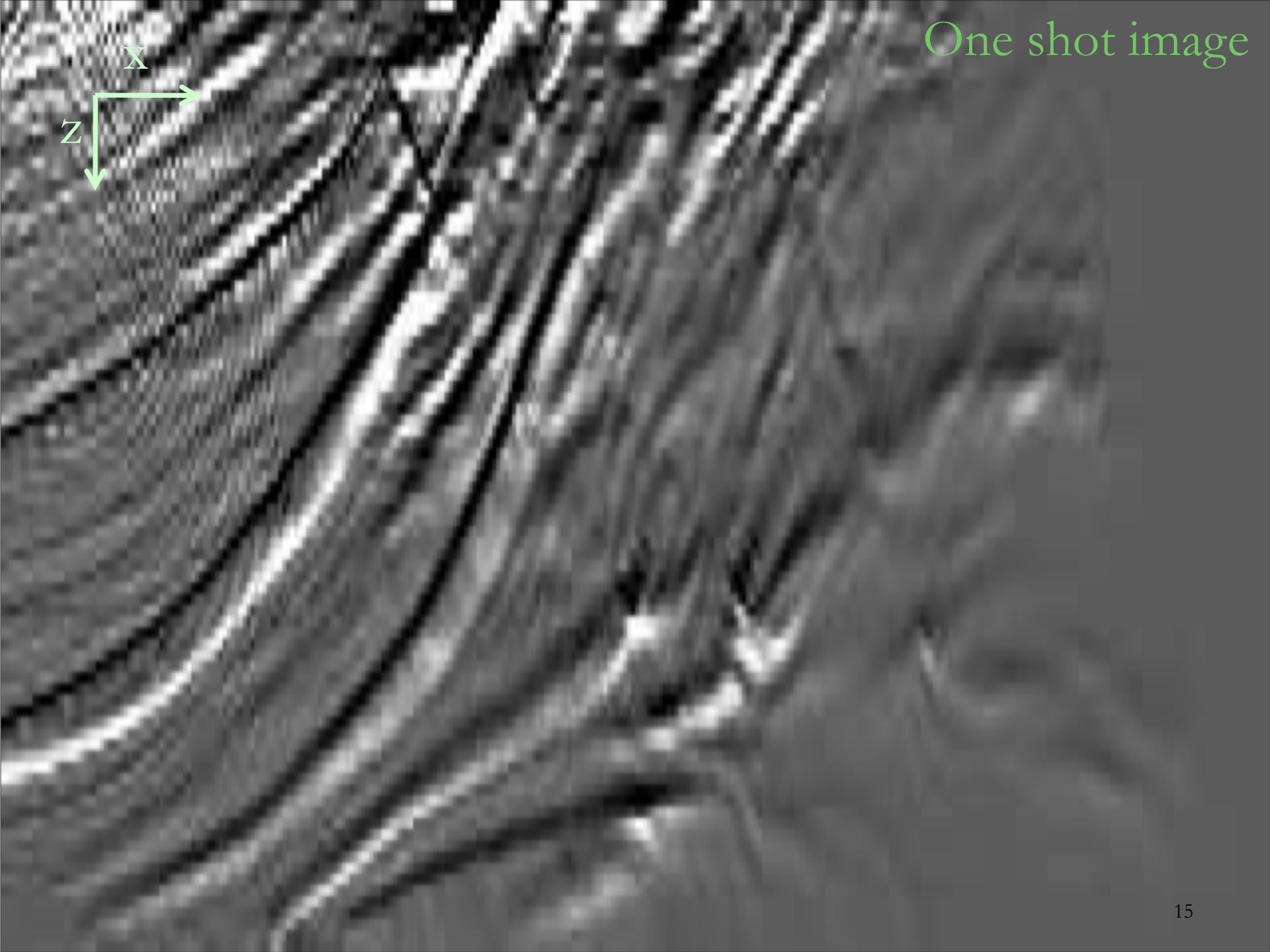
Receiver wavefield
 $t=1.75\text{s}$



Receiver wavefield
 $t=1.05\text{s}$



Receiver wavefield
 $t=0.35\text{s}$



One shot image

Image:

$$\mathbf{g}(\mathbf{x}) = \mathbf{U}_s(\mathbf{x}, t) * \mathbf{U}_r(\mathbf{x}, t)$$

\mathbf{U}_r Data residual wavefield

\mathbf{U}_s Source wavefield

\mathbf{x} Spatial location (x, y, z)

Image: $\mathbf{g}(\mathbf{x}) = \mathbf{U}_s(\mathbf{x}, t) * \mathbf{U}_r(\mathbf{x}, t)$

Conventional:

\mathbf{U}_r Data residual wavefield

\mathbf{U}_s Source wavefield

\mathbf{x} Spatial location (x, y, z)

Save at least one wavefield

e.g. $n_x * n_y * n_z * n_t = 500 * 500 * 500 * 500 \sim 250\text{G}$

Image: $\mathbf{g}(\mathbf{x}) = \mathbf{U}_s(\mathbf{x}, t) * \mathbf{U}_r(\mathbf{x}, t)$

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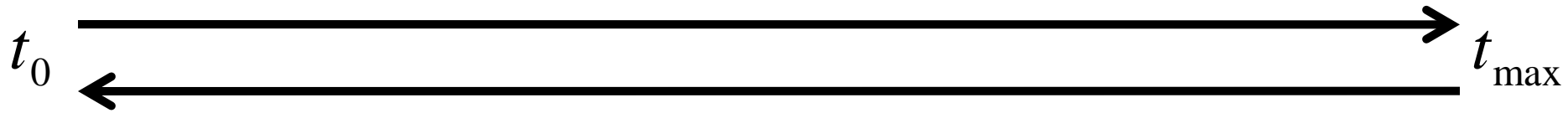
e.g. $n_x * n_y * n_z * n_t = 500 * 500 * 500 * 500 \sim 250\text{G}$

Write wavefield to disk

Save everything in memory by avoiding
saving wavefield movie!!!

Image calculation :

Source propagation , record source wavefield \mathbf{U}_s

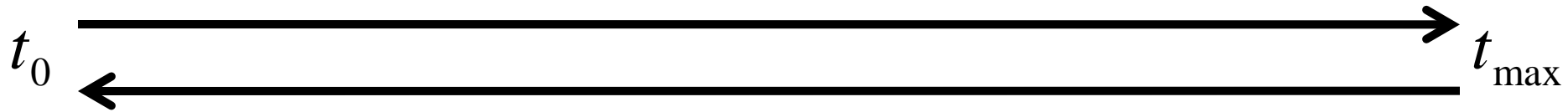


Data propagation, record receiver wavefield \mathbf{U}_r , correlate with \mathbf{U}_s

Image calculation with random

boundary:

Source propagation , record last 2 slices of \mathbf{U}_s



Data and source propagation, correlate \mathbf{U}_s and \mathbf{U}_r

Image: $\mathbf{g}(\mathbf{x}) = \mathbf{U}_s(\mathbf{x}, t) * \mathbf{U}_r(\mathbf{x}, t)$

\mathbf{U}_r Data residual wavefield

Random boundary condition:

\mathbf{U}_s Source wavefield

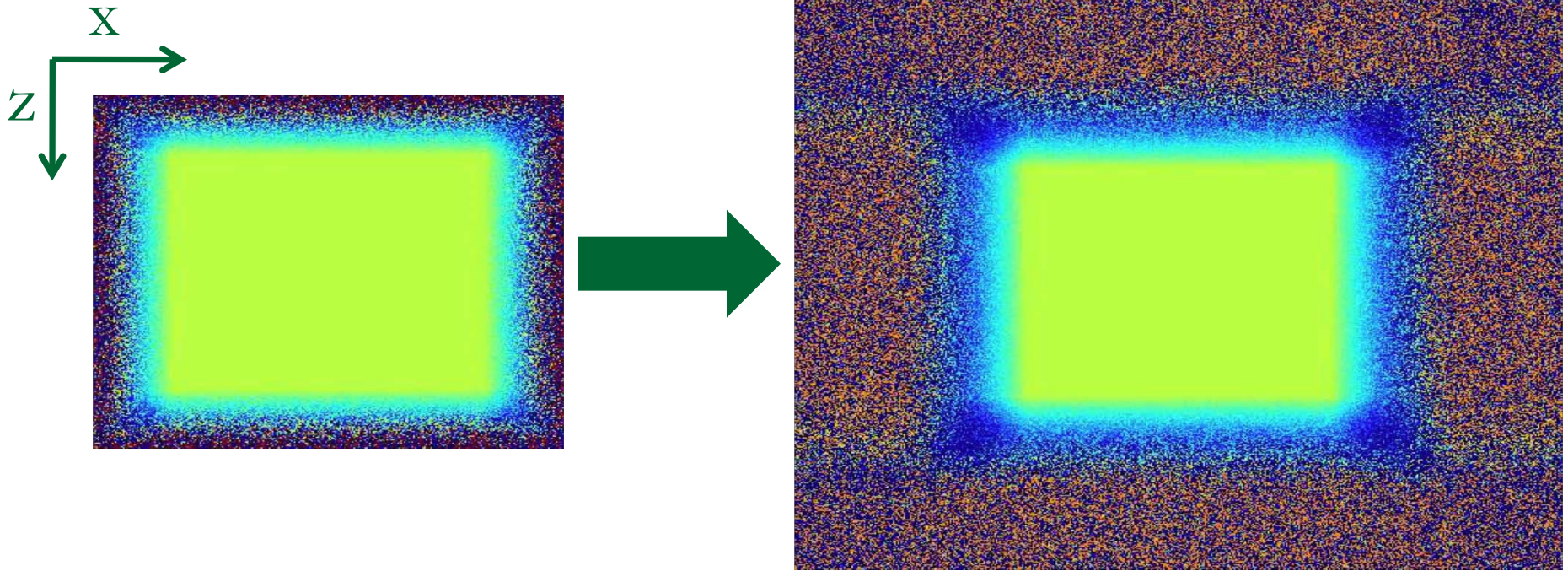
\mathbf{x} Spatial location (x, y, z)

No need to save whole wavefield

e.g. $n_x * n_y * n_z * 2 = 500 * 500 * 500 * 2 \sim 1.0\text{G}$

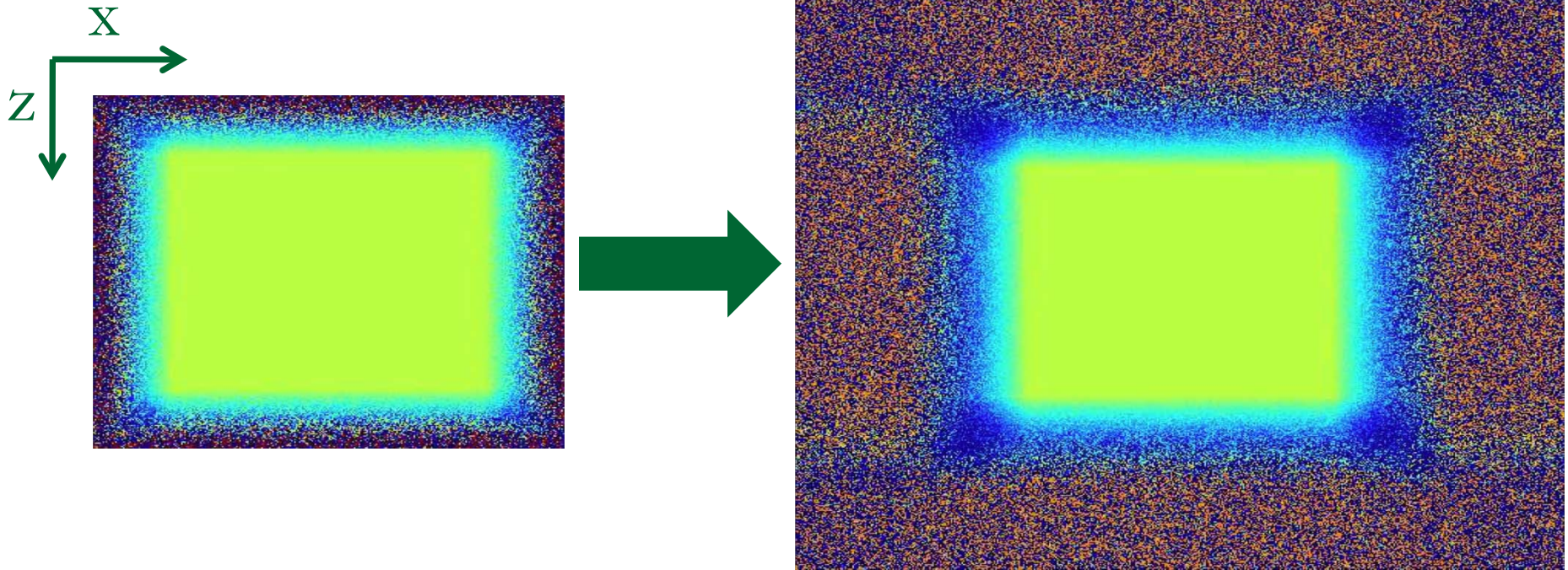
How to design random boundary for low frequency wave

How to design random boundary for low frequency wave



How to design random boundary for low frequency wave

Big increase in computation and memory



How to design **economic** random boundary for low frequency wave

RTM





Random anomalies used for RTM is too small compared to the dominant wavelength in FWI

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1. Motivation
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3. Examples

Use bigger anomaly grains in random boundary

Use bigger anomaly grains in random boundary

1. Grain size

2. Grain shape

Use bigger anomaly grains in random boundary

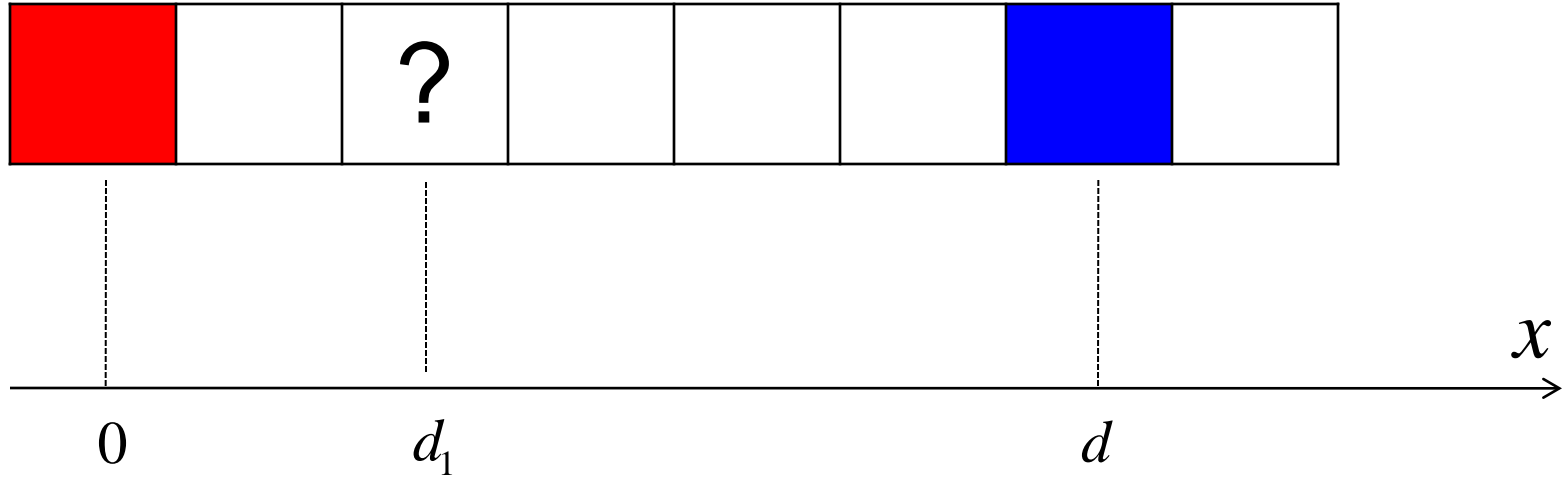
1. Grain size

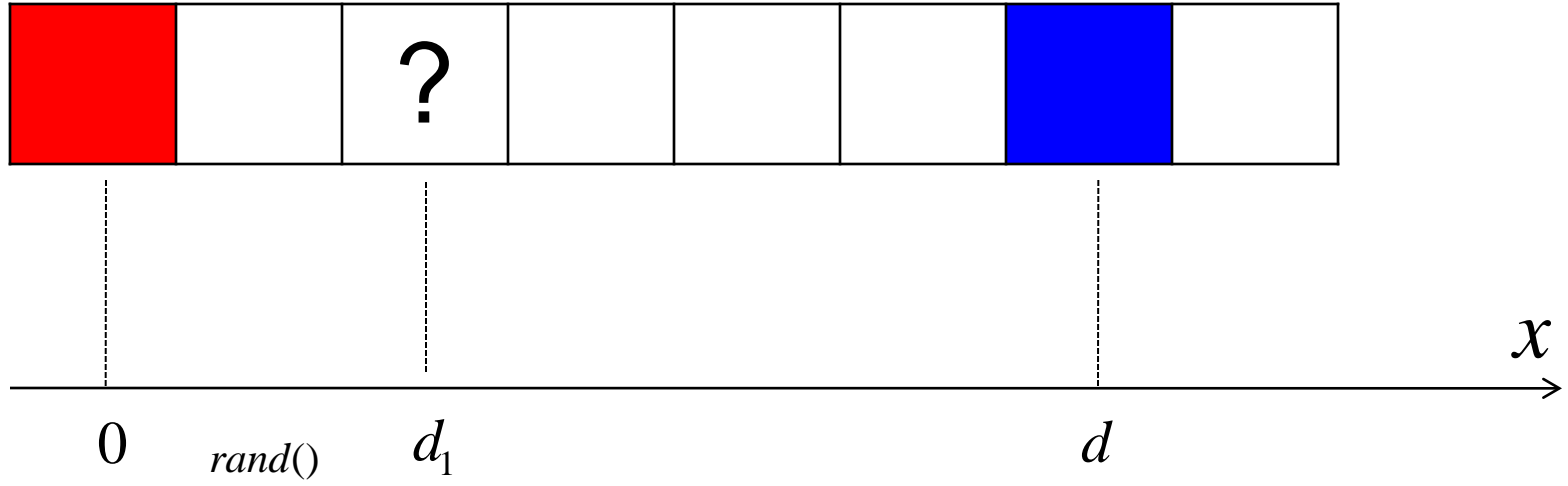
2. Grain shape


Cubic

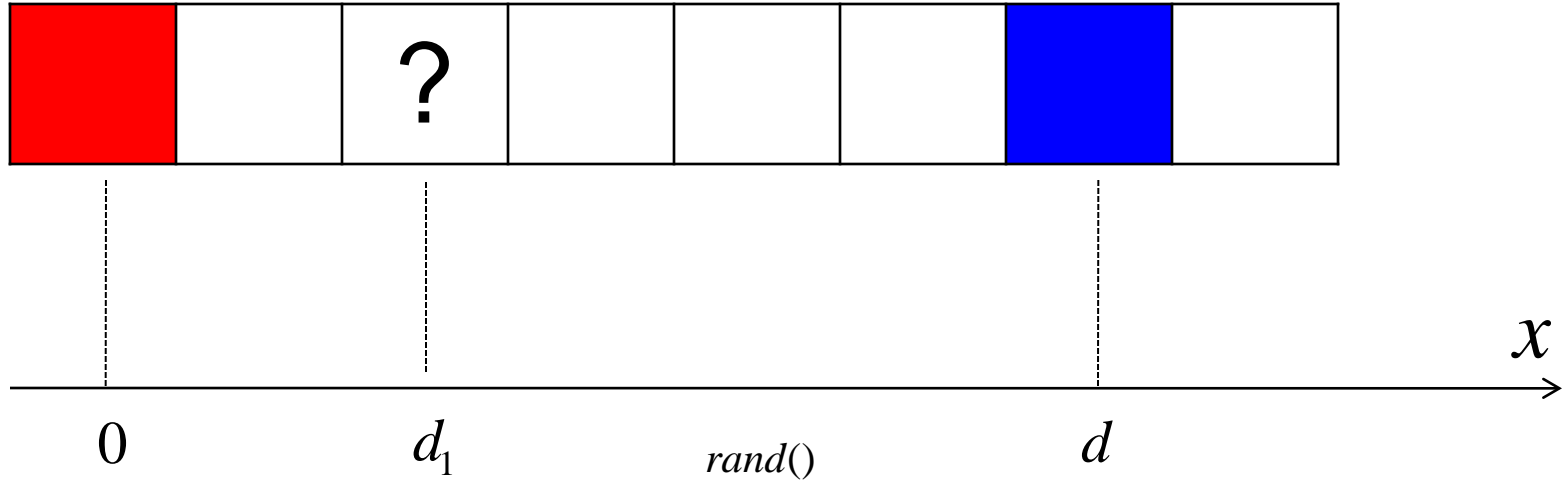
Random








? = 



$? =$ 

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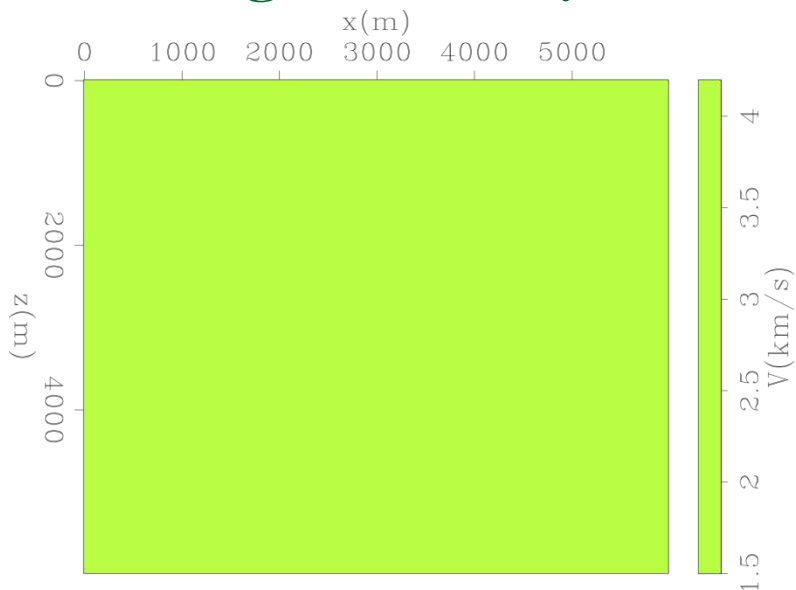
Modeling: Parameters

Full velocity mode: $300 \times 300 \times 300$ in grids
20m grid spacing in all directions

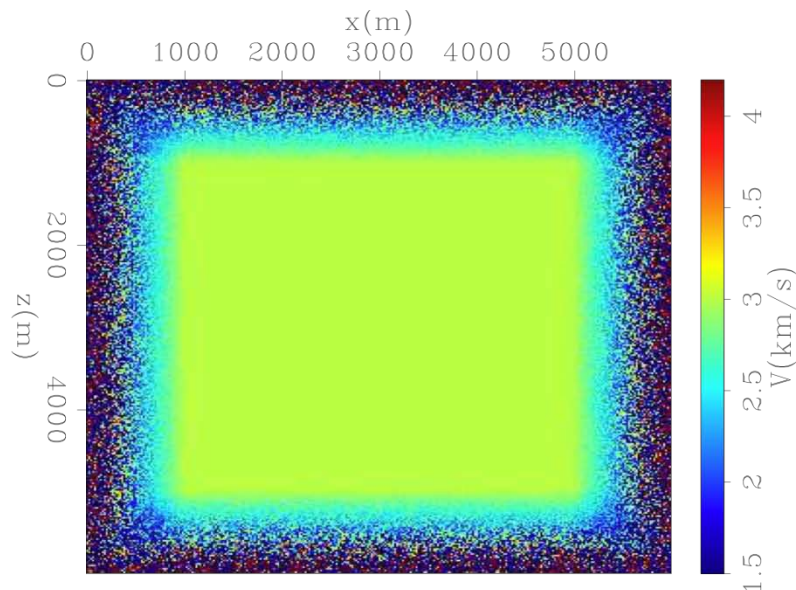
Boundary region: 50 grids on each side

Velocity: mean 3km/s, min 1.5km/s, max 4.2km/s

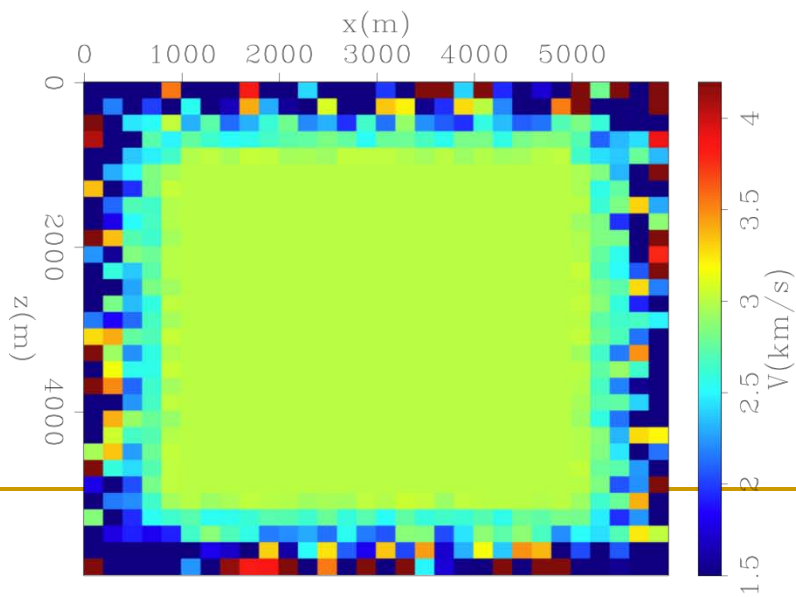
Modeling: Velocity



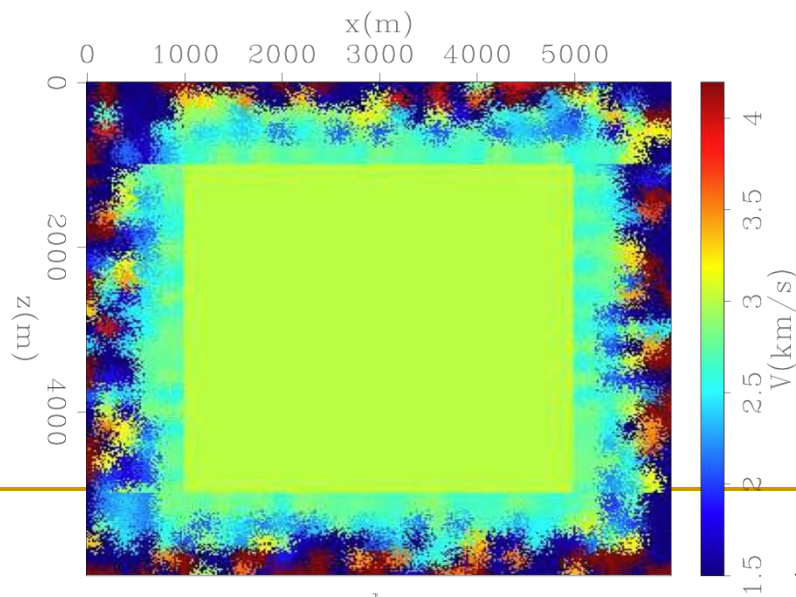
a



b

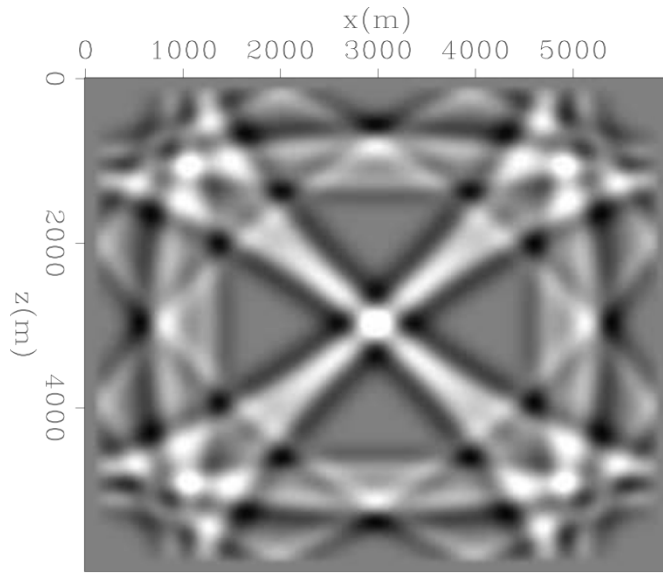


c

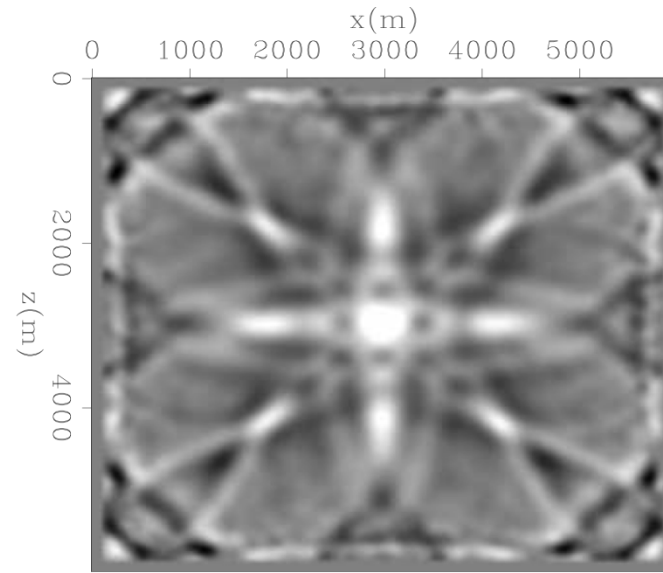


d

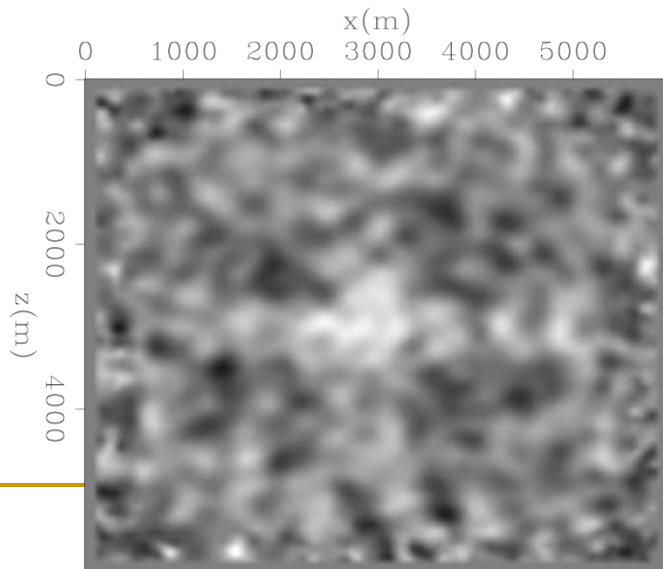
Modeling: Low frequency (6Hz peak)



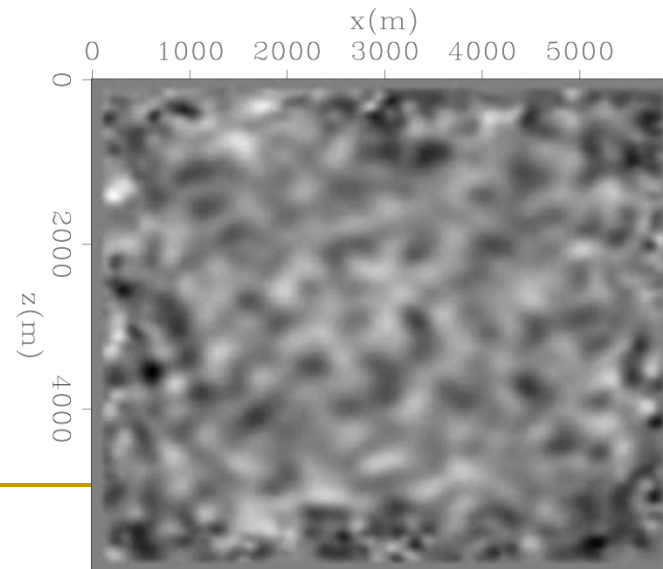
a



b

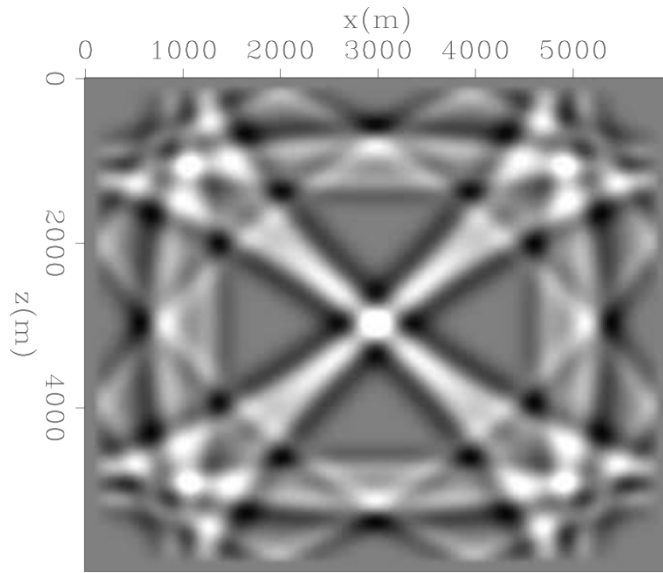


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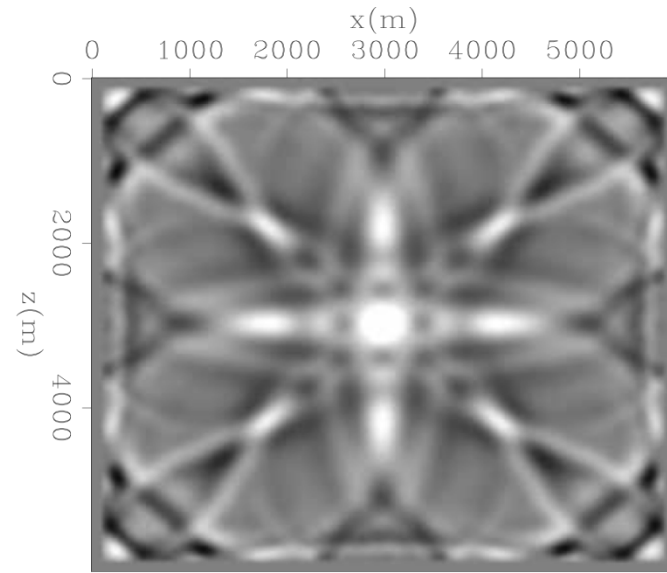


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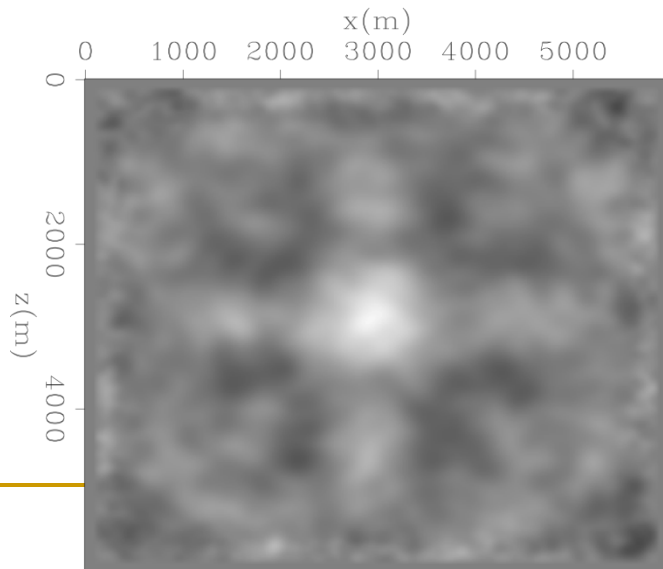
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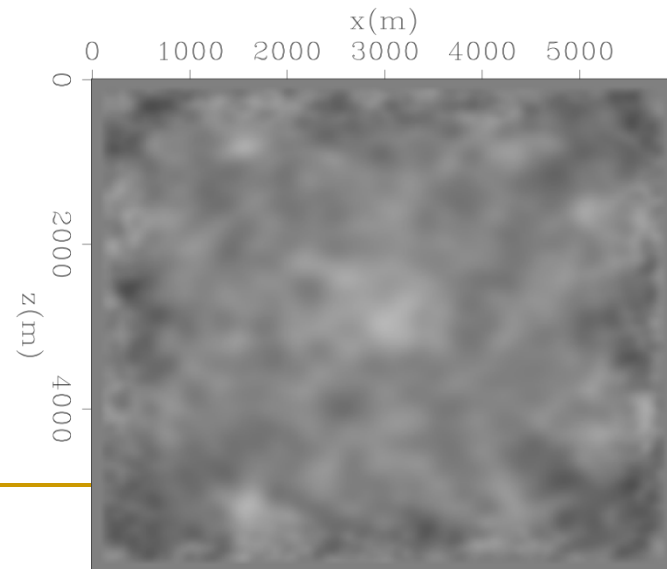
a



b

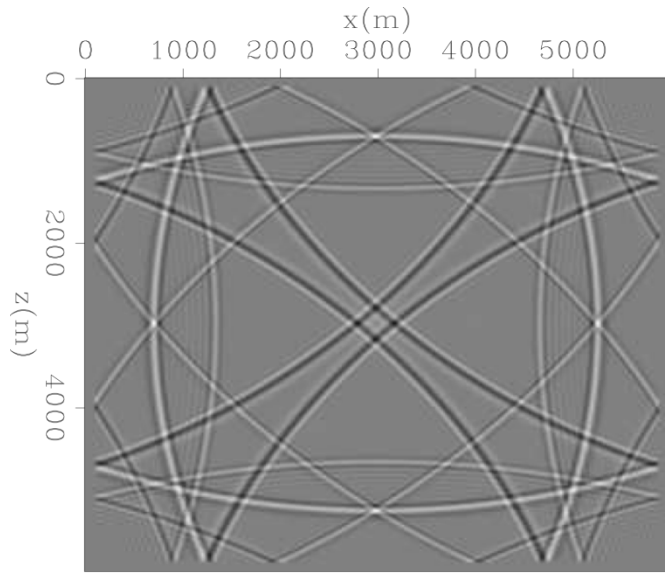


c

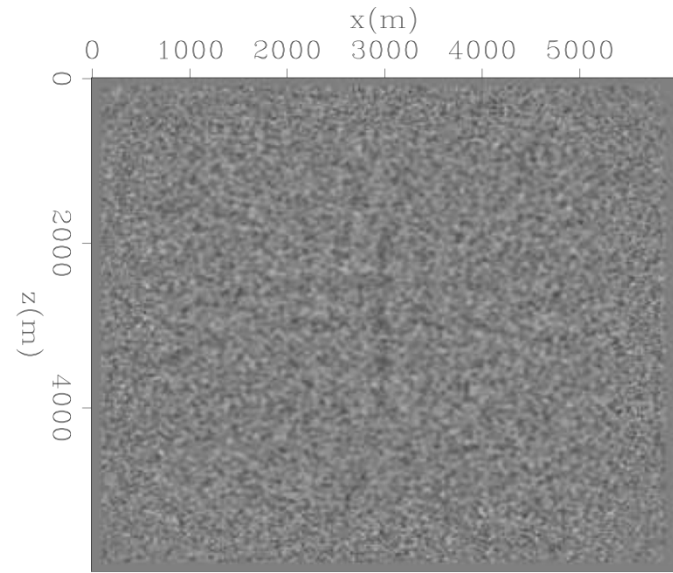


d

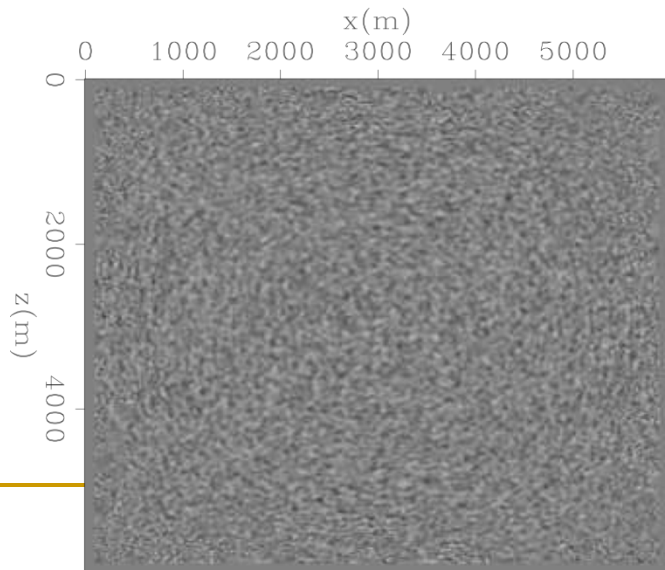
Modeling: Broadband (25Hz peak)



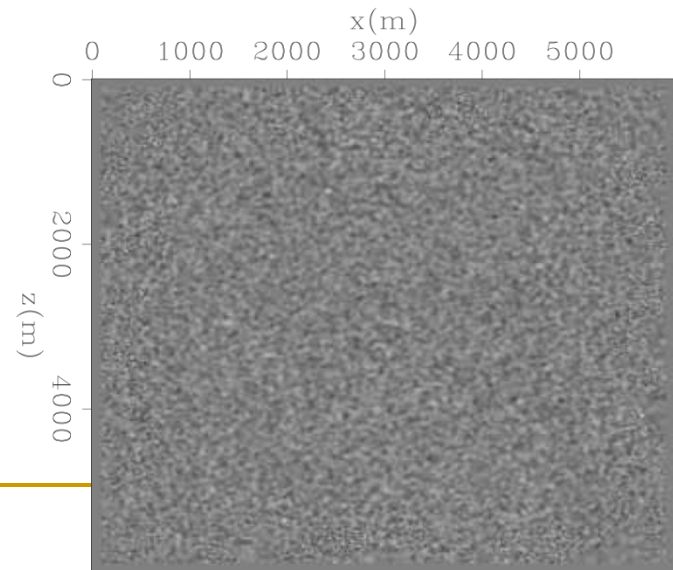
a



b

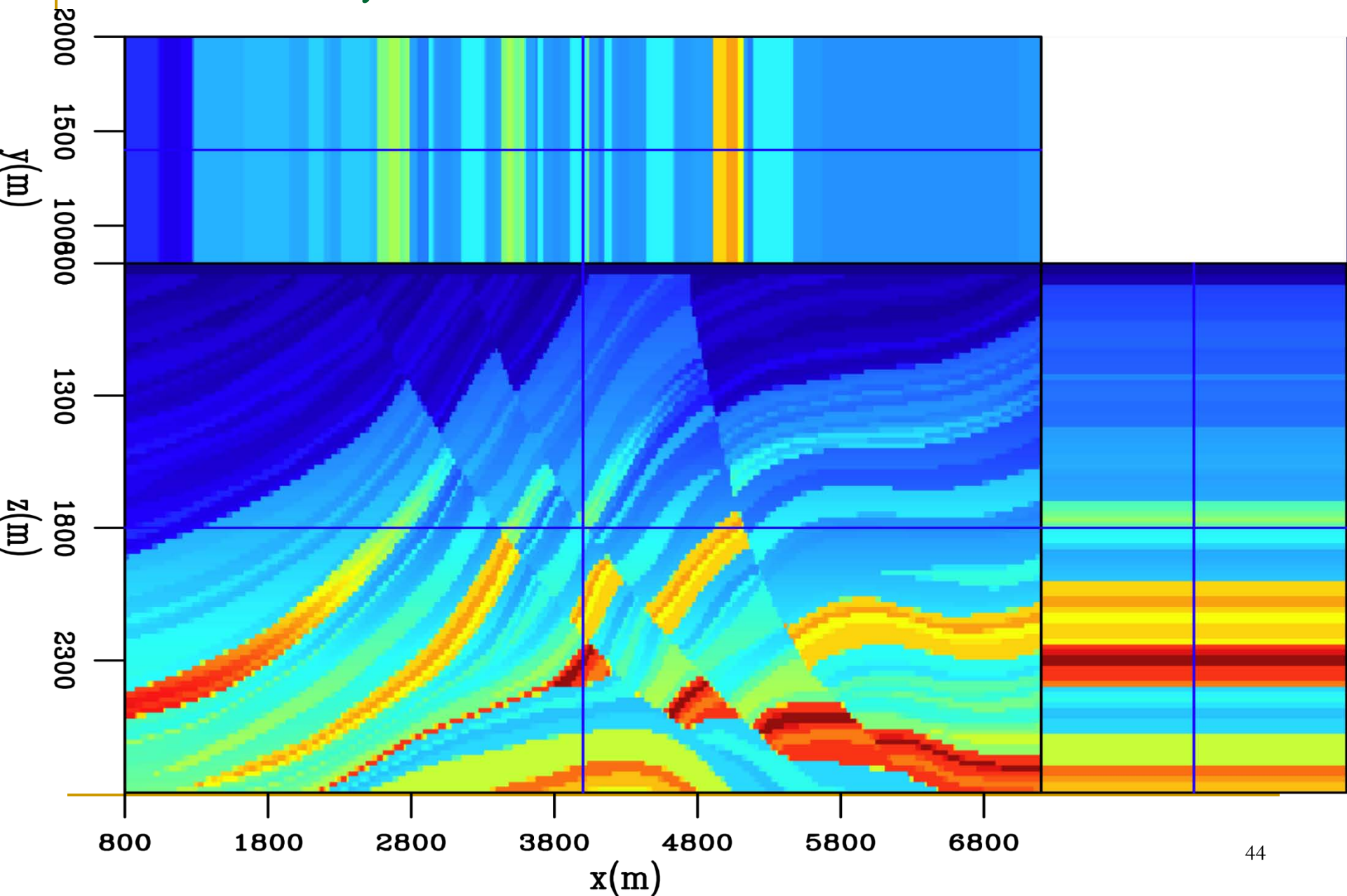


c

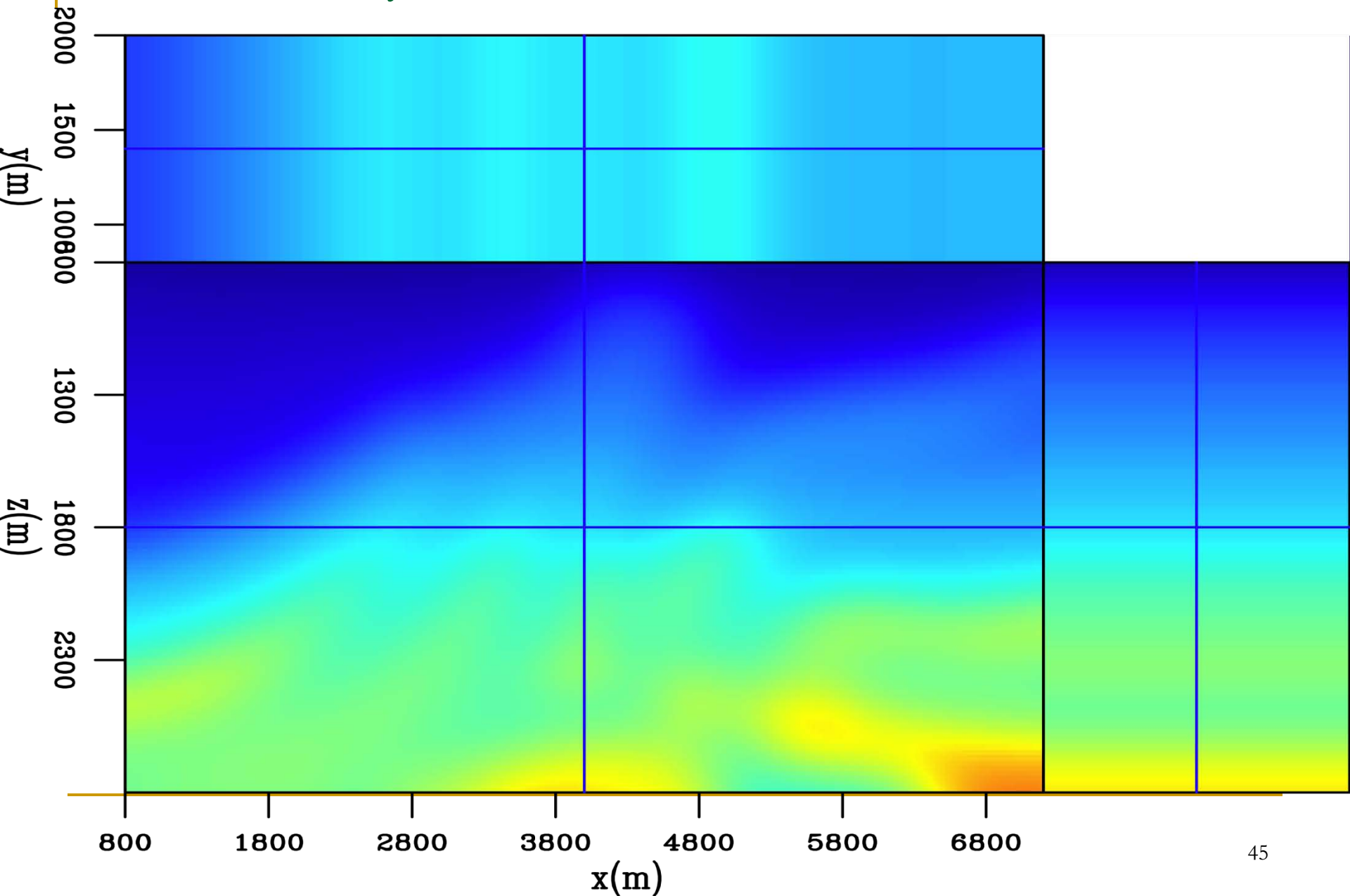


d

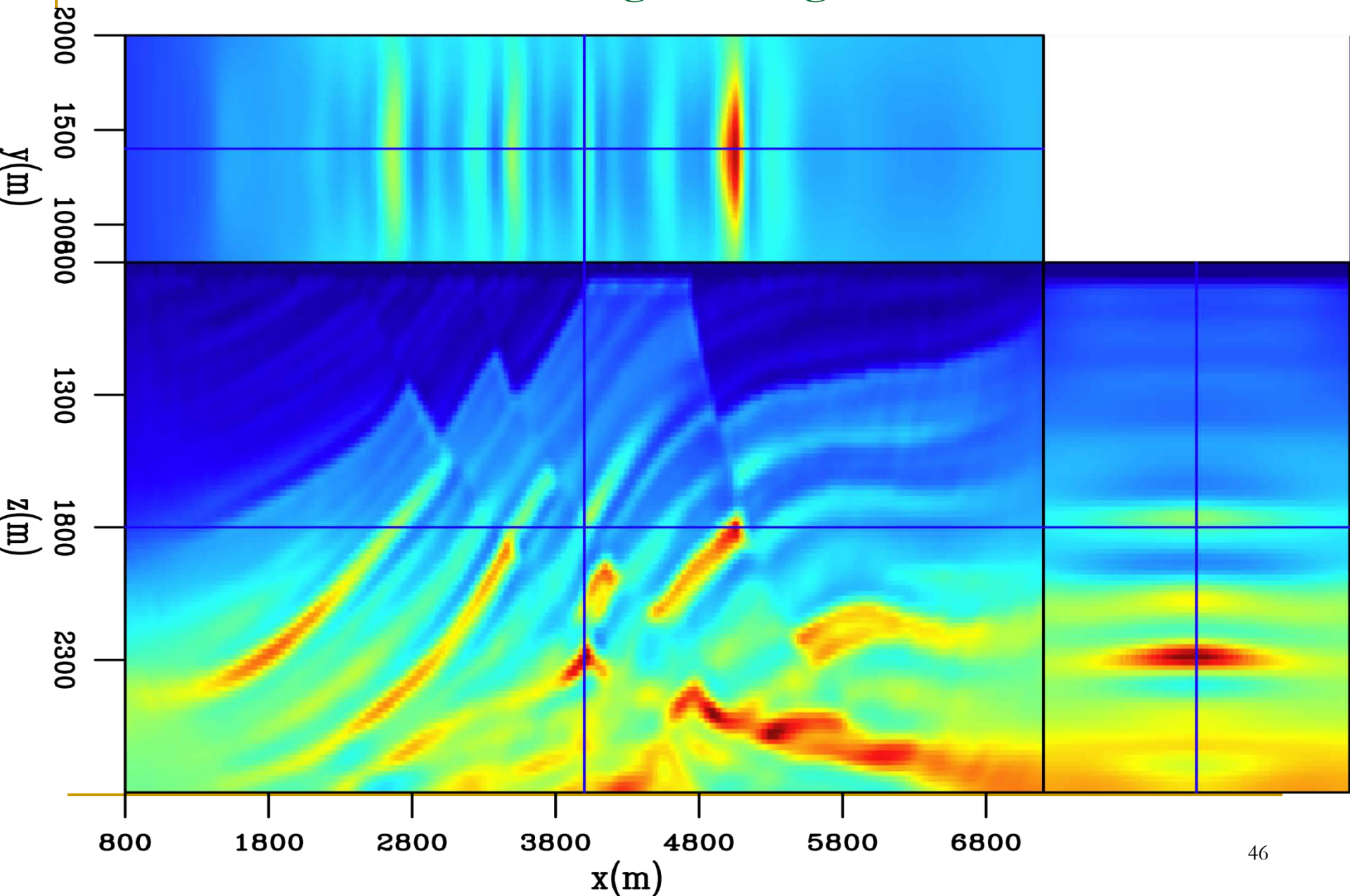
True velocity



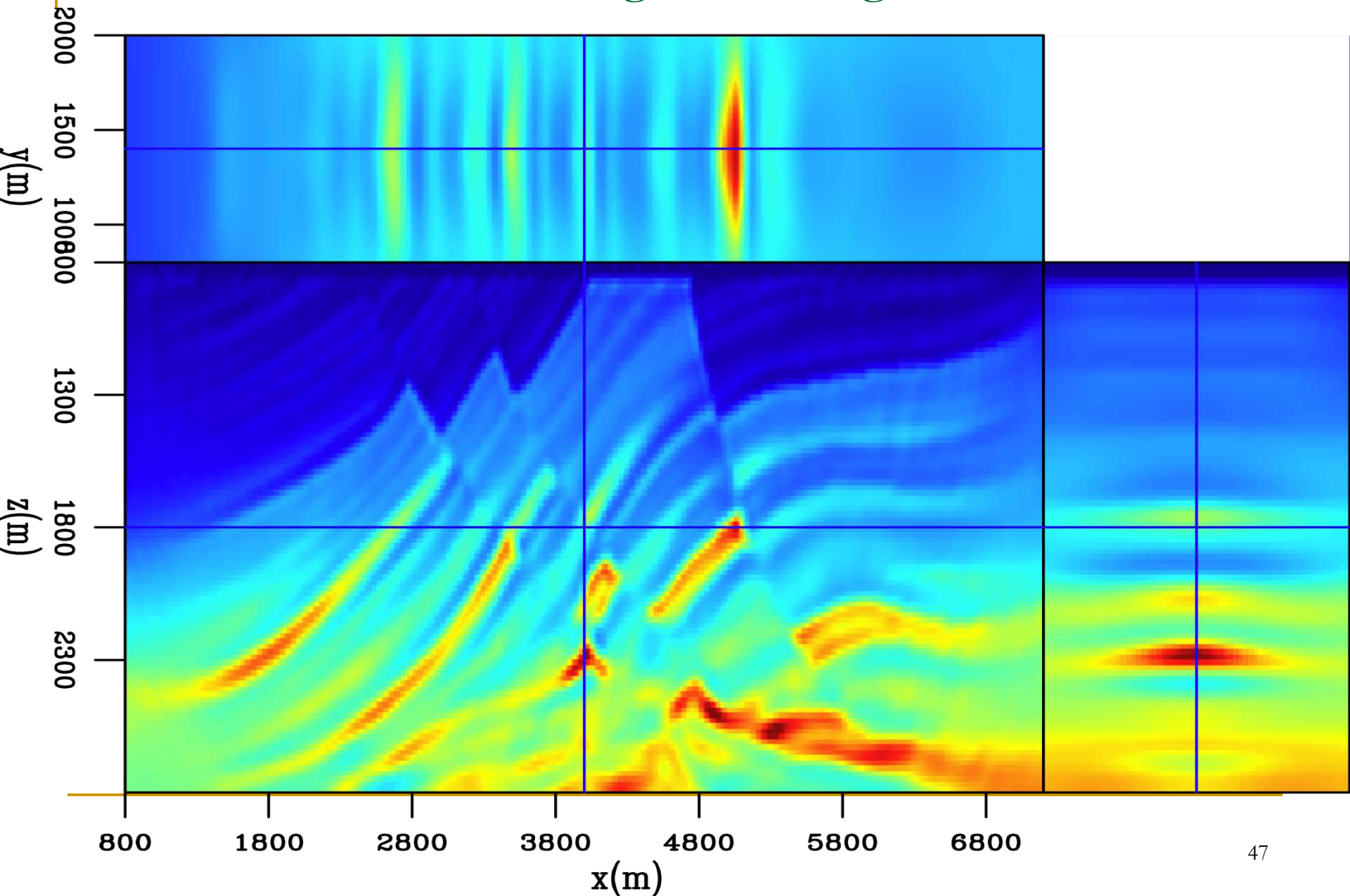
Initial velocity



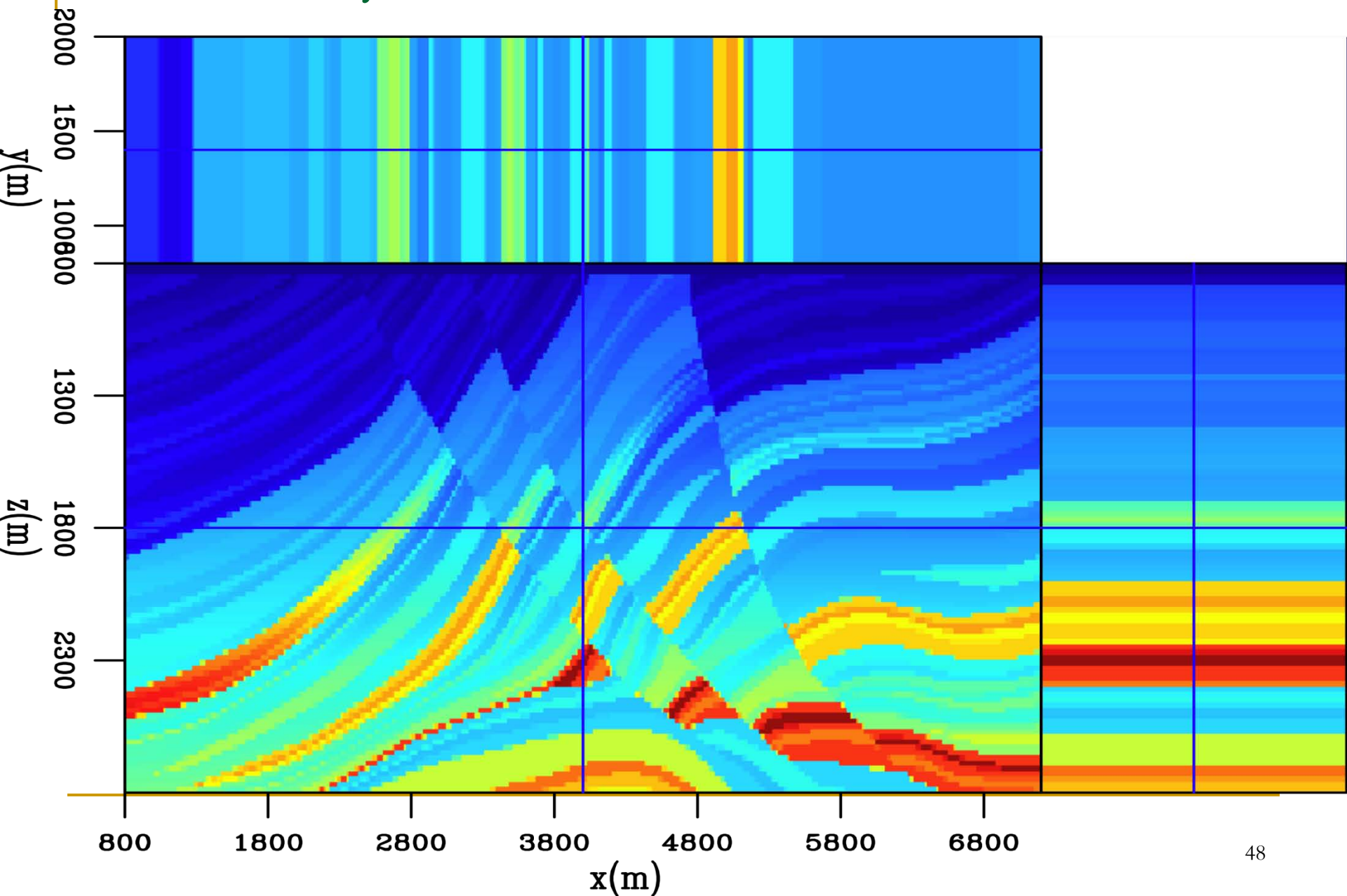
Inversion result with big cubic grain



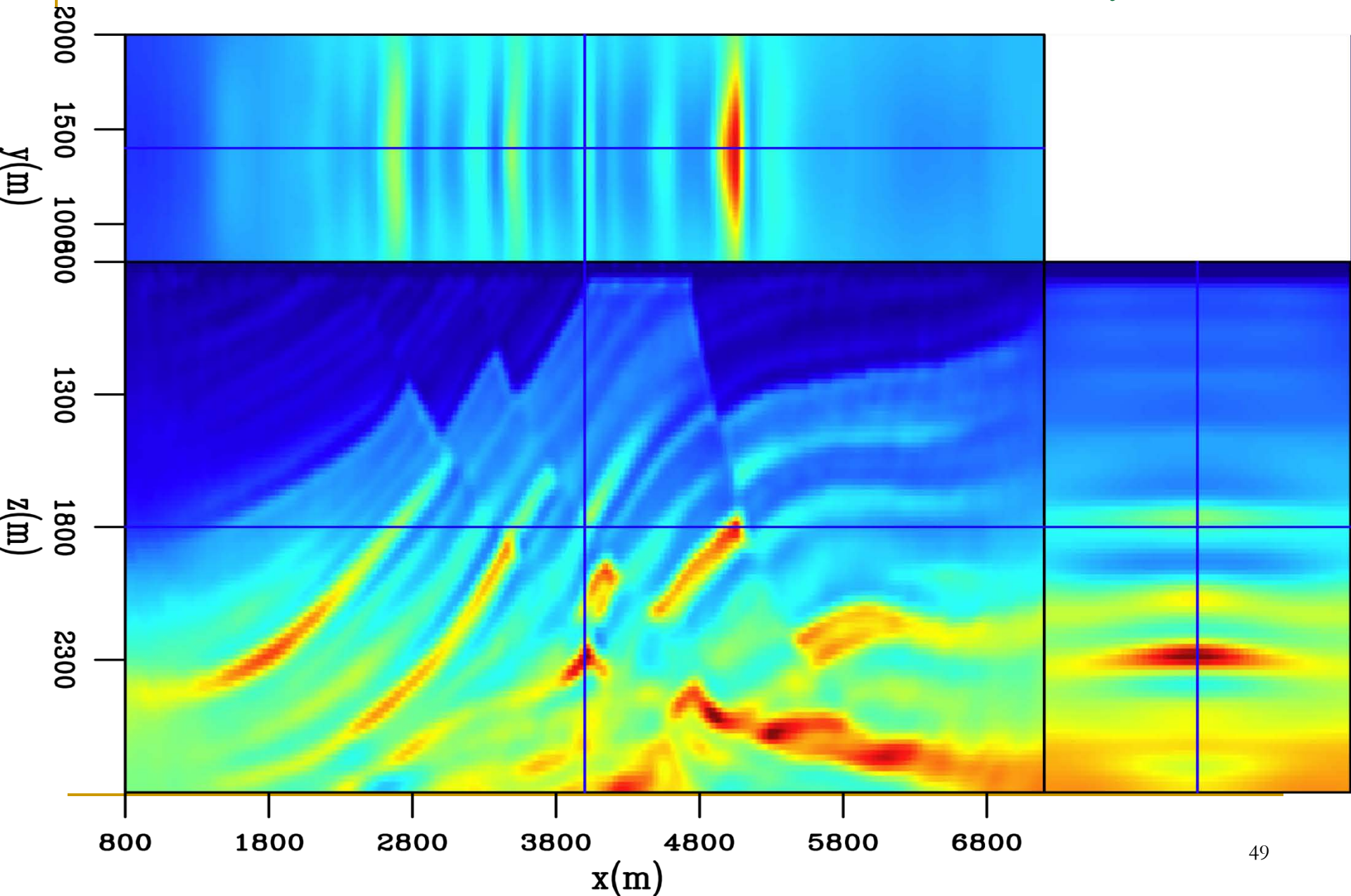
Inversion result with big random grain



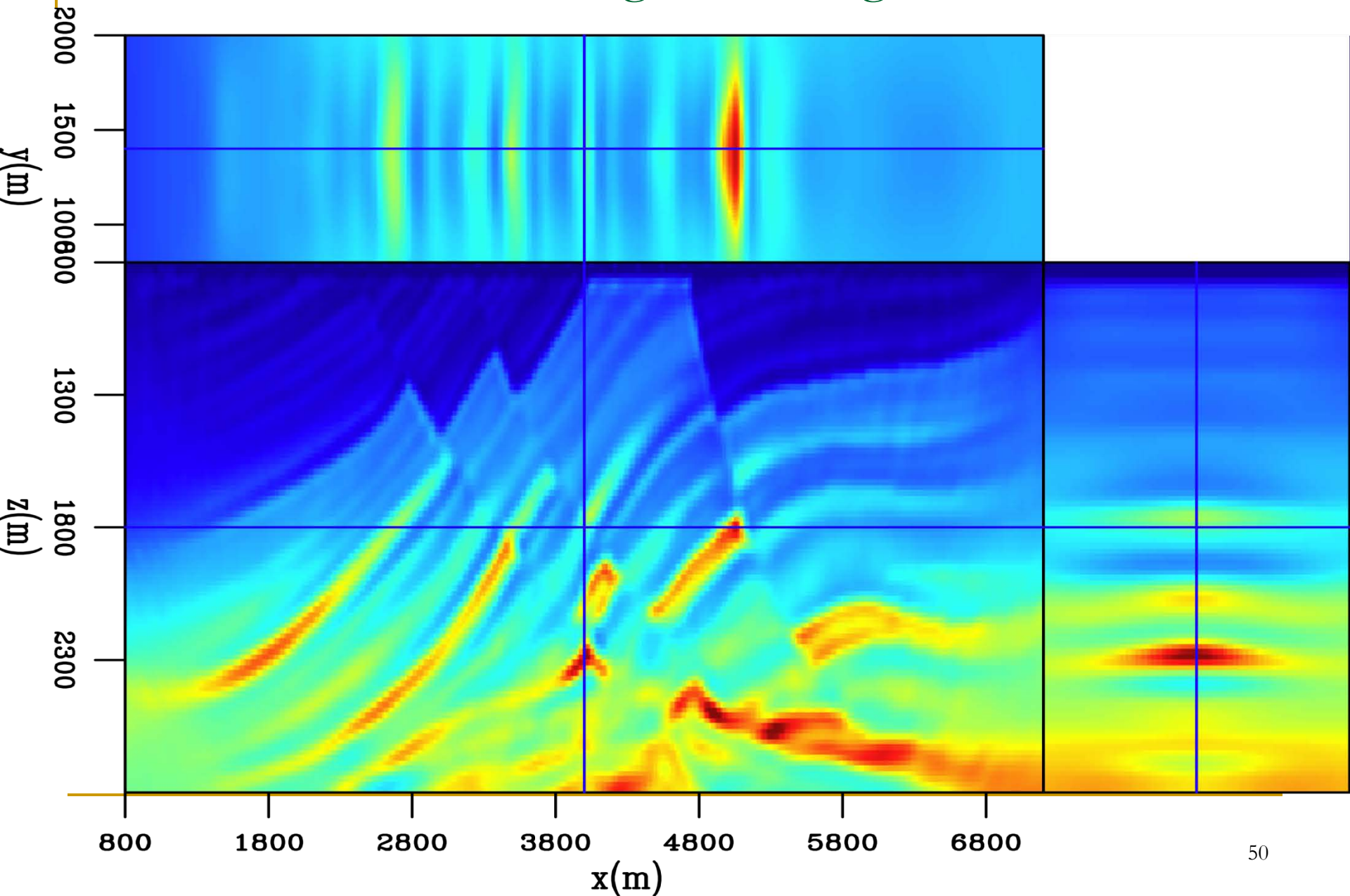
True velocity



Inversion result with continuation of velocity



Inversion result with big random grain



Why constant pad works almost equally well as random boundary in this case?

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Boundary reflection in complex synthetic does not put much artifacts in gradient

Conclusions

- Randomly-shaped grains in the random boundary effectively scatter low frequency wave without increasing the boundary size

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- Waveform inversion using random boundary works

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- Randomly-shaped grains in the random boundary effectively scatter low frequency wave without increasing the boundary size
- Waveform inversion using random boundary works
- Whether using continuation of velocity works in complex synthetic/real data is to be determined

Thank you

Questions & Suggestions

pseudo code for gradient calculation using random boundaries:

```
{  
  generate  $d_{cal}$  using absorbing boundary  
   $d_{res} = f(d_{obs}, d_{cal})$   
  for  $t = 0, t_{max}$   
    propagate the same source using random boundary  
  for  $t = t_{max}, 0$   
    propagate source and residual wavefield, generate gradient  
}
```

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    propagate the same source using random boundary  
  for  $t = t_{max}, 0$   
    propagate source and residual wavefield, generate gradient  
}
```

4 propagations instead of 2, but avoid saving wavefield.

Can be further optimized by simultaneous encoding of residual/source wavefield